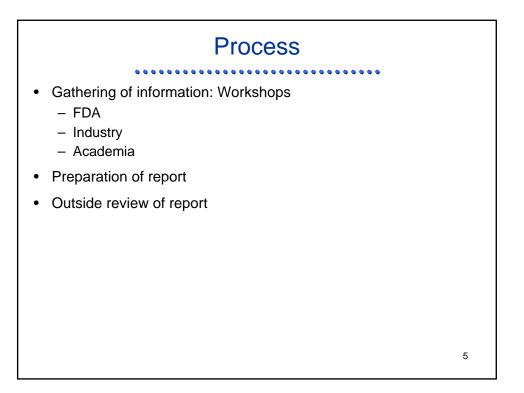
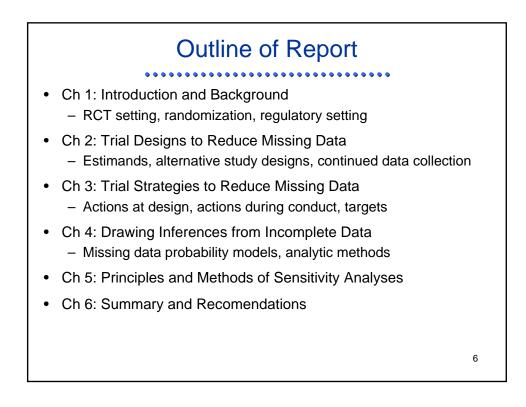
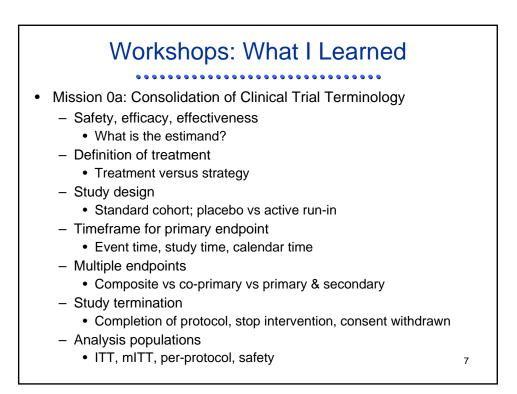
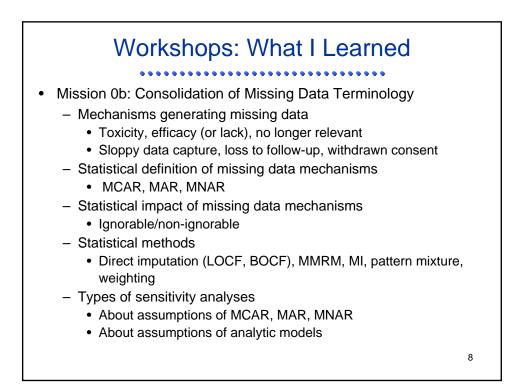


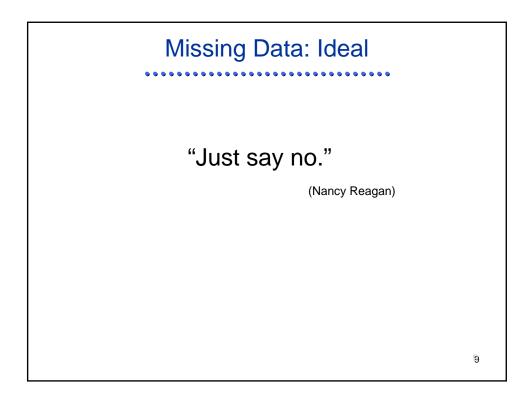
	perts in missing data meth	t Committee	
me	thodology		
	Roderick Little, Chair		
	Ralph D'Agostino	Susan Murphy	
	Kay Dickersin	James Neaton	
	Scott Emerson	Andrea Rotnizky	
	John Farrar	Daniel Scharfstein	
	Constantine Frangakis	Weichung (Joe) Shih	
	Joseph Hogan	Jay Siegel	
	Geert Molenberghs	Hal Stern	

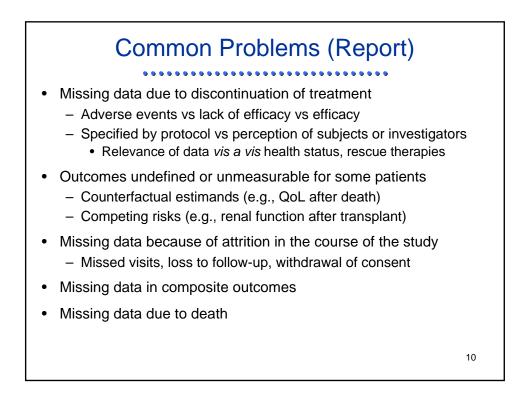


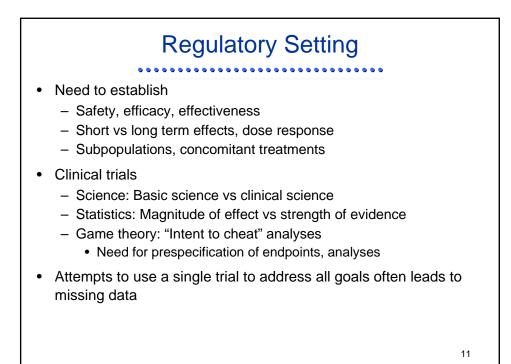


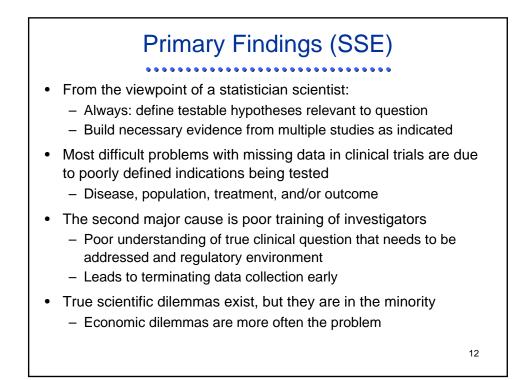




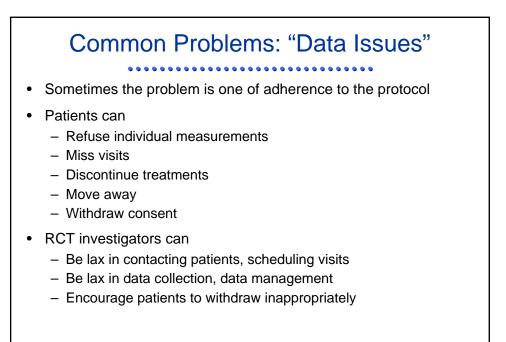


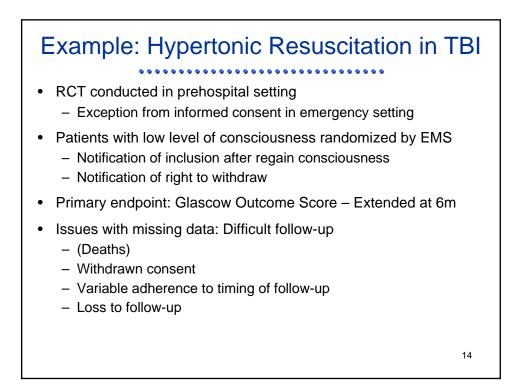


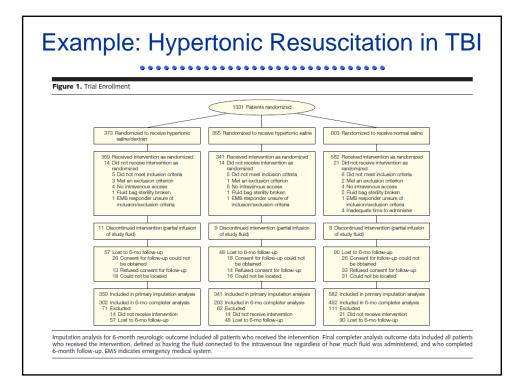


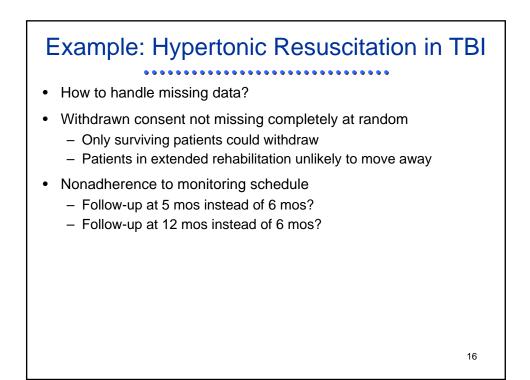


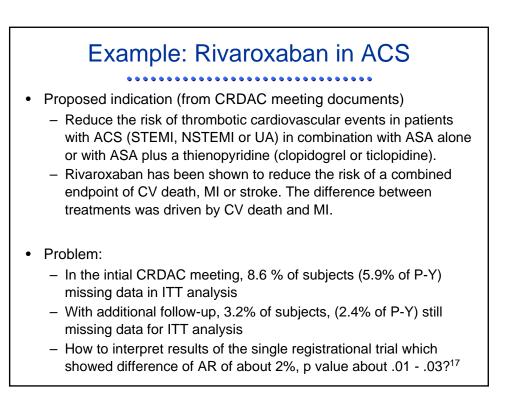
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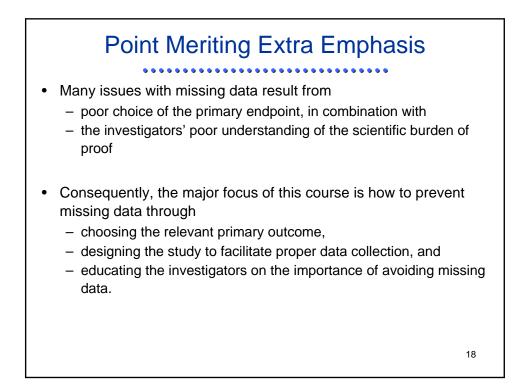


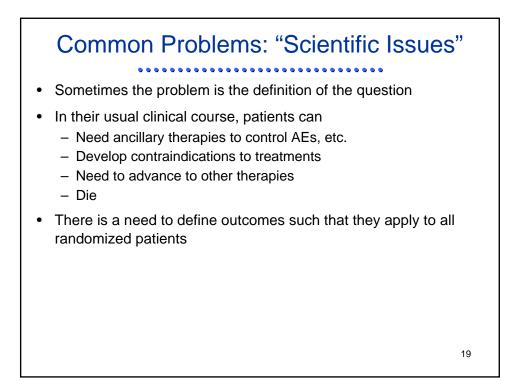


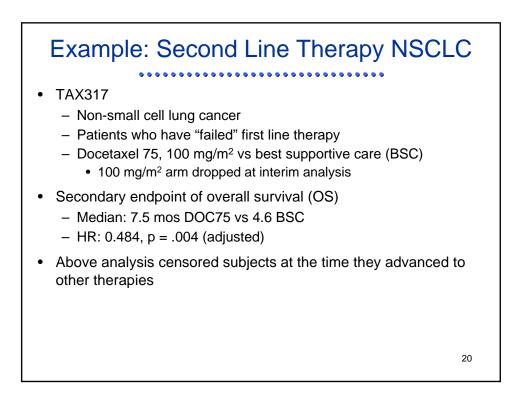


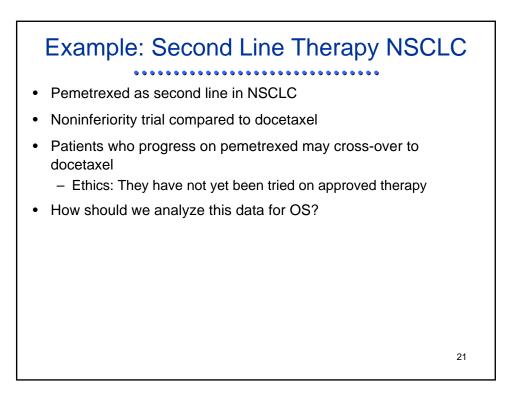


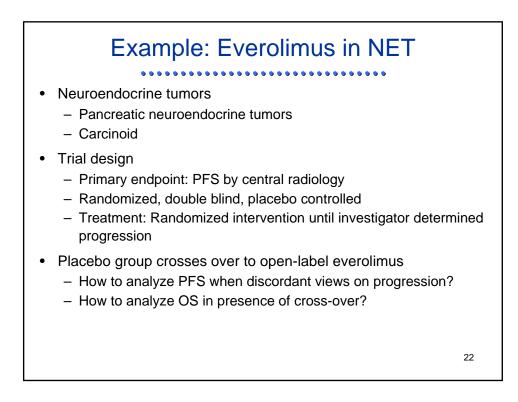


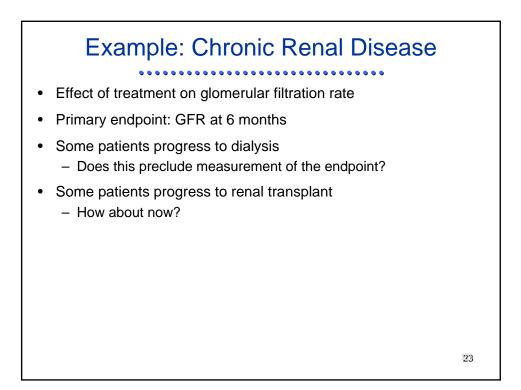


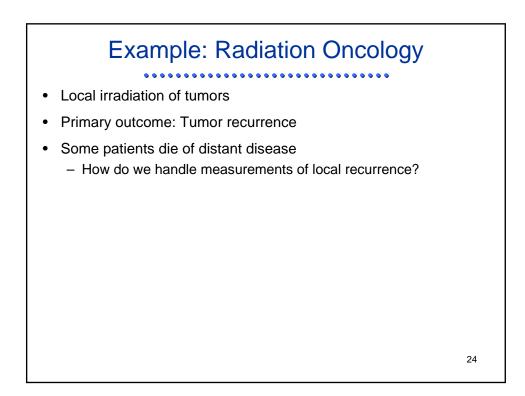




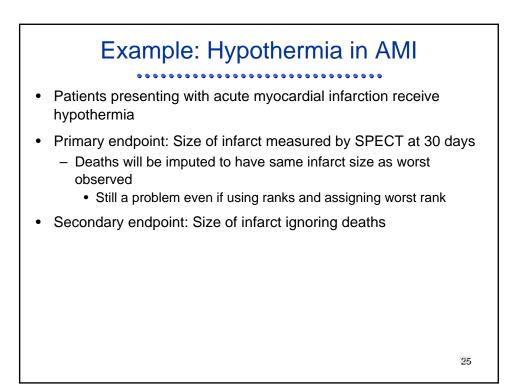


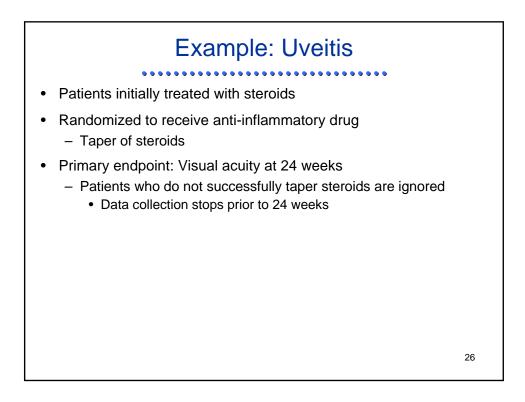


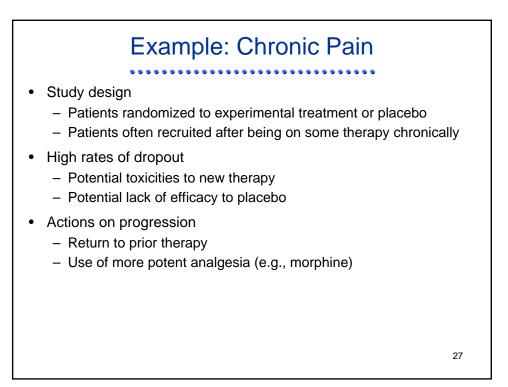


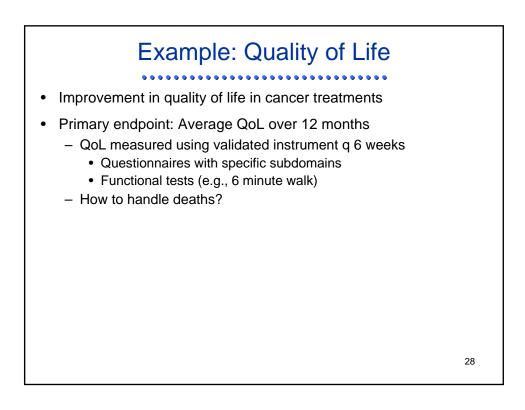


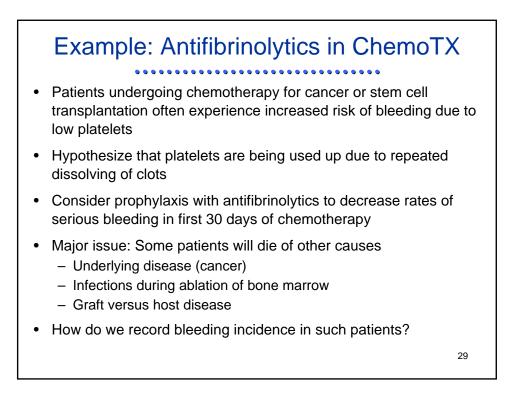
Module 3: Missing Data in RCT Scott S. Emerson, M.D., Ph.D.

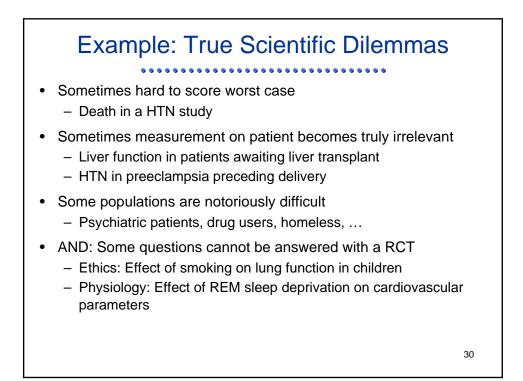


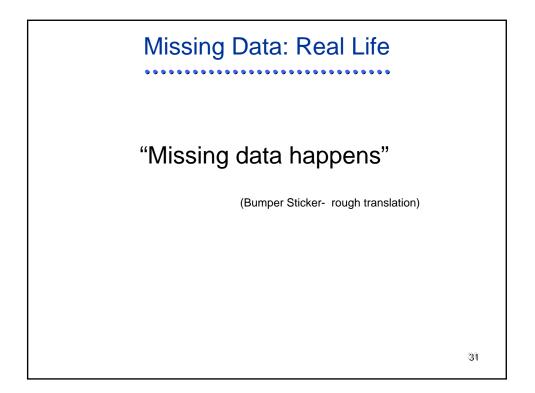


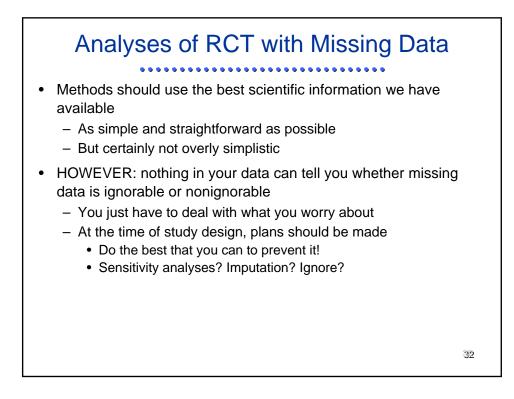


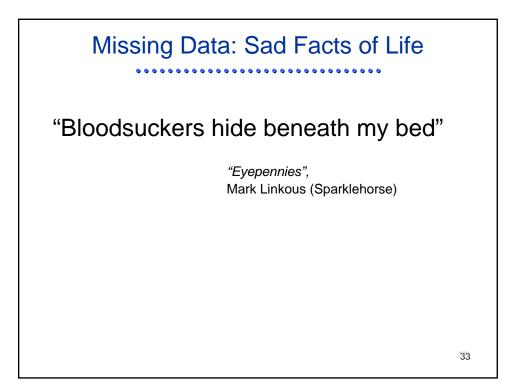


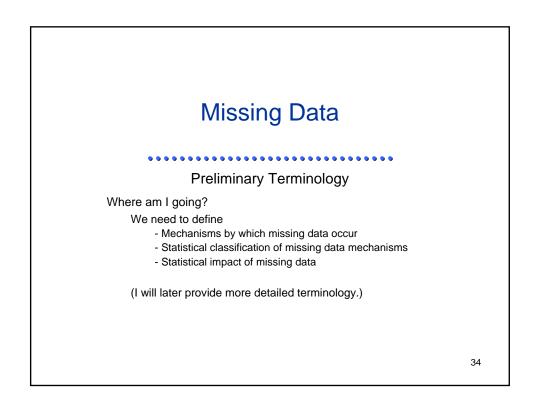


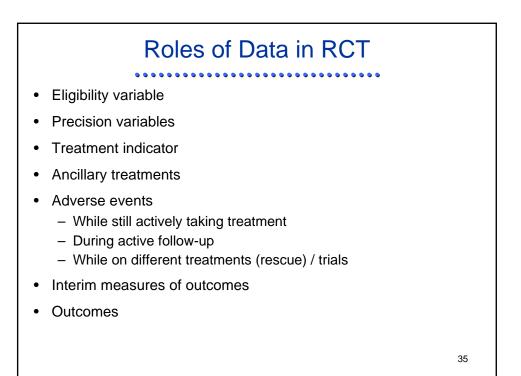


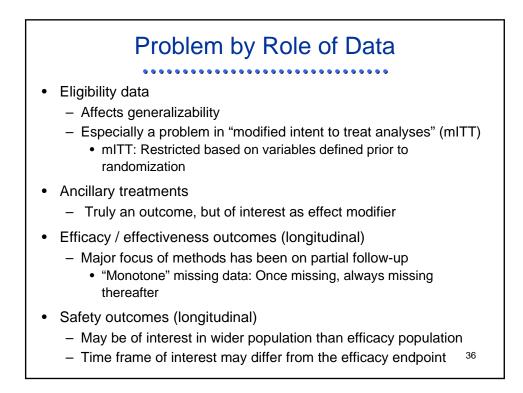


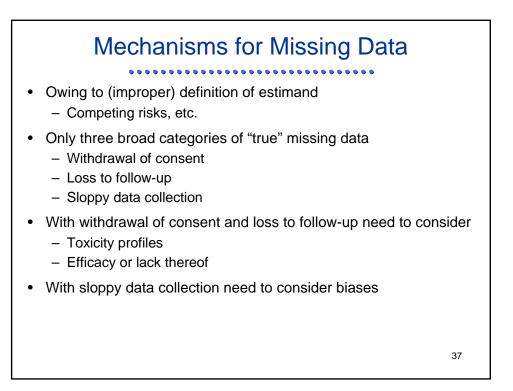


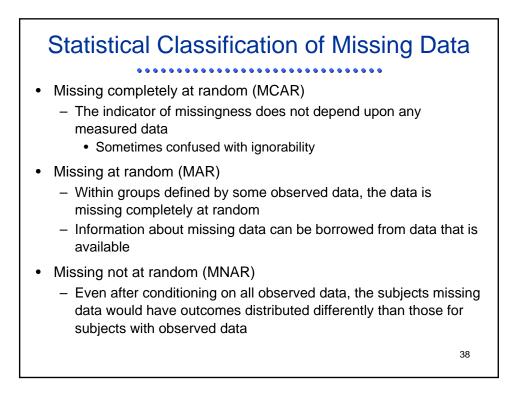


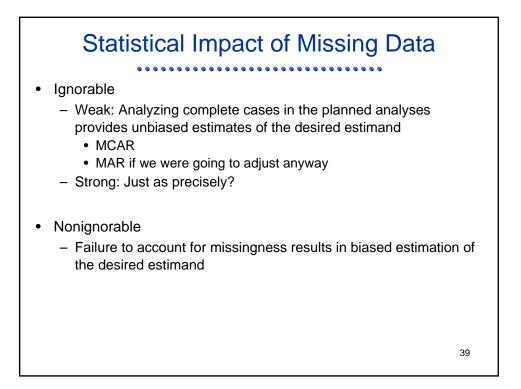


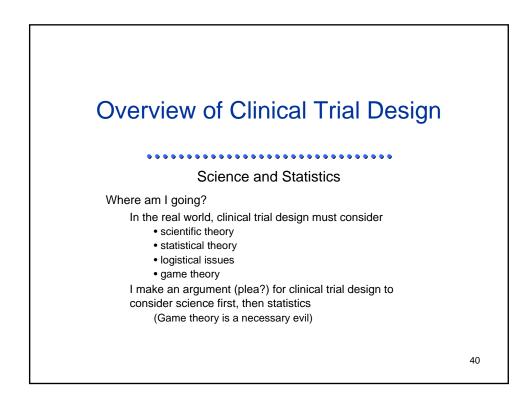


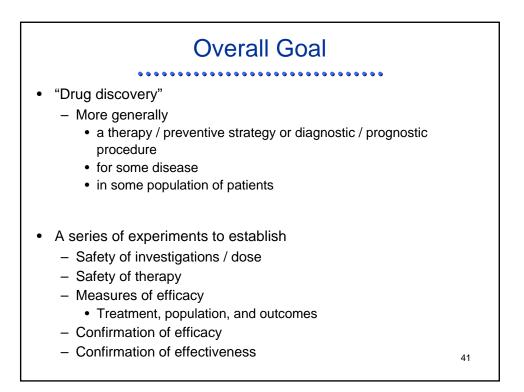


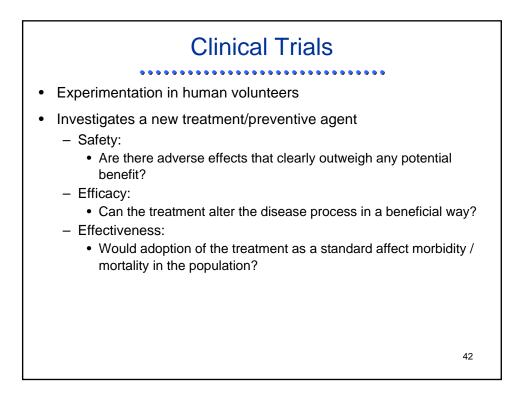


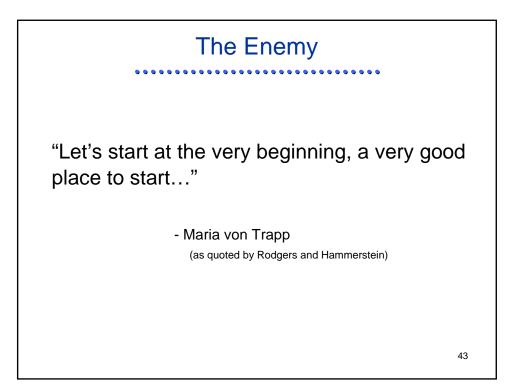


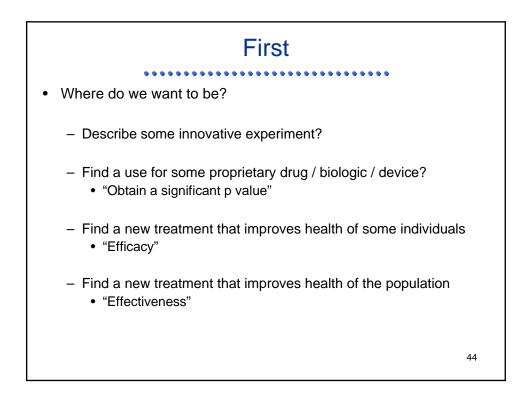


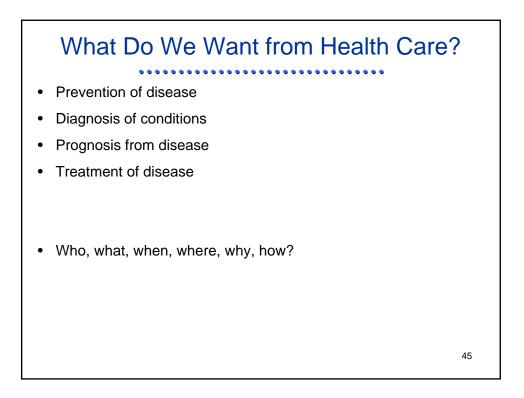


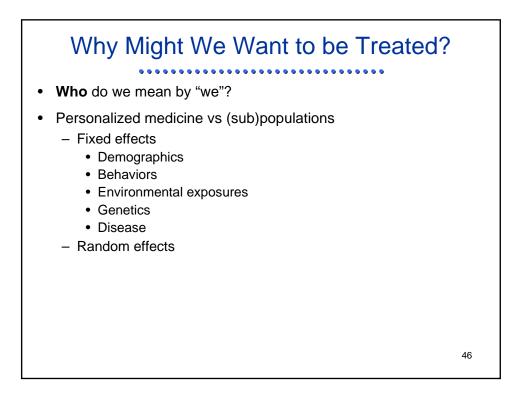




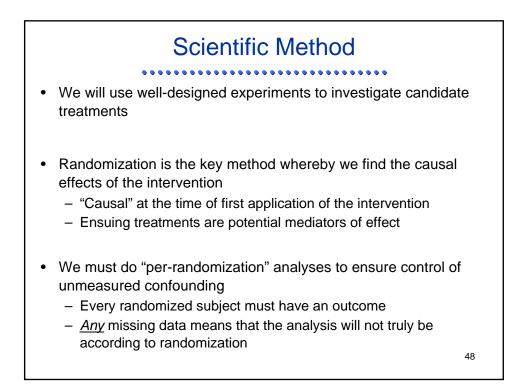


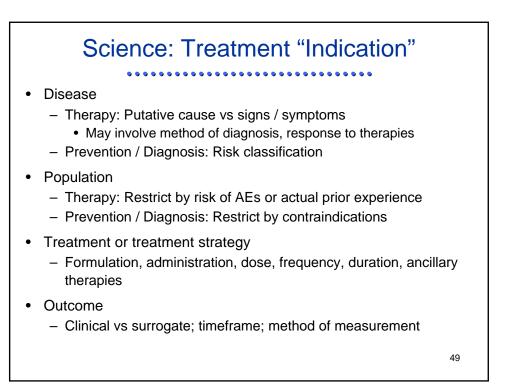


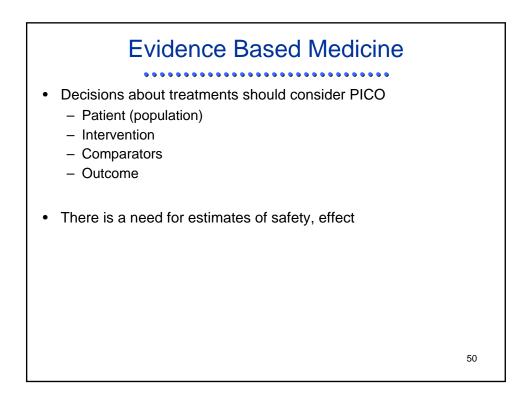








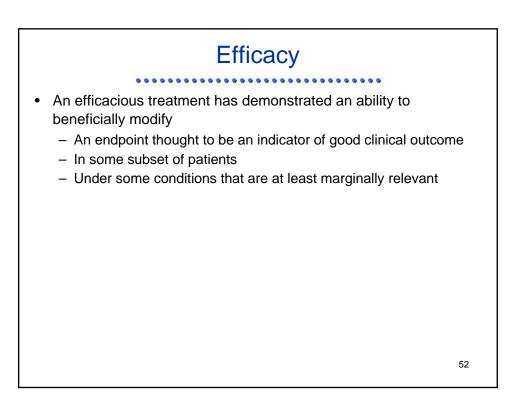


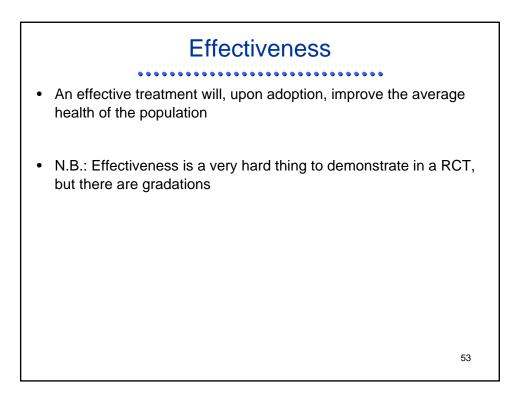


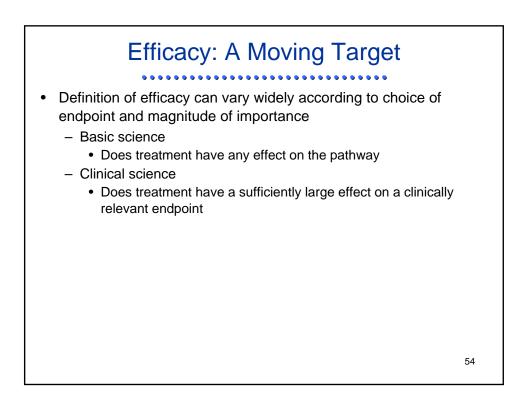
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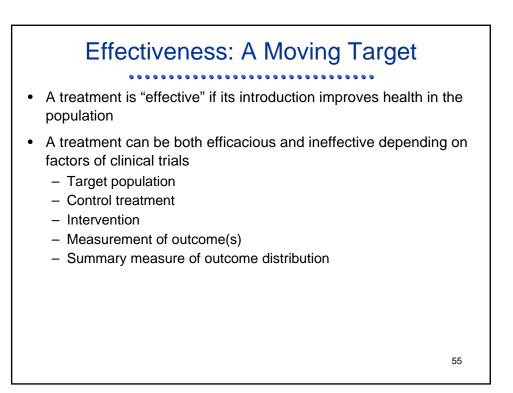


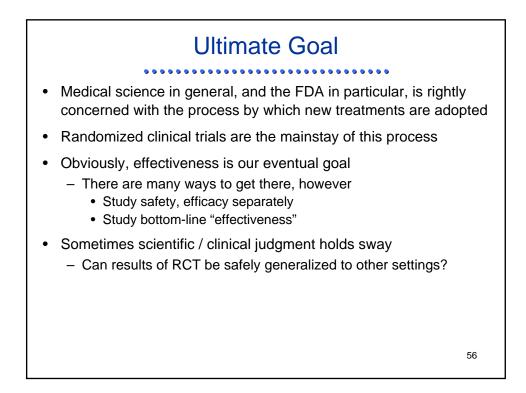
- Multiple levels of concern
- Safety of conducting RCTs
 - Phase I dose finding studies
- Safety in the ideal population
 - Phase II or phase III efficacy studies
- Safety in the general population
 - Phase III effectiveness studies
 - Vulnerable populations
 - Concomitant renal, liver disease
 - Expansion of indication to patients with little benefit
 - Changes in behavior associated with adoption
 - Rare but serious adverse events

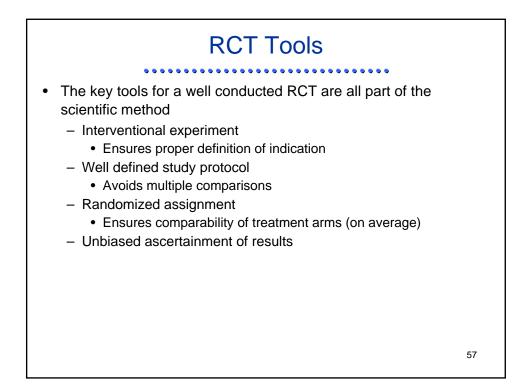


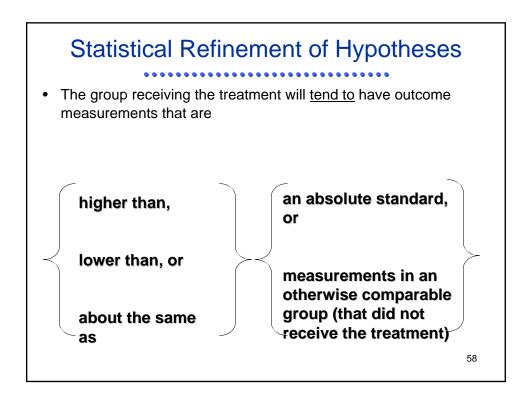


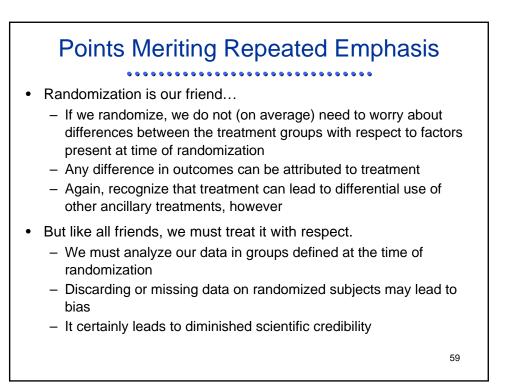


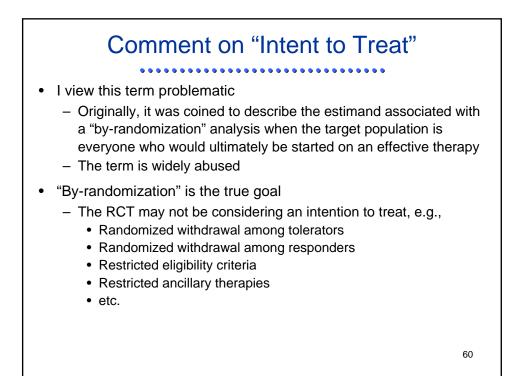


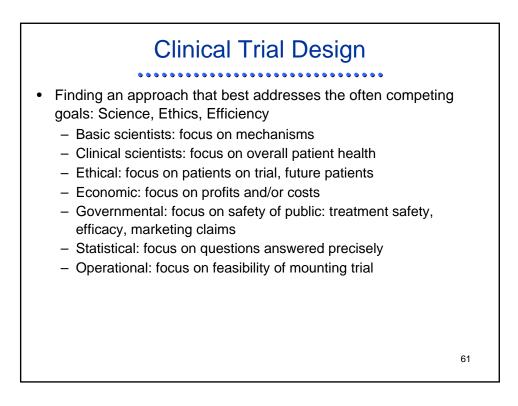


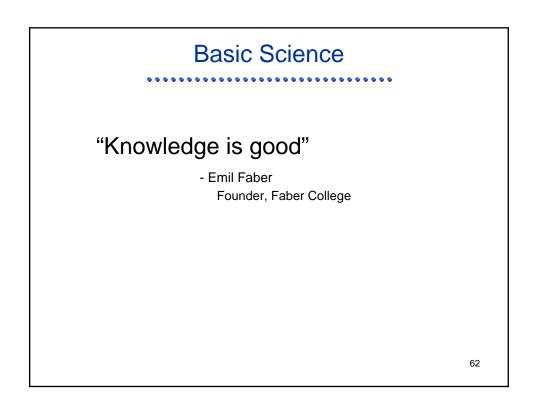




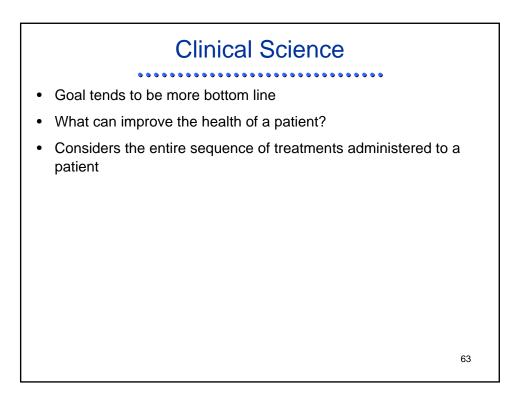


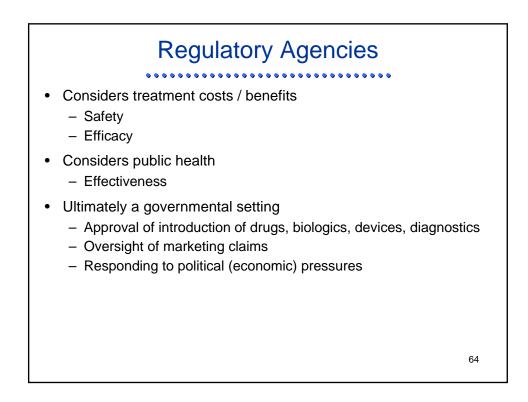


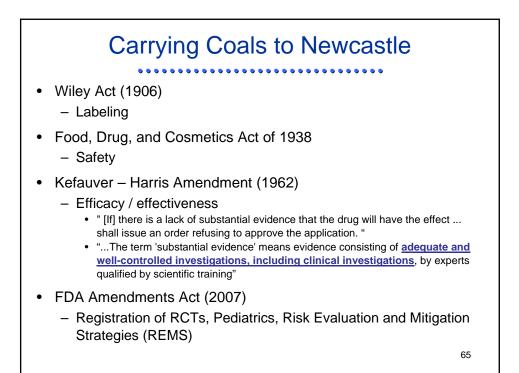


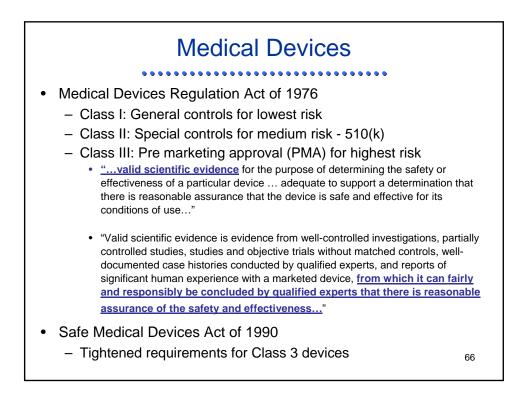


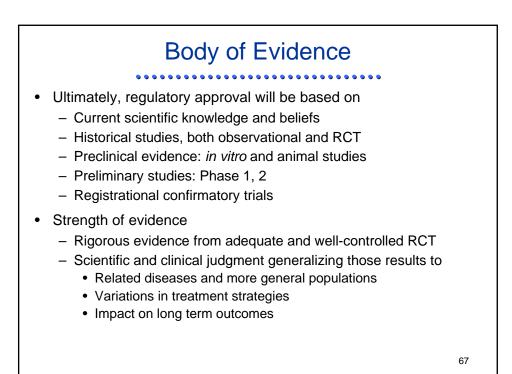
Module 3: Missing Data in RCT Scott S. Emerson, M.D., Ph.D.

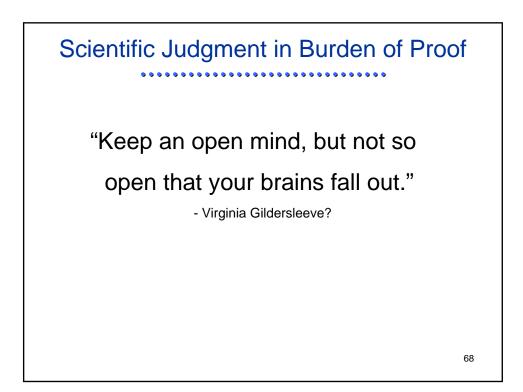


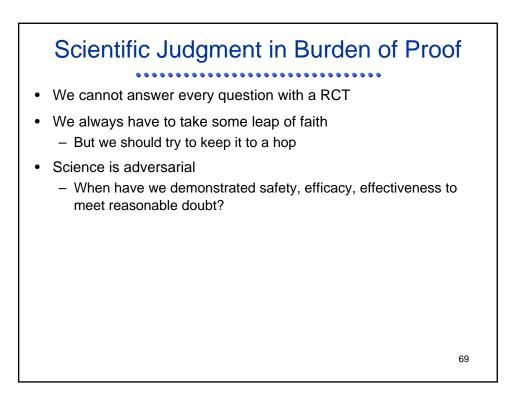


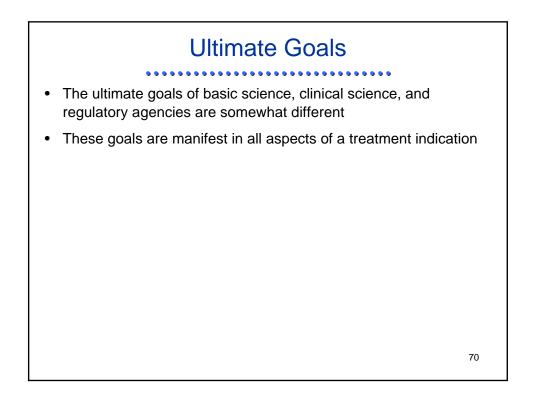


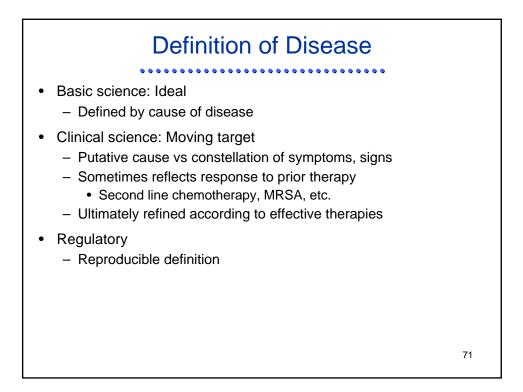


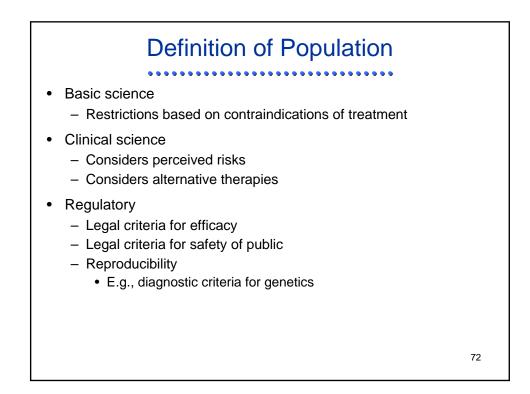


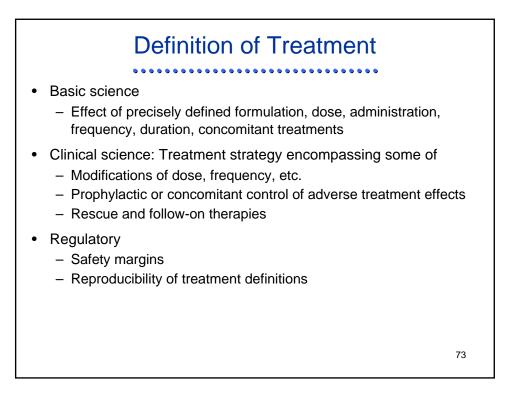


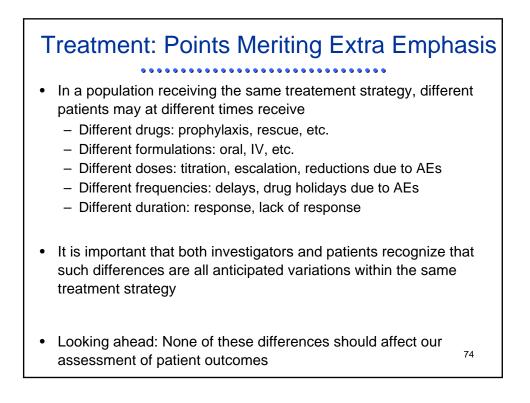


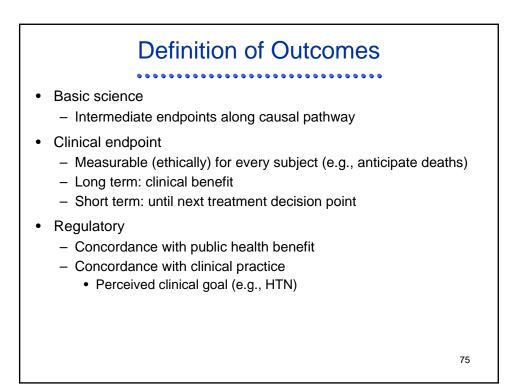


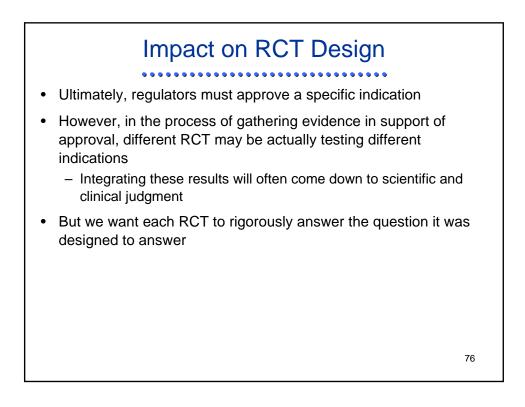


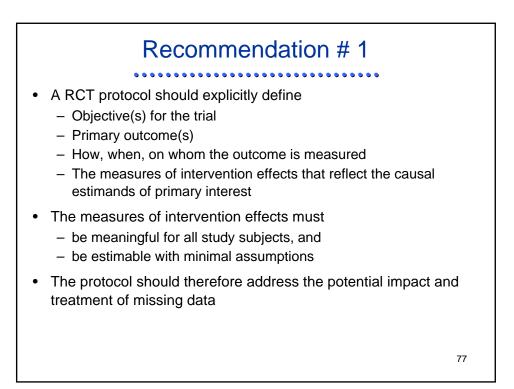


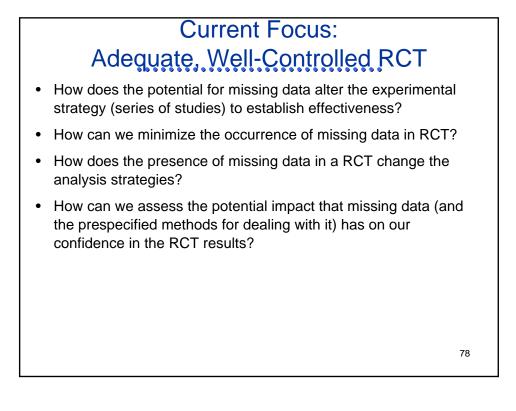


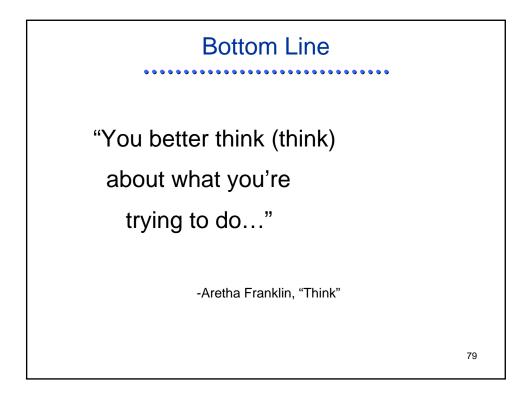


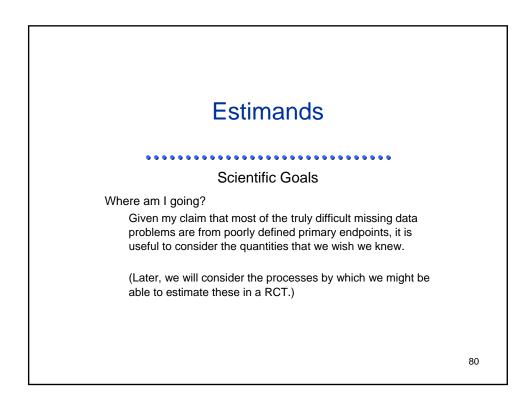


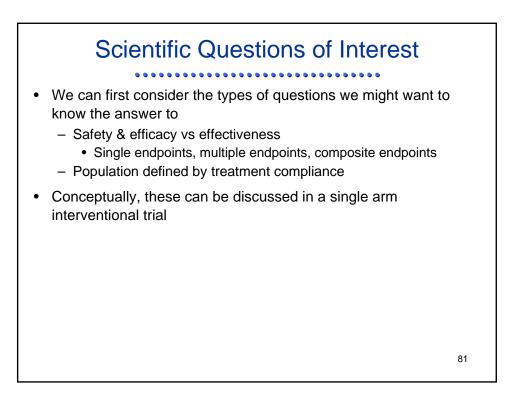




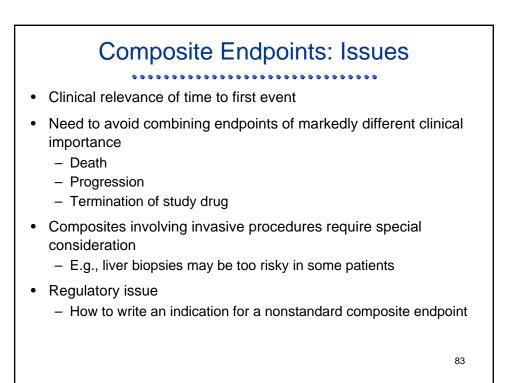


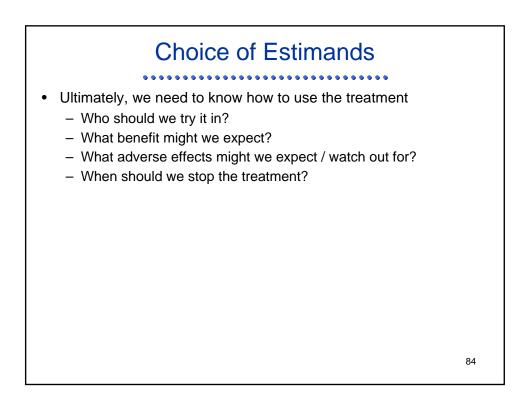


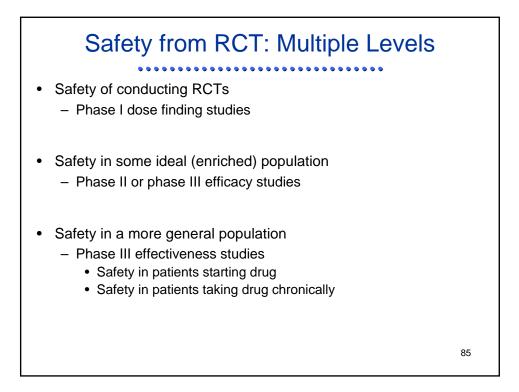


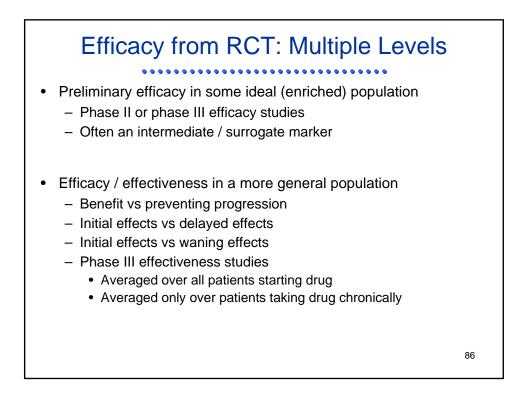


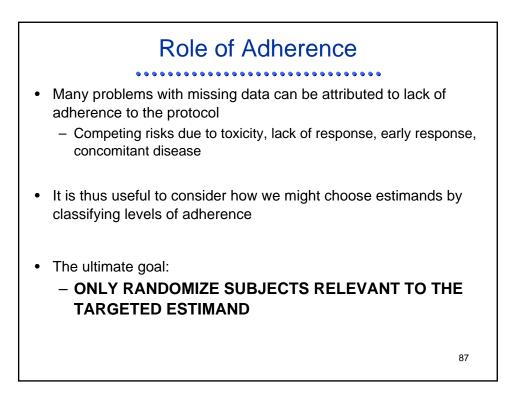


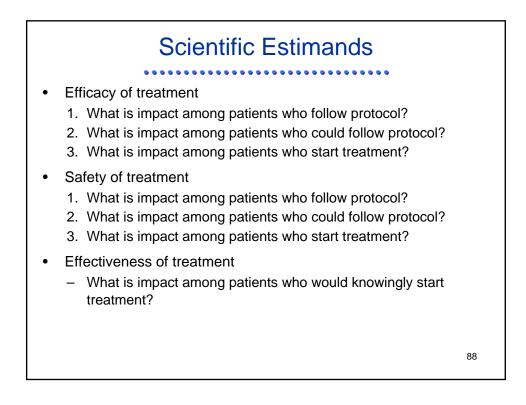


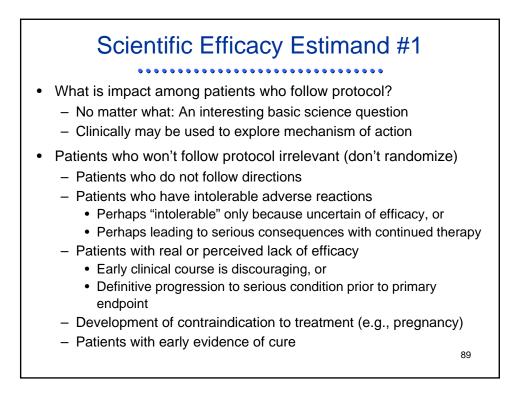


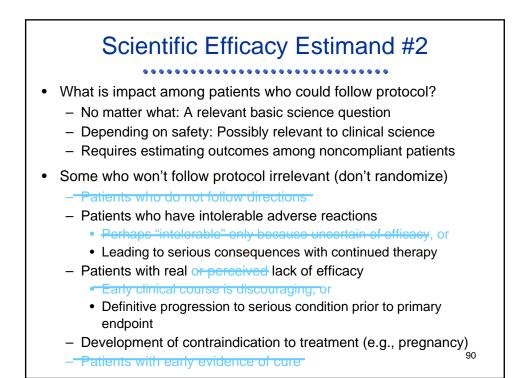


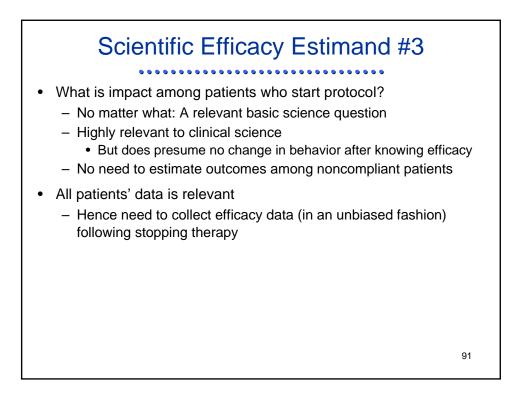


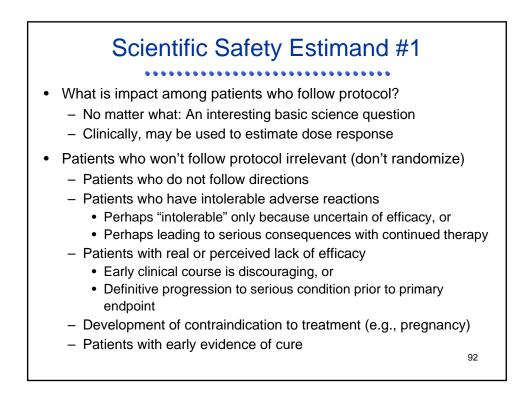


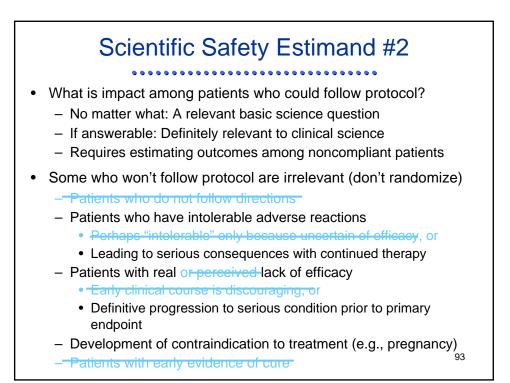


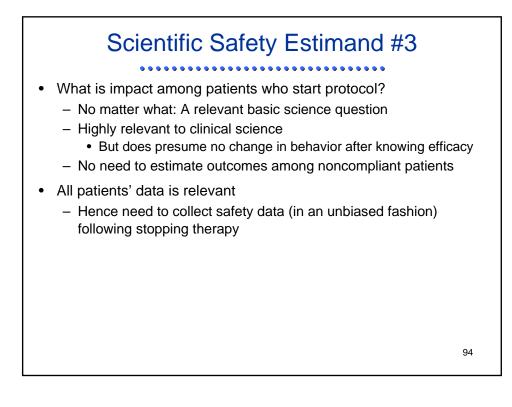


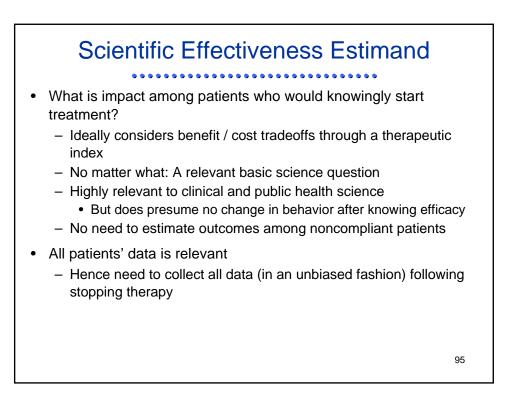


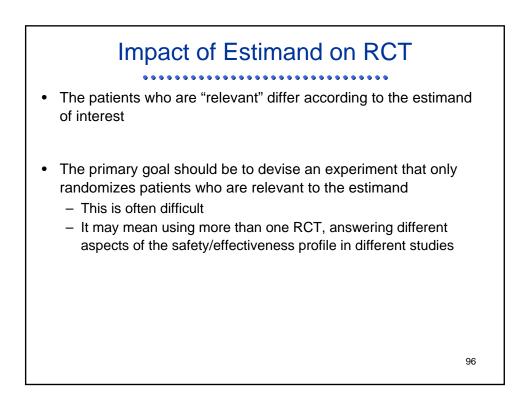


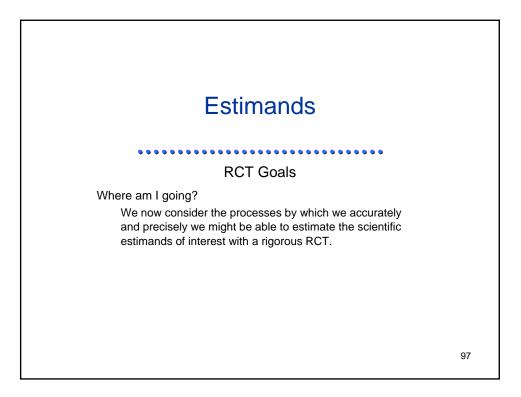


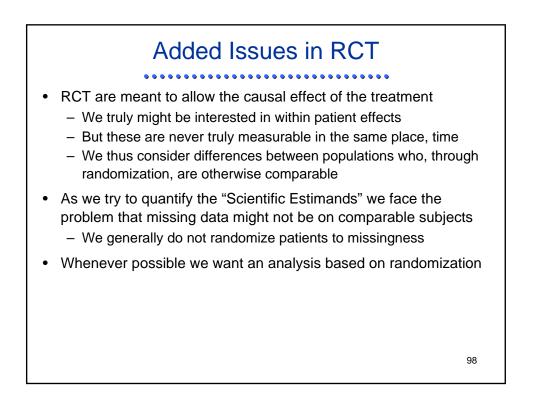


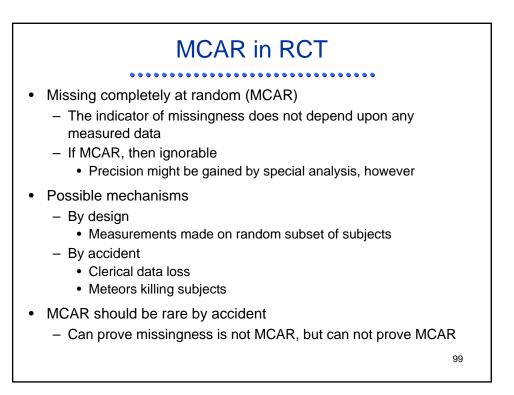


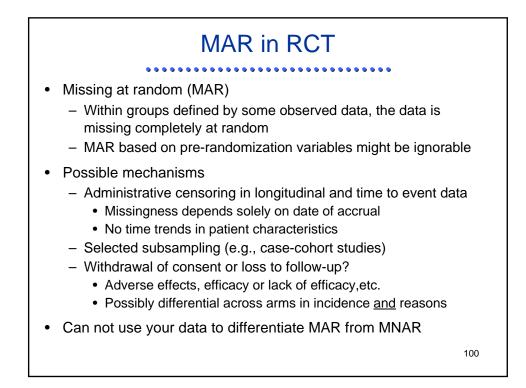


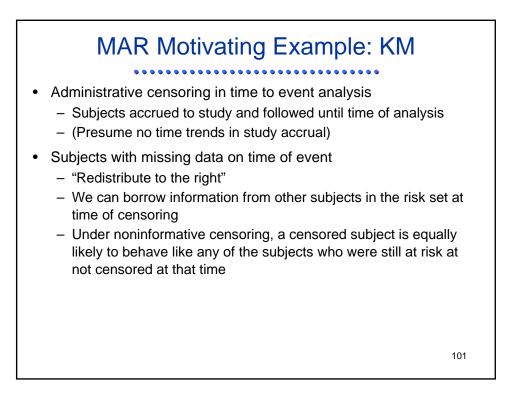


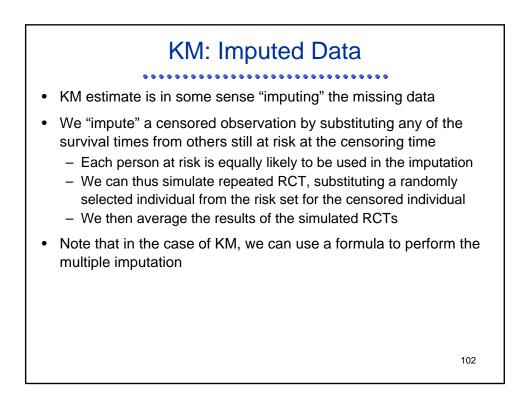


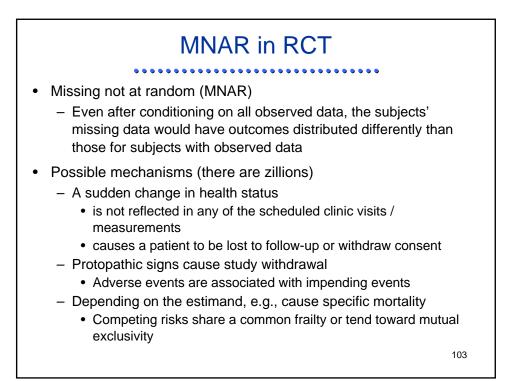


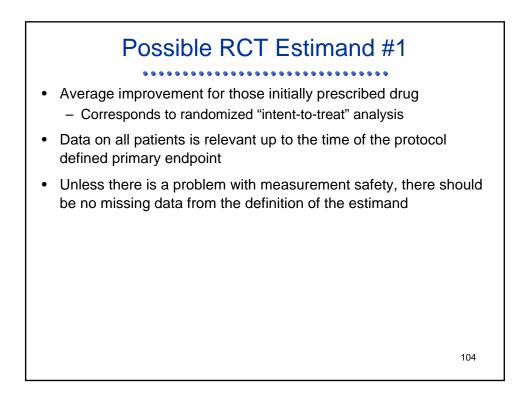


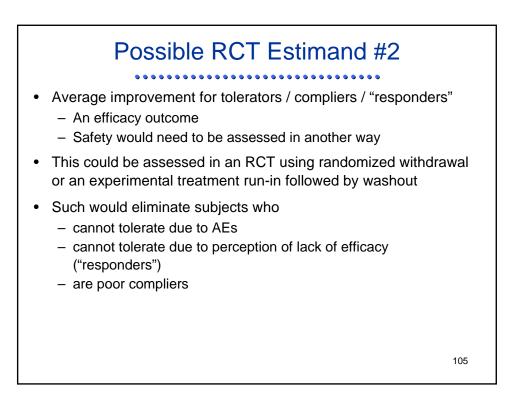


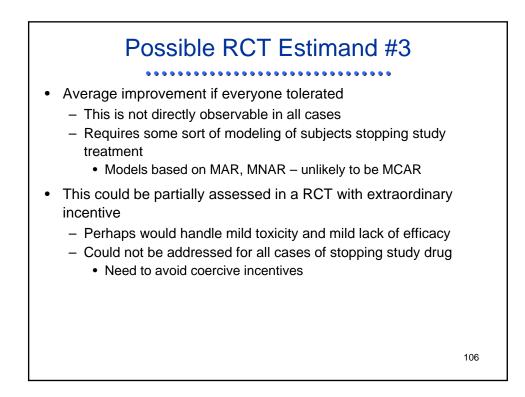


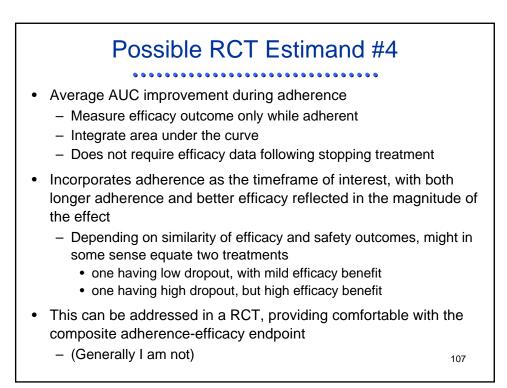


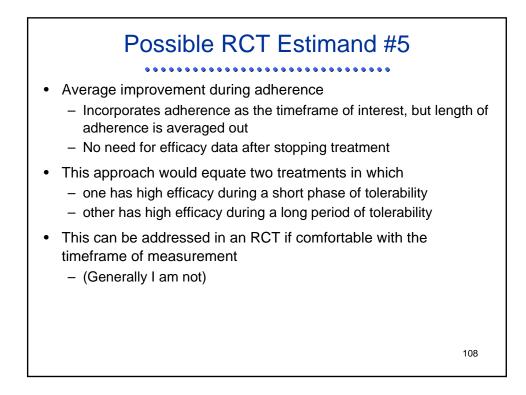


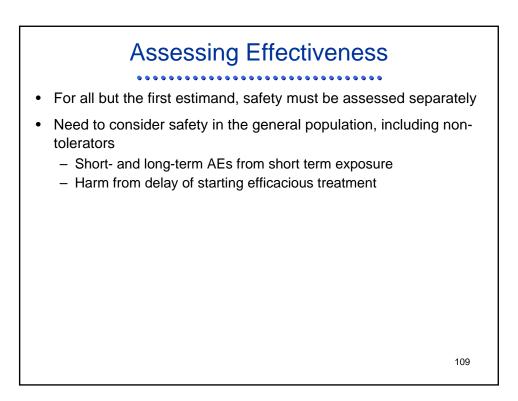


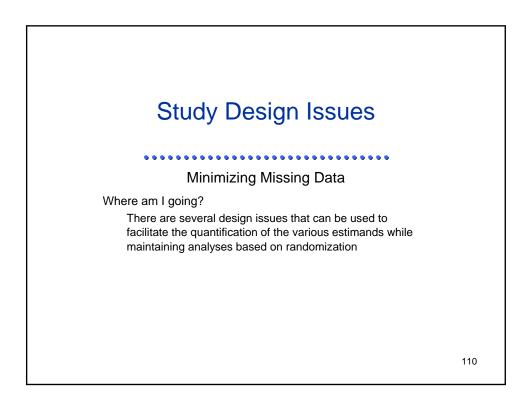


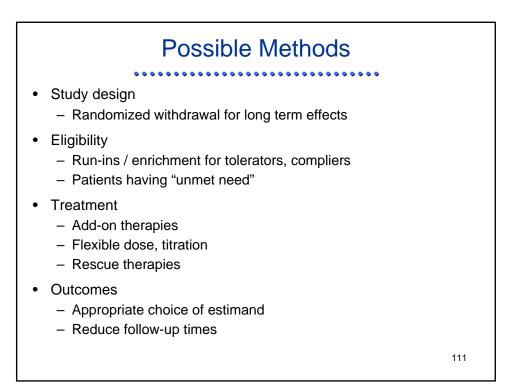


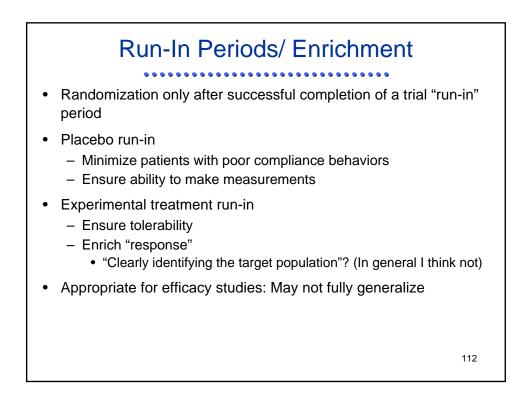


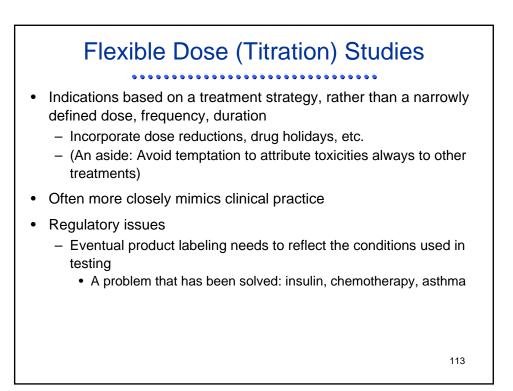


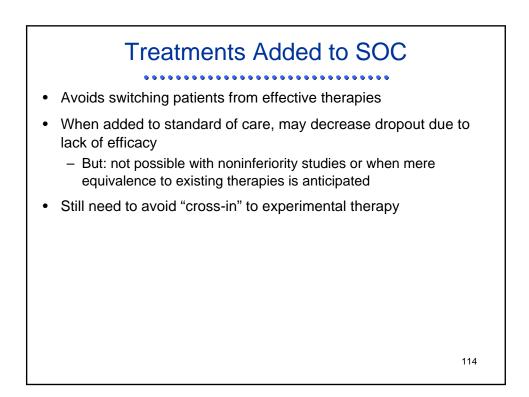


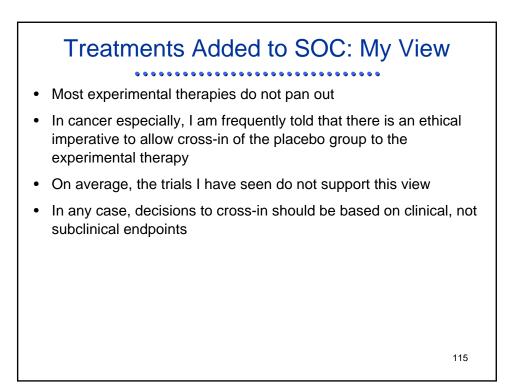


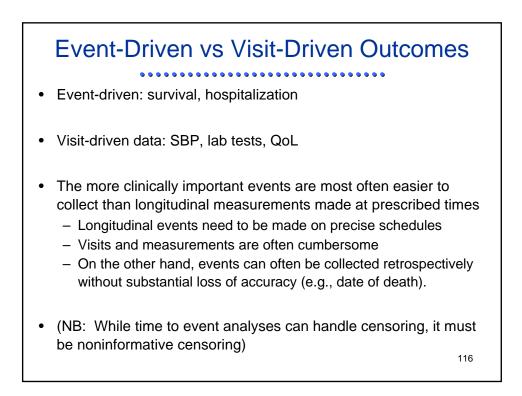


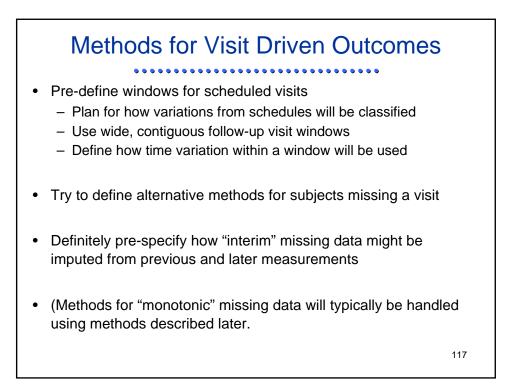


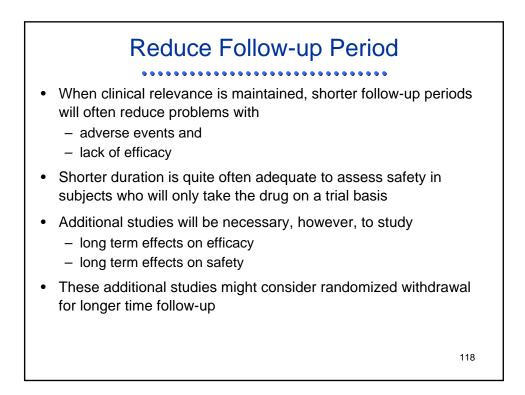


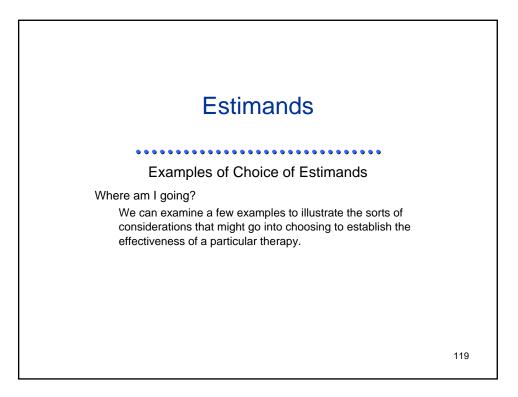


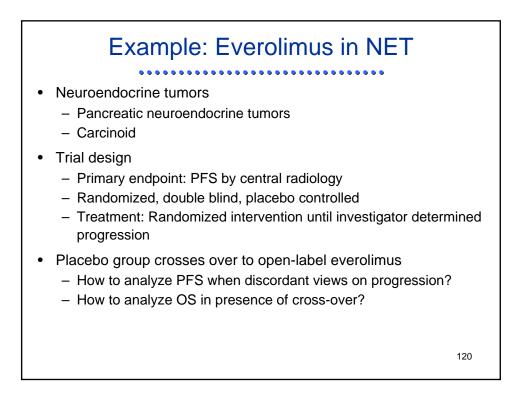


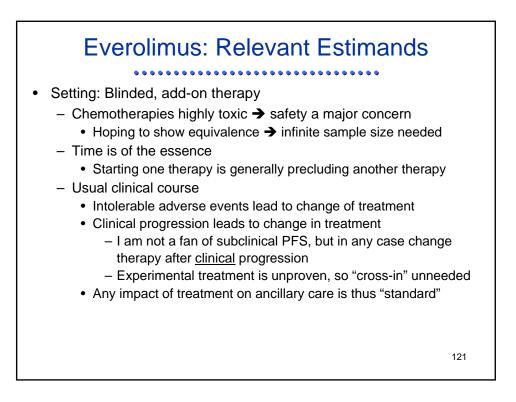


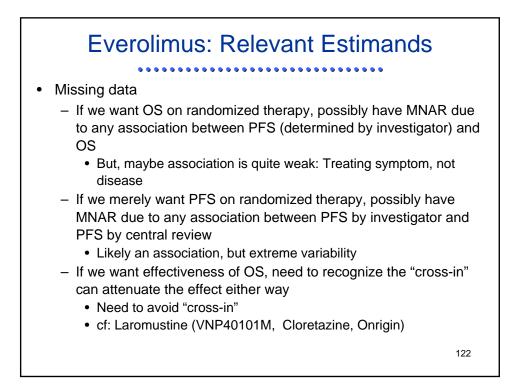


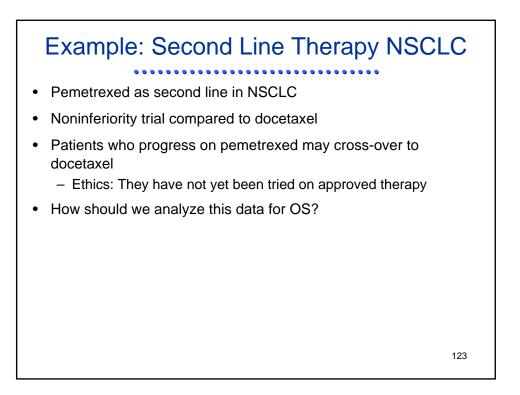


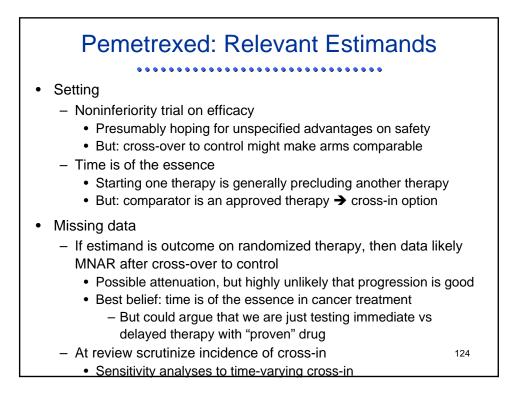


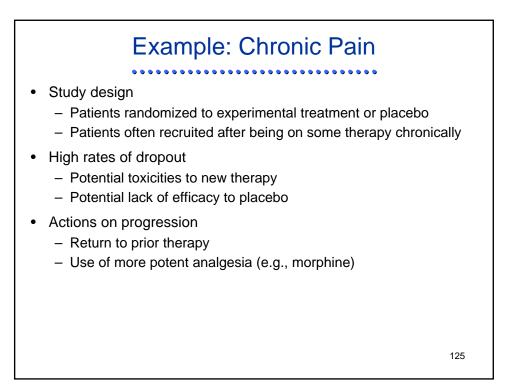


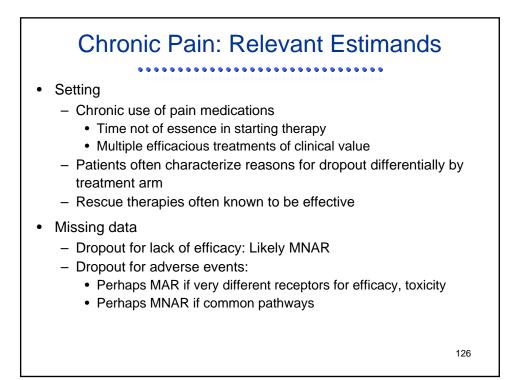


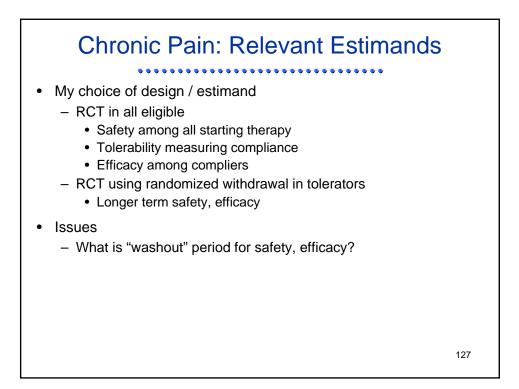


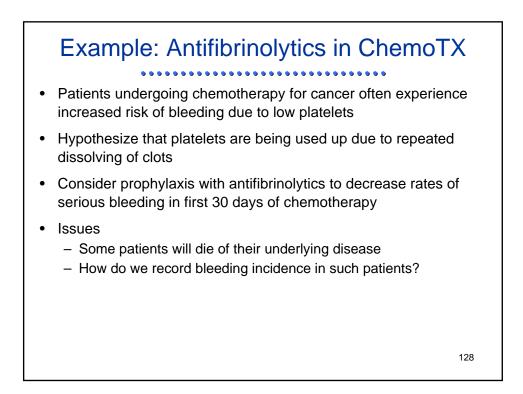


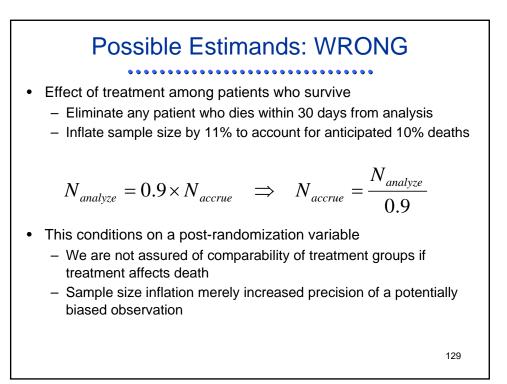


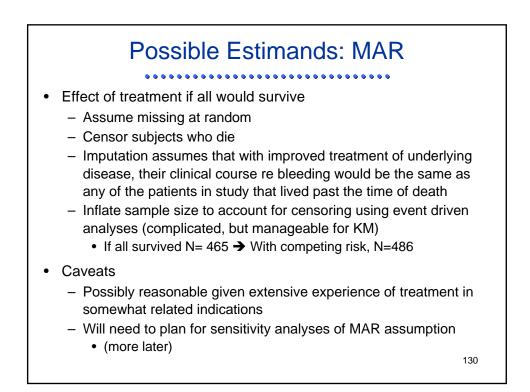


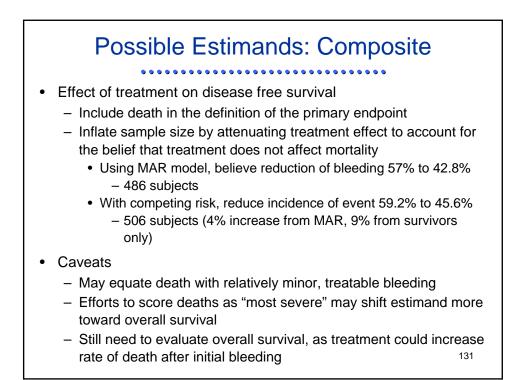


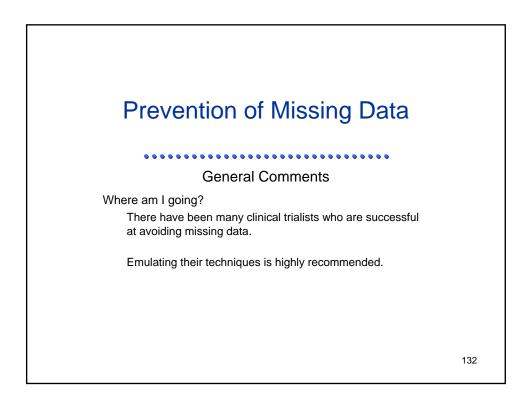


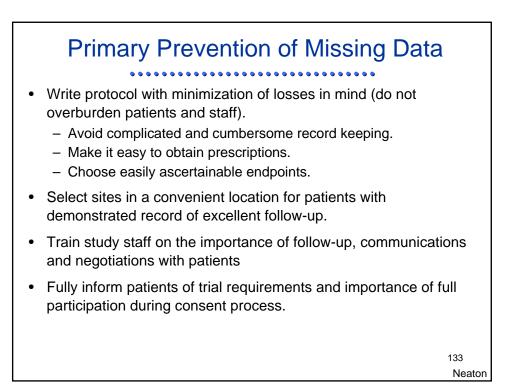


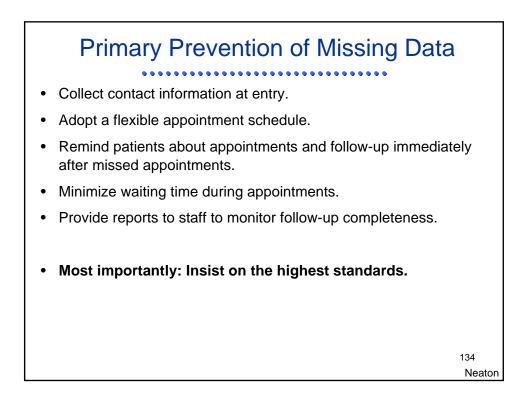


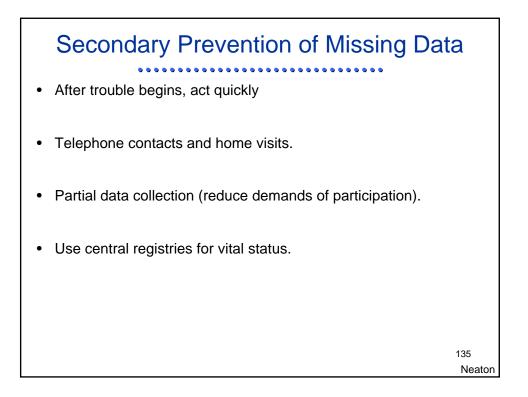


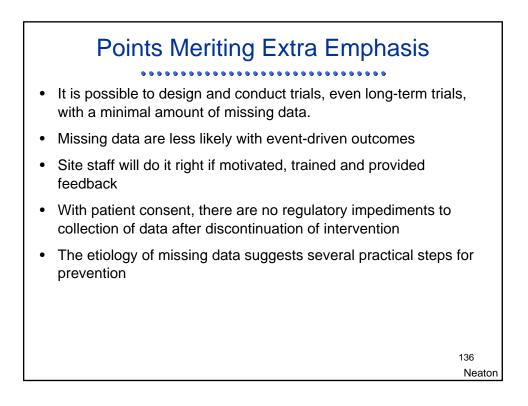


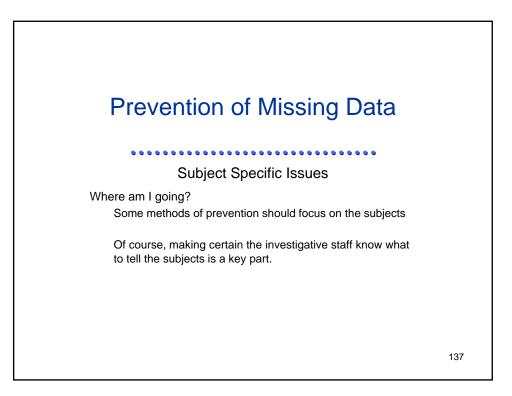


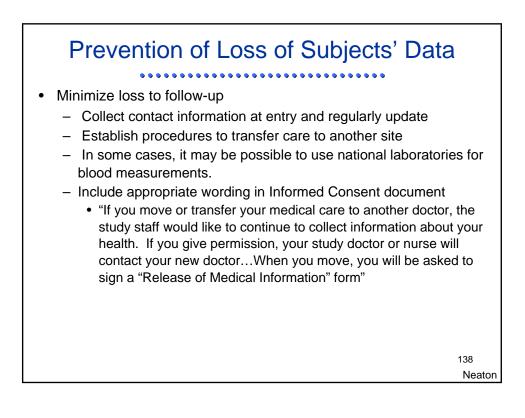


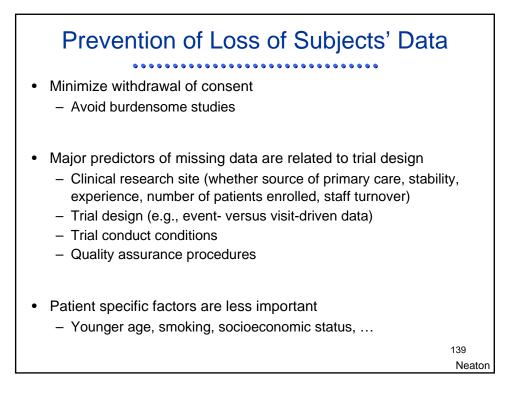


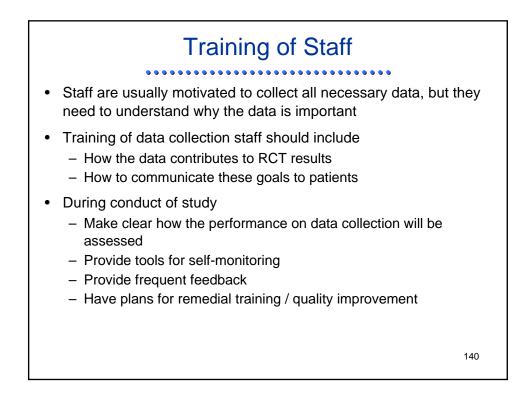


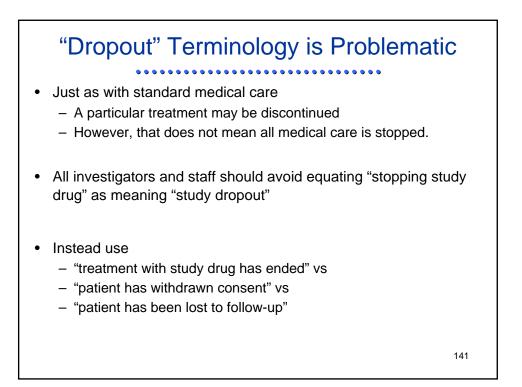


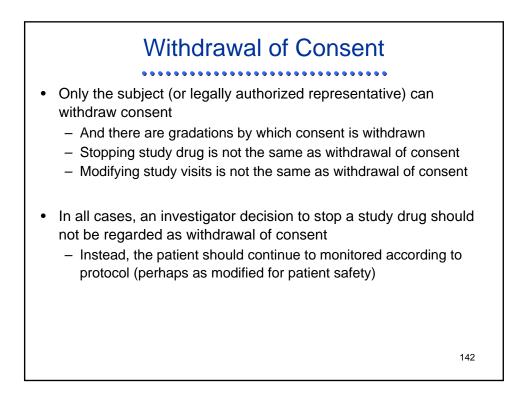


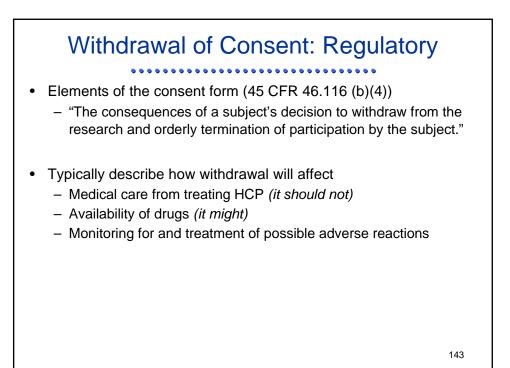


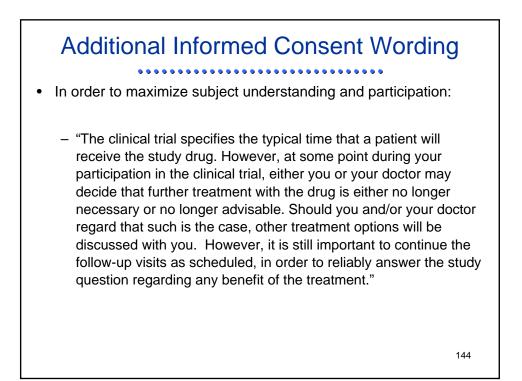


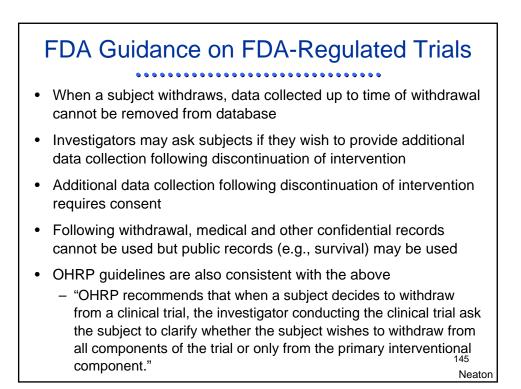


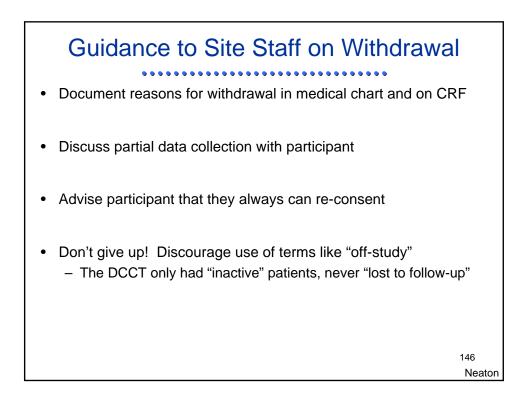


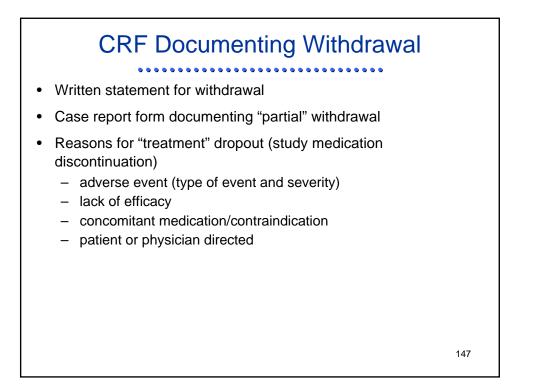


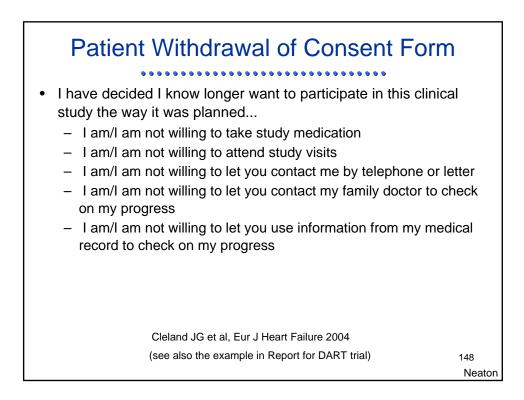


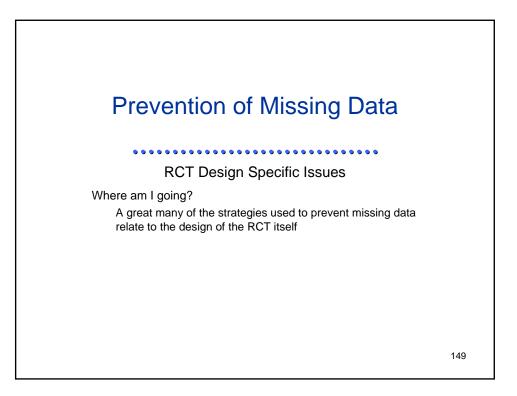


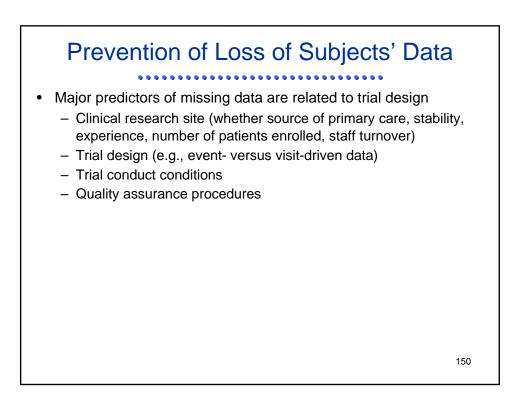


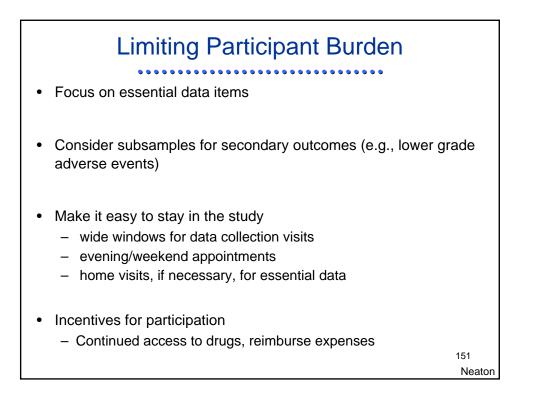


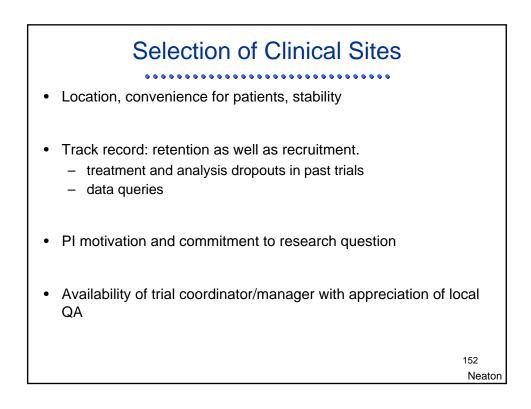


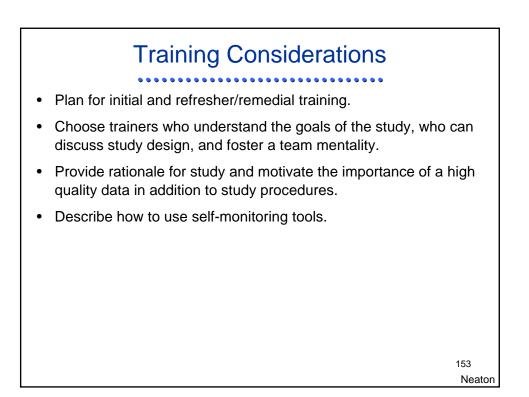


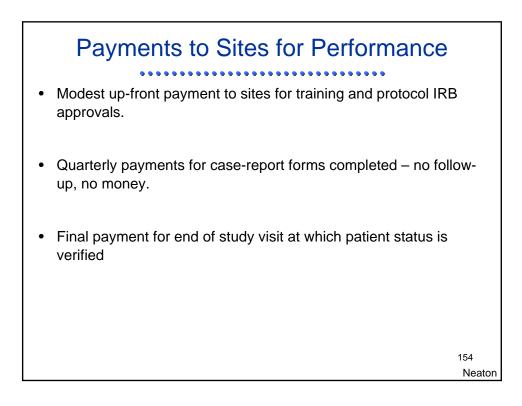


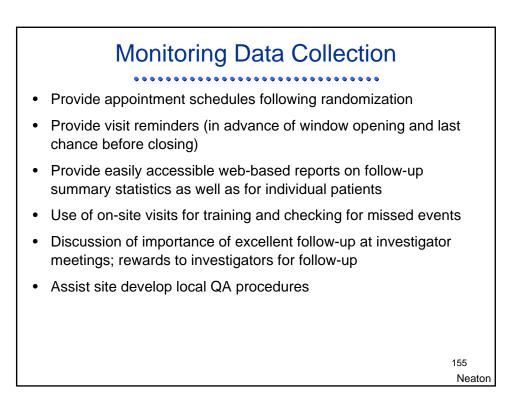


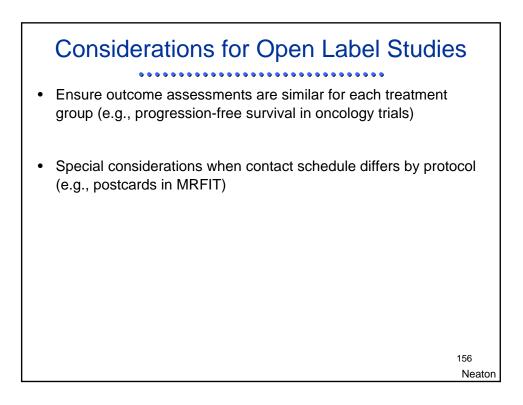


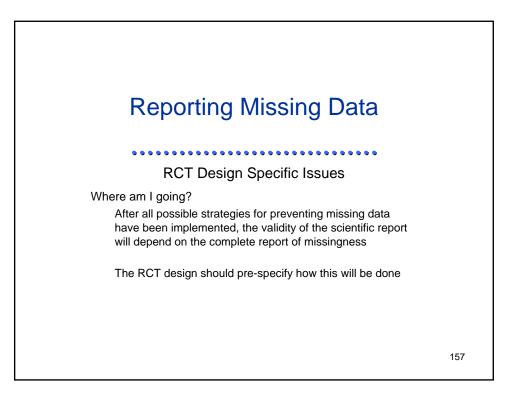


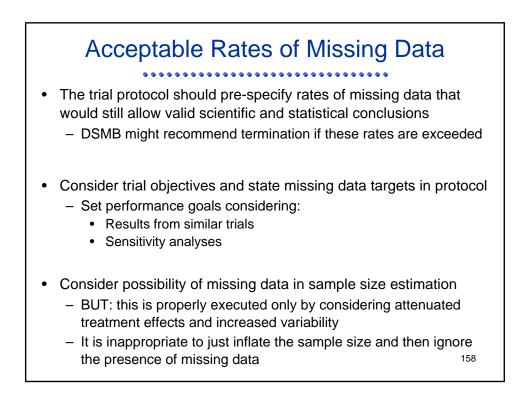


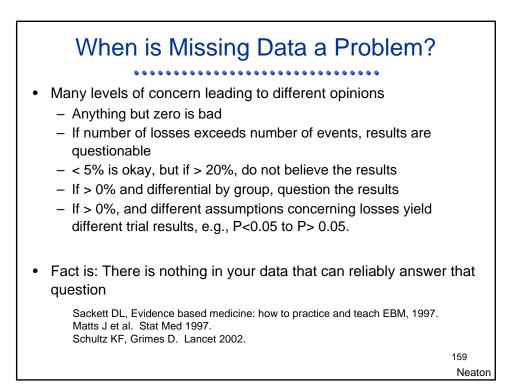


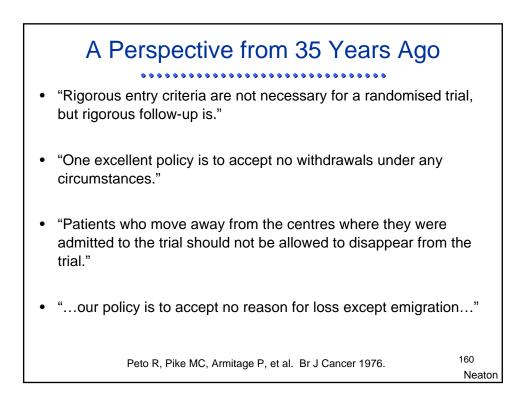


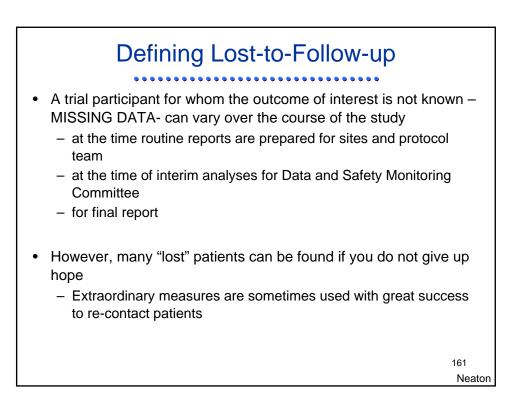


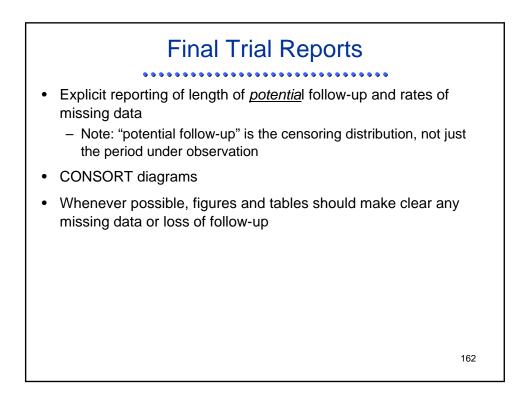


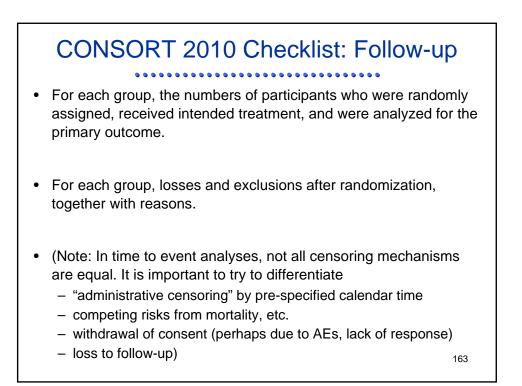


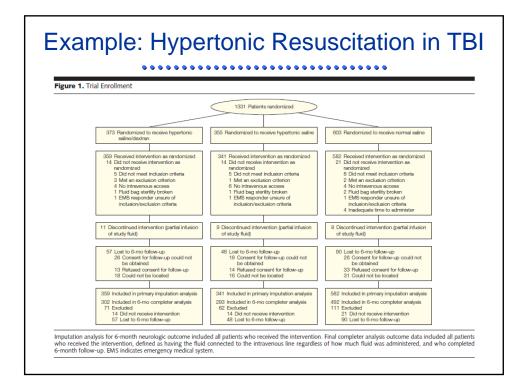












Example: Methotrexate in PBC

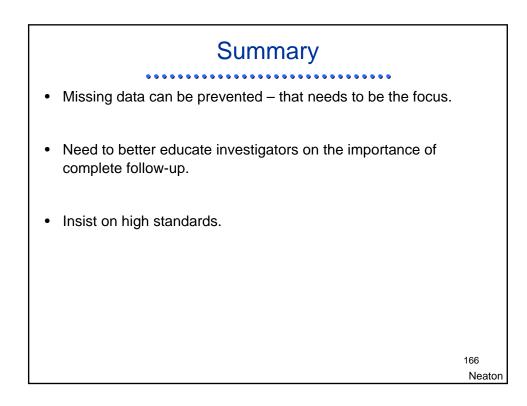
• Combes, et al, Hepatology, 2005

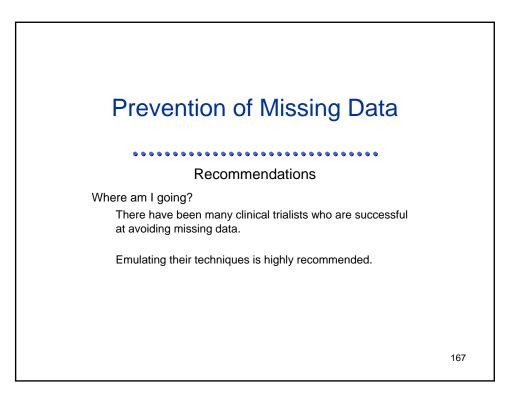
Forty-one patients on the MTX arm and 47 patients on the placebo arm discontinued taking study drug prior to the end of the interventional phase and prior to experiencing the primary endpoint of liver transplant or death.

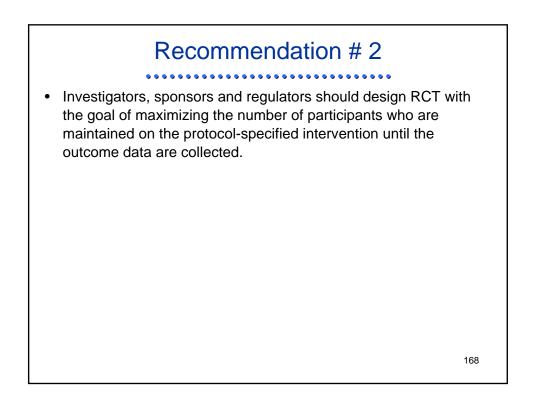
By the seventh year postrandomization, approximately one third of patients in both arms discontinued study treatment with no statistically significant differences between the treatment arms. Table 2 presents the numbers of patients discontinuing treatment early for each of several categories of reasons for early termination.

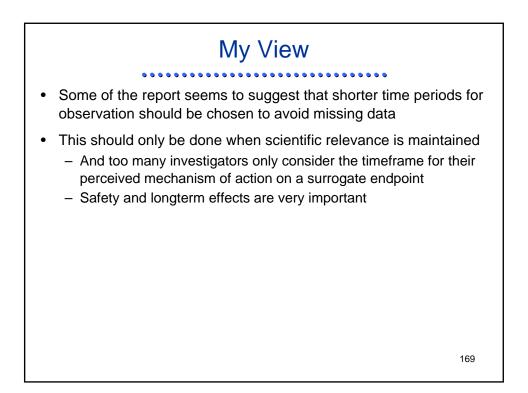
The overwhelming majority of patients who discontinued their study drug were still followed for occurrence of the study endpoints. Only 11 patients prematurely withdrew consent for follow-up of transplant-free survival status: 3 in the MTX arm and 8 in the placebo arm. The cumulative proportion withdrawing from the study in this manner was 1%, 3%, and 4.5% at 1, 2, and 6 years Table 2. Reasons Provided for Discontinuing Study Treatment (Mtx or Placebo) Prior to the End of the Interventional Phase and Prior to Experiencing the Primary Endpoint of Liver Transplantation or Death

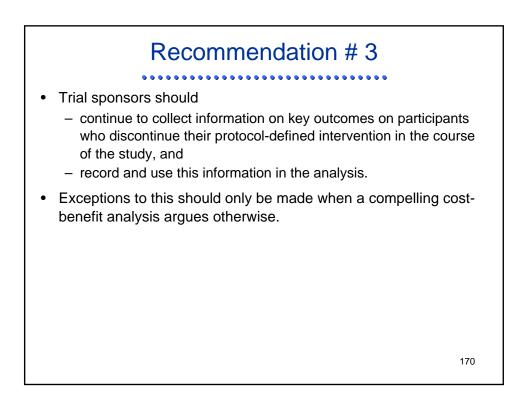
	MTX (n = 132)	Placebo (n = 133)	
Signs of bone marrow suppression	4	5	
Signs/symptoms of gastrointestinal toxicity	5	1	
Signs/symptoms of respiratory adverse			
effects	2	4	
Cancer	9	5	
Other indications for MTX	0	2	
Pregnancy	0	1	
PBC progression	5	5	
Other medical conditions	3	8	
Other signs/symptoms (AEs)	4	2	
Study burden	9	14	
	41	47	
		165	

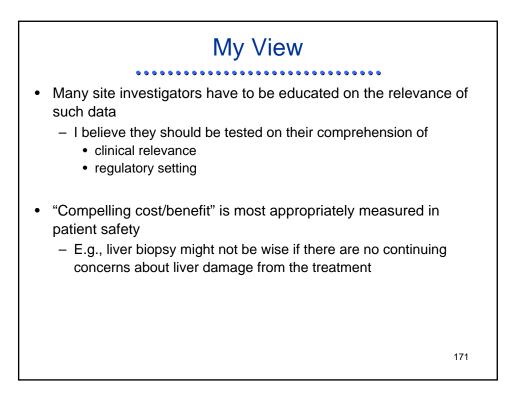


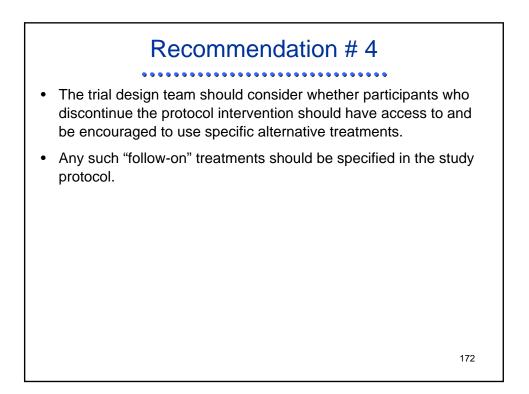


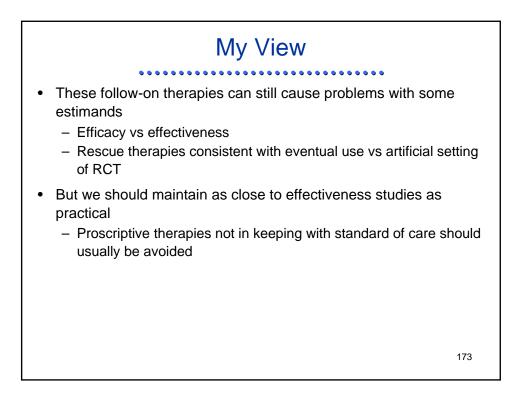


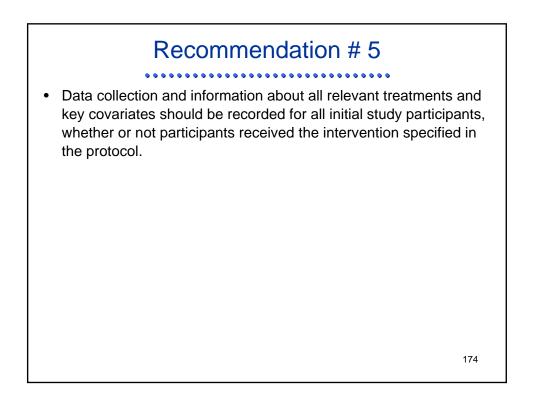


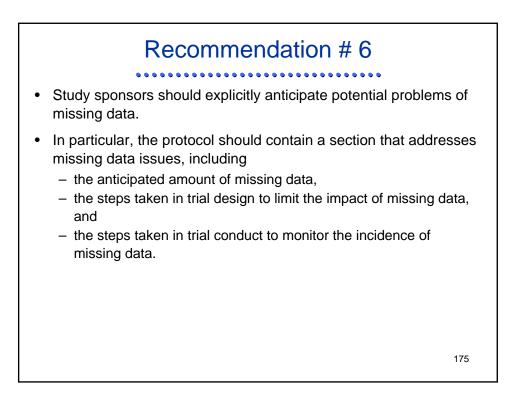


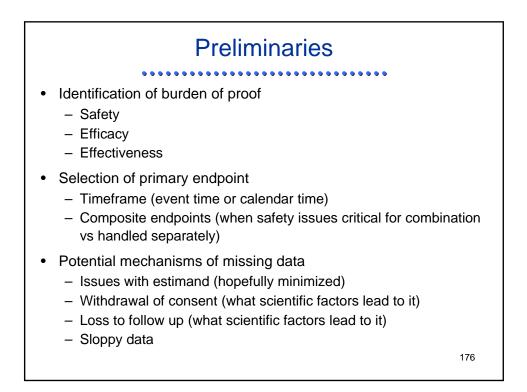


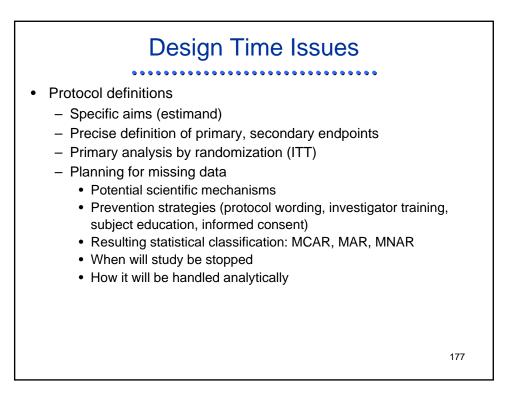


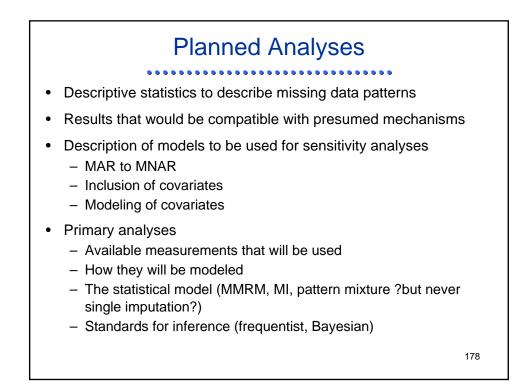


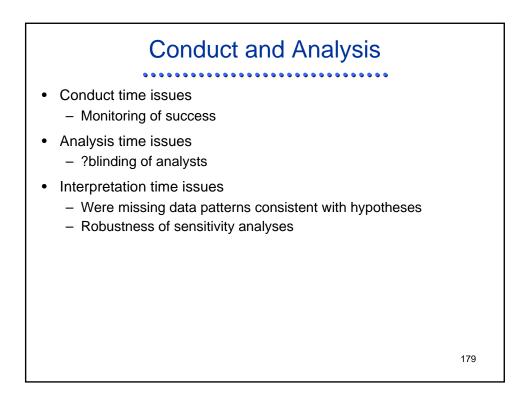


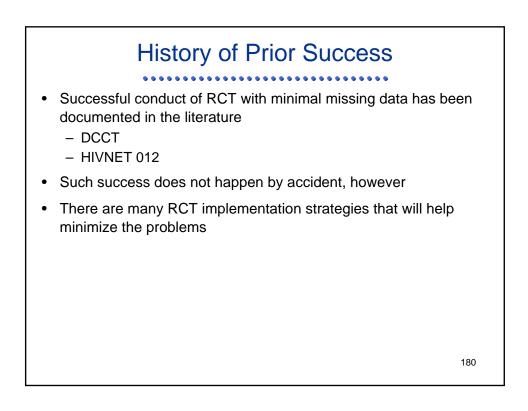








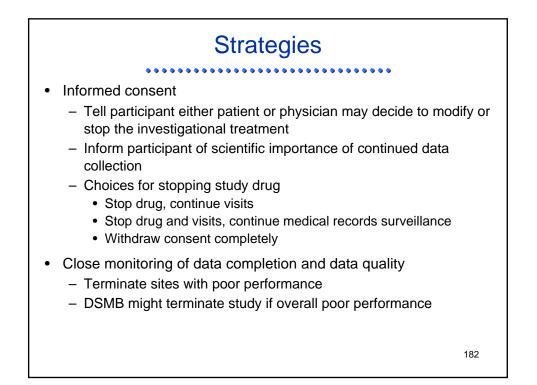


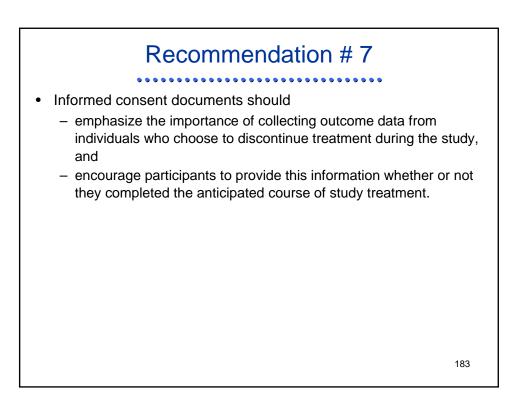


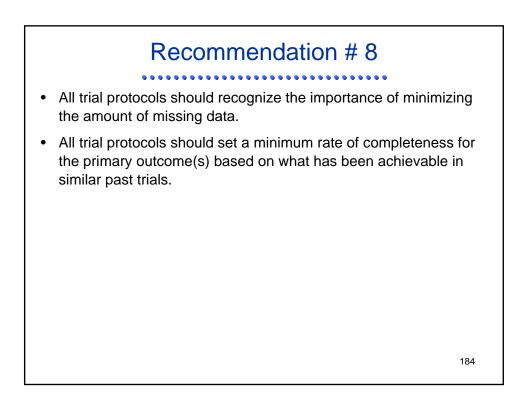


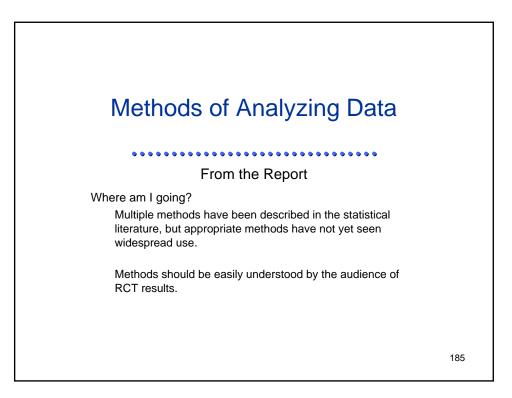
- Minimize patient burden
 - Minimize number of visits, and make them pleasant experiences
 - Collect only the necessary information
 - Use user-friendly CRFs
 - Use direct data capture
 - Use relatively large time window for ascertainment
- Provide incentives for continued participation
 - Access to health care for participants
 - Adequate reimbursement for investigators
- · Use experienced investigators and provide good training
 - Particularly important to educate on need for continued data collection
 - Investigators, study coordinators, data management

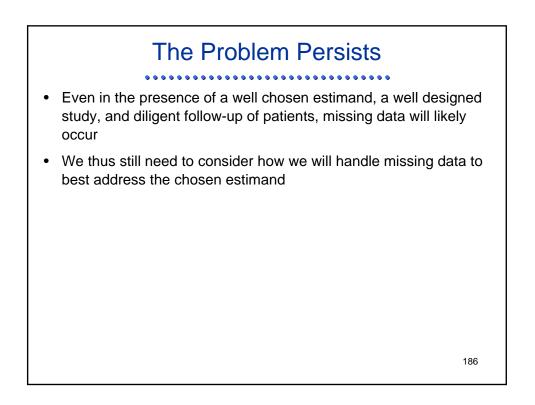
181

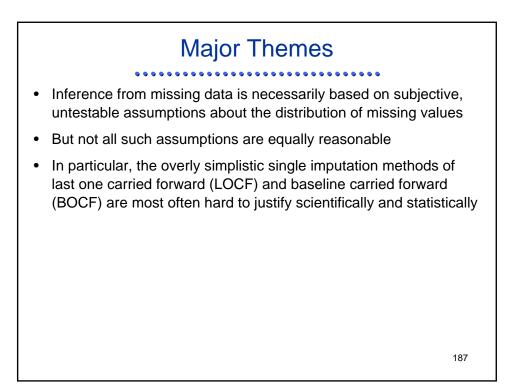


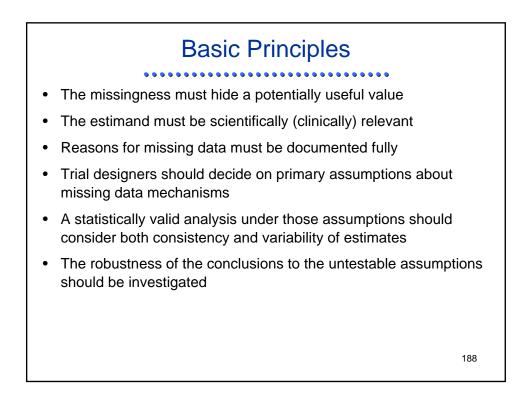


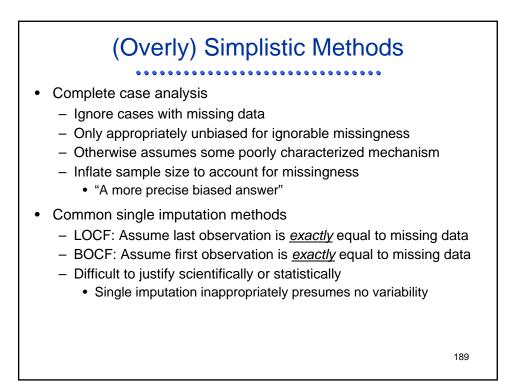


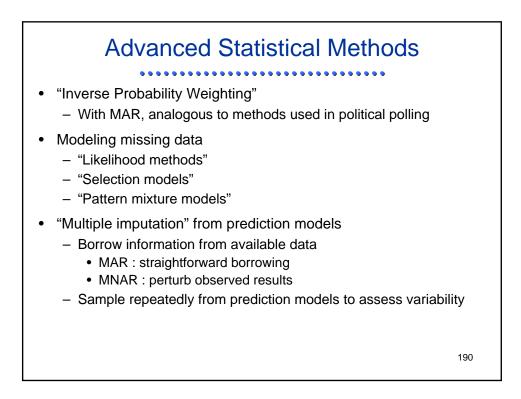


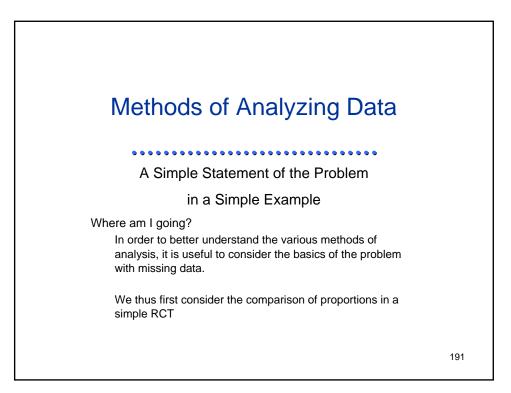


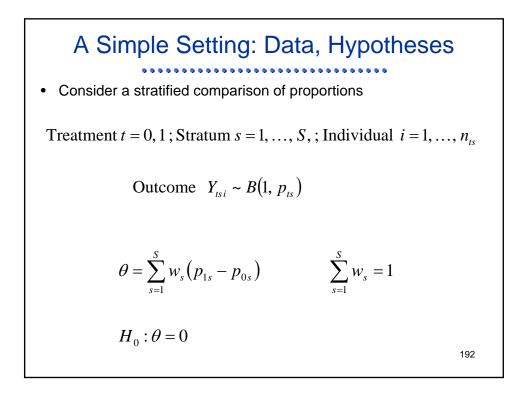


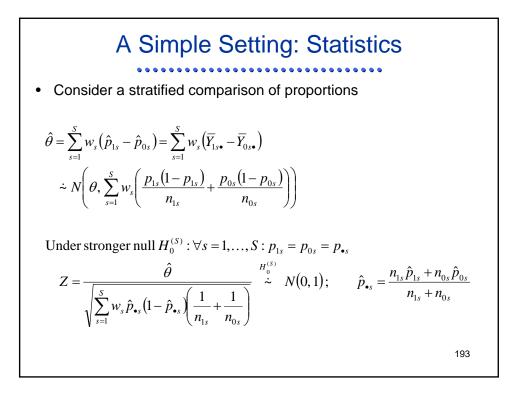




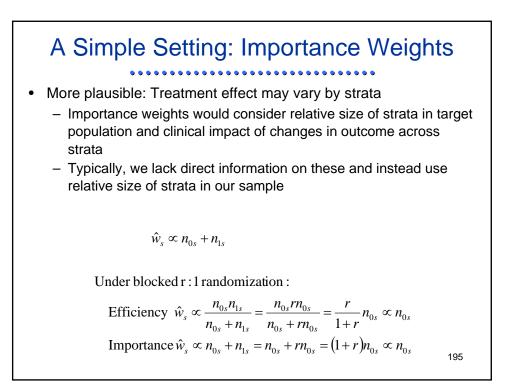




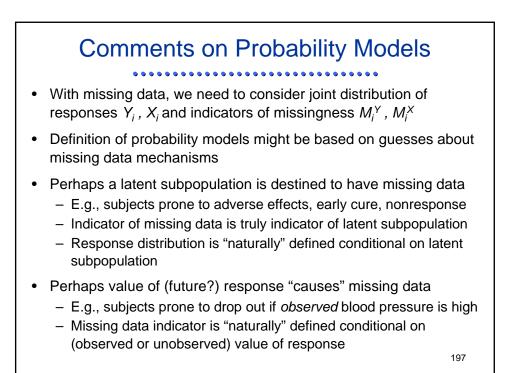




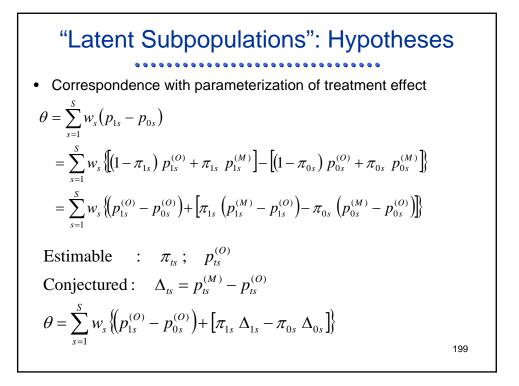
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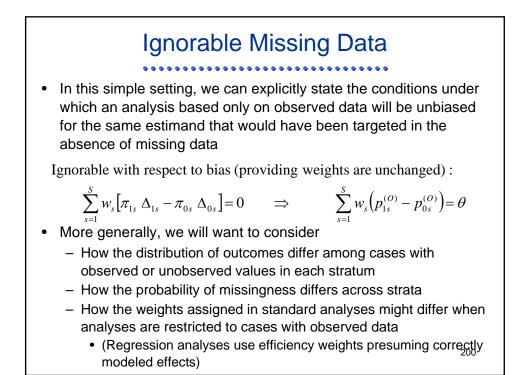


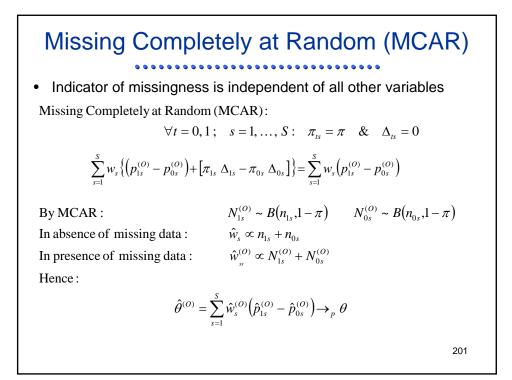
A Simple Setting: Missing Data • Consider a stratified comparison of proportions with some data potentially missing Treatment t = 0, 1; Stratum s = 1, ..., S, ; Individual $i = 1, ..., n_{ts}$ Outcome $Y_{tsi} \sim B(1, p_{ts})$ Indic Msng $M_{tsi} \sim B(1, \pi_{ts})$ $N_{ts}^{(M)} = \sum_{i=1}^{n_{ts}} M_{tsi}$ $N_{ts}^{(O)} = n_{ts} - N_{ts}^{(M)}$ Aux Data $V_{tsi} \sim G_{ts}$ $\theta = \sum_{s=1}^{S} w_s (p_{1s} - p_{0s})$ $\sum_{s=1}^{S} w_s = 1$ $H_0: \theta = 0$ ¹⁹⁶

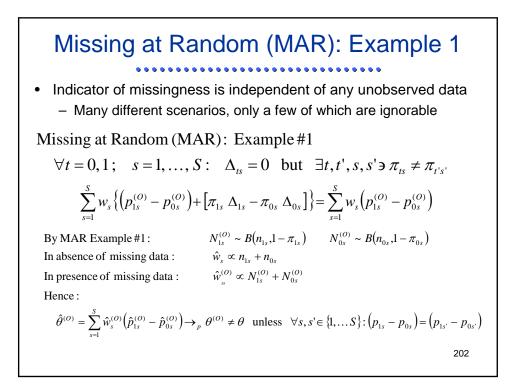


$$\begin{aligned}
\textbf{``Static Static S$$











analysis that adjusts for missing data has the same estimand as would be targeted in the absence of missing data

Inverse Probability Weighting (IPW) Ex #1:

$$N_{1s}^{(O)} \sim B(n_{1s}, 1 - \pi_{1s})$$
 $N_{0s}^{(O)} \sim B(n_{0s}, 1 - \pi_{0s})$

 $\hat{W}_s \propto n_{1s} + n_{0s}$

In absence of missing data : In presence of missing data: $\hat{w}^{(O)} \propto N_{1s}^{(O)} + N_{0s}^{(O)}$

Hence:

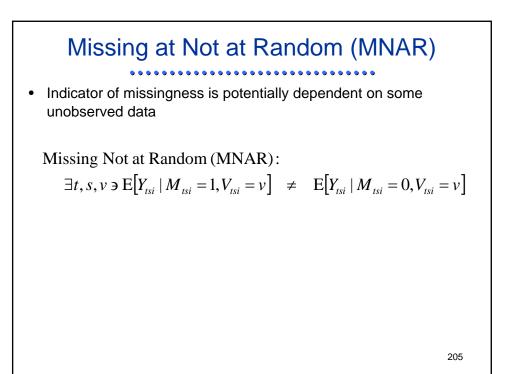
$$\hat{\theta}^{(O^*)} = \sum_{s=1}^{S} \hat{w}_s^{(O)} \left(\frac{\hat{p}_{1s}^{(O)}}{1 - \pi_{1s}} - \frac{\hat{p}_{0s}^{(O)}}{1 - \pi_{0s}} \right) \rightarrow_p \theta$$

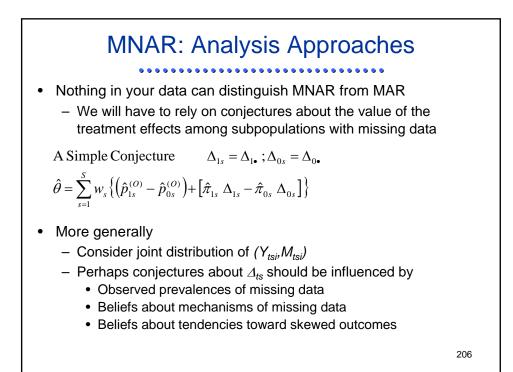
Providing the sample sizes do not lead to unstable weights

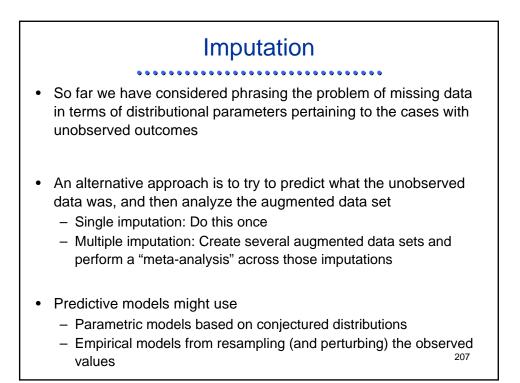
$$\hat{\theta}^{(O^*)} = \sum_{s=1}^{s} \hat{w}_s^{(O)} \left(\frac{\hat{p}_{1s}^{(O)}}{1 - \hat{\pi}_{1s}} - \frac{\hat{p}_{0s}^{(O)}}{1 - \hat{\pi}_{0s}} \right) \rightarrow_p \theta$$

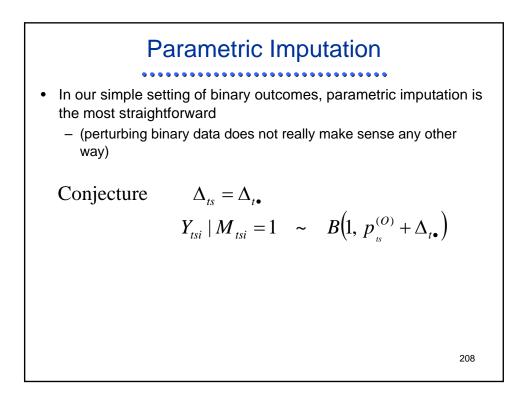
203

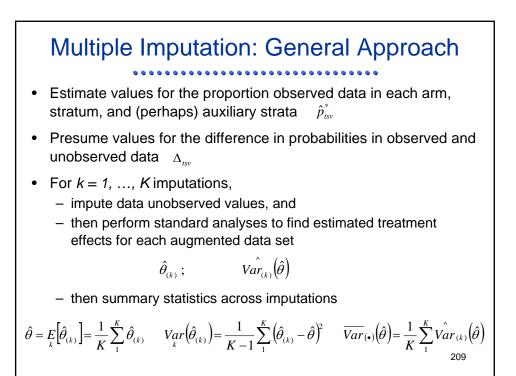
Missing at Random (MAR): Example 2 Indicator of missingness is independent of any unobserved data - Consider a scenario where missingness depends on auxiliary variable (perhaps an intermediate measure of outcome) - IPW can be used with any consistent estimates of probability of observed data Missing at Random (MAR): Example #2 $\exists t, t', s, s' \ni \pi_{ts} \neq \pi_{t's'}; \qquad \exists t, s \ni \Delta_{ts} \neq 0;$ But: $E[Y_{tsi} | M_{tsi} = 1, V_{tsi} = v] = E[Y_{tsi} | M_{tsi} = 0, V_{tsi} = v] = p_{tsv}^*$ with $\sum p_{tsv}^* \Pr[V_{tsi} = v] = p_{ts}$ Inverse Probability Weighting (IPW) Ex #2: $\hat{\theta}^{(O^*)} = \sum_{s=1}^{S} \hat{w}_{s}^{(O)} \left[\sum_{v} \left(\frac{\sum_{i=1}^{n_{is}} Y_{1si} (1 - M_{1si}) \mathbf{l}_{[V_{1si} = v]}}{\mathbf{P} \hat{\mathbf{r}} (M_{1si} = 0 | V_{1si} = v)} - \frac{\sum_{i=1}^{n_{is}} Y_{0si} (1 - M_{0si}) \mathbf{l}_{[V_{0si} = v]}}{\mathbf{P} \hat{\mathbf{r}} (M_{0si} = 0 | V_{0si} = v)} \right) \right] \rightarrow_{p} \theta_{204}$



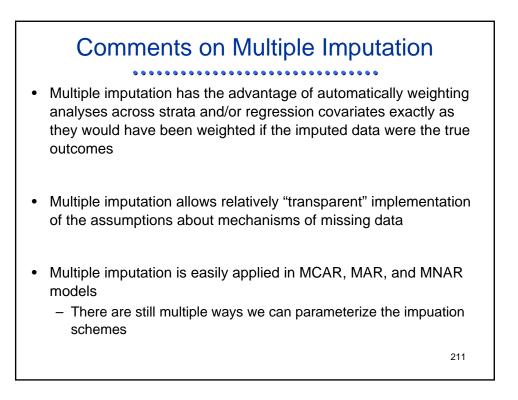


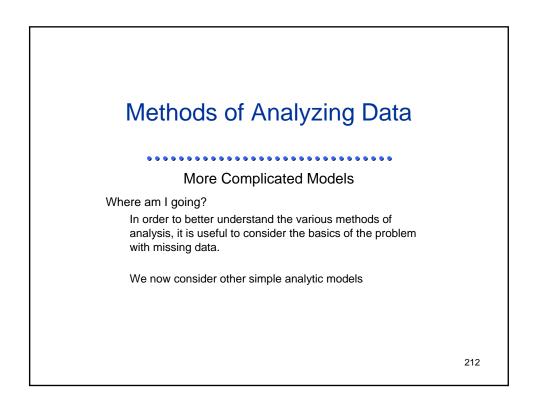


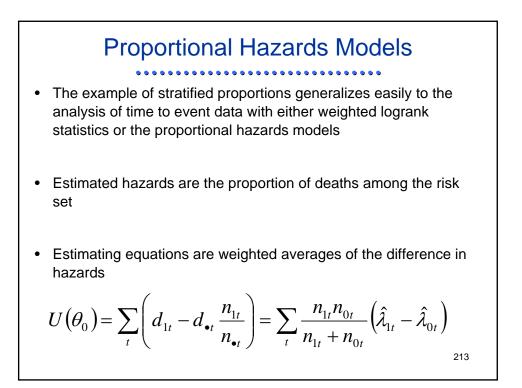


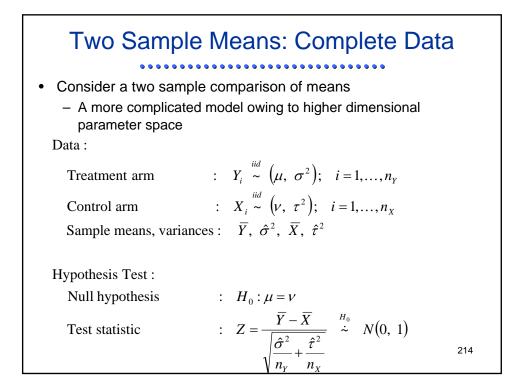


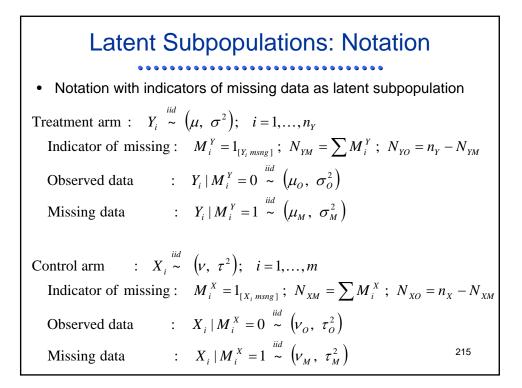
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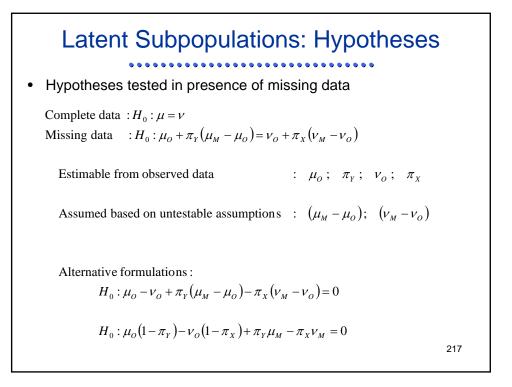


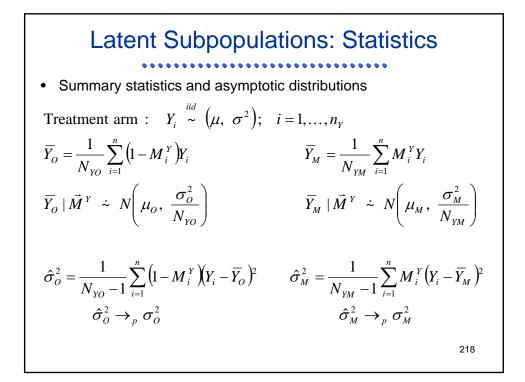


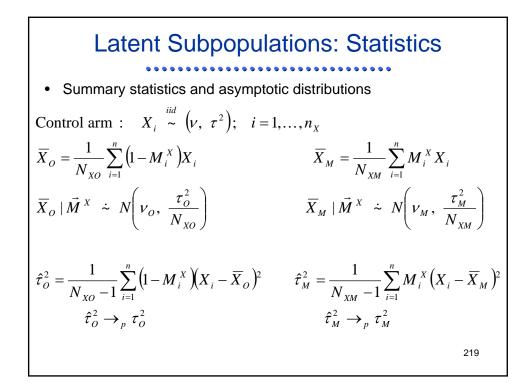




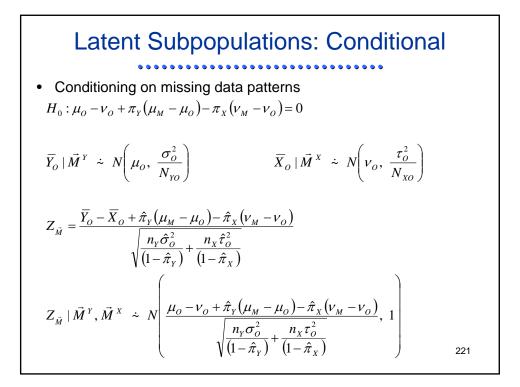
Latent Subpopulations: Models • Correspondence with complete data models Treatment arm : Marginal distns : $Y_i \stackrel{iid}{\sim} (\mu, \sigma^2); M_i^Y \stackrel{iid}{\sim} B(1, \pi_Y); i = 1,...,n_Y$ Conditional distns : $Y_i | M_i^Y = 1 \stackrel{iid}{\sim} (\mu_M, \sigma_M^2); Y_i | M_i^Y = 0 \stackrel{iid}{\sim} (\mu_o, \sigma_o^2)$ $\Rightarrow \mu = \mu_o + \pi_Y (\mu_M - \mu_o); \sigma^2 = \sigma_o^2 \left[1 - \pi_Y + \pi_Y \frac{\sigma_M^2}{\sigma_o^2} + \pi_Y (1 - \pi_Y \left(\frac{\mu_M - \mu_o}{\sigma_o} \right)^2 \right]$ Control arm : Marginal distns : $X_i \stackrel{iid}{\sim} (\nu, \tau^2); M_i^X \stackrel{iid}{\sim} B(1, \pi_X); i = 1,...,n_X$ Conditional distns : $Y_i | M_i^Y = 1 \stackrel{iid}{\sim} (\nu_M, \tau_M^2); Y_i | M_i^Y = 0 \stackrel{iid}{\sim} (\nu_o, \tau_o^2)$ $\Rightarrow \nu = \nu_o + \pi_X (\nu_M - \nu_o); \tau^2 = \tau_o^2 \left[1 - \pi_X + \pi_X \frac{\tau_M^2}{\tau_o^2} + \pi_X (1 - \pi_X \left(\frac{\nu_M - \nu_o}{\tau_o} \right)^2 \right]_{216}$



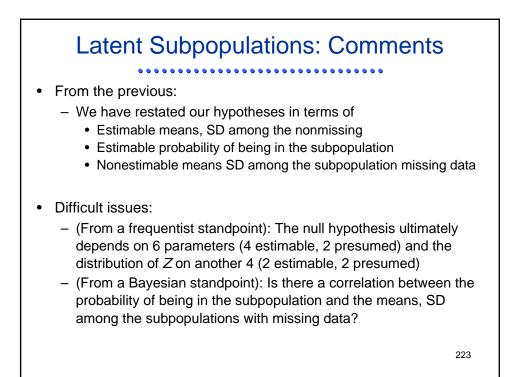


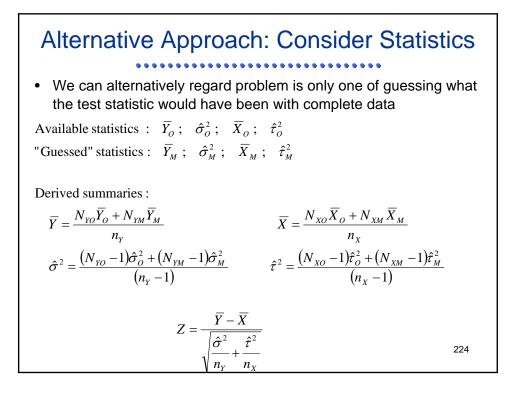


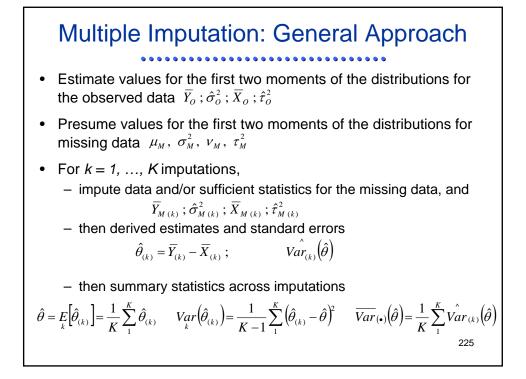
Latent Subpopulations: Statistics • Correspondence with overall statistics Treatment arm : $Y_i \stackrel{iid}{\sim} (\mu, \sigma^2)$; i = 1, ..., n $\overline{Y} = \frac{N_{YO}\overline{Y}_O + N_{YM}\overline{Y}_M}{n_Y}$ $\hat{\sigma}^2 = \frac{(N_{YO} - 1)\hat{\sigma}_O^2 + (N_{YM} - 1)\hat{\sigma}_M^2}{n_Y - 1}$ Control arm : $X_i \stackrel{iid}{\sim} (\nu, \tau^2)$; $i = 1, ..., n_X$ $\overline{X} = \frac{N_{XO}\overline{X}_O + N_{XM}\overline{X}_M}{n_X}$ $\hat{\tau}^2 = \frac{(N_{XO} - 1)\hat{\tau}_O^2 + (N_{XM} - 1)\hat{\tau}_M^2}{n_X - 1}$ $Z = \frac{\overline{Y} - \overline{X}}{\sqrt{\frac{\hat{\sigma}^2}{n_Y} + \frac{\hat{\tau}^2}{n_X}}} = \frac{\frac{N_{YO}\overline{Y}_O + N_{YM}\overline{Y}_M}{\sqrt{\frac{(N_{YO} - 1)\hat{\sigma}_O^2 + (N_{YM} - 1)\hat{\sigma}_M^2}} + \frac{(N_{XO} - 1)\hat{\tau}_O^2 + (N_{XM} - 1)\hat{\tau}_M^2}{n_X(n_X - 1)}}$ 220



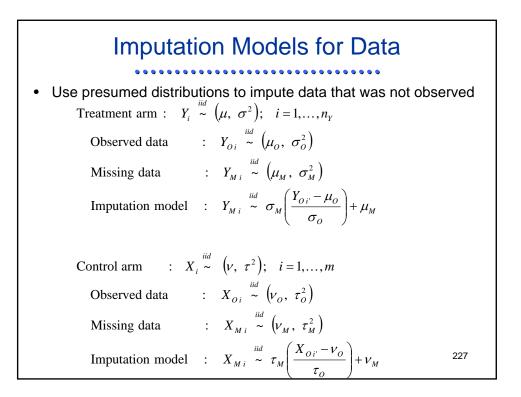
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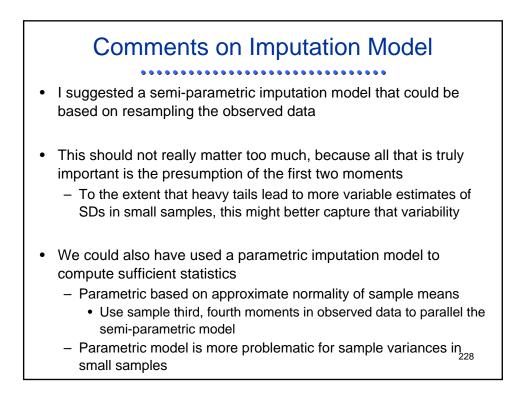


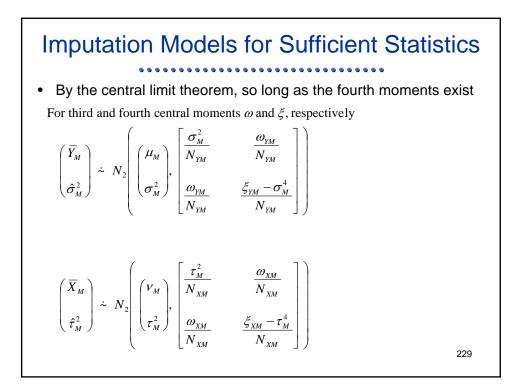


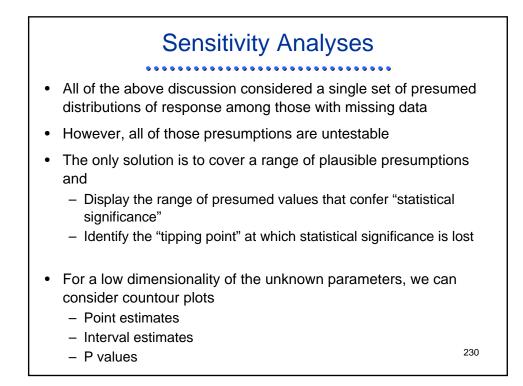


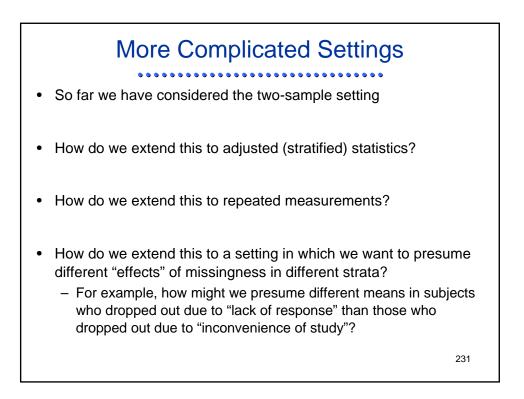
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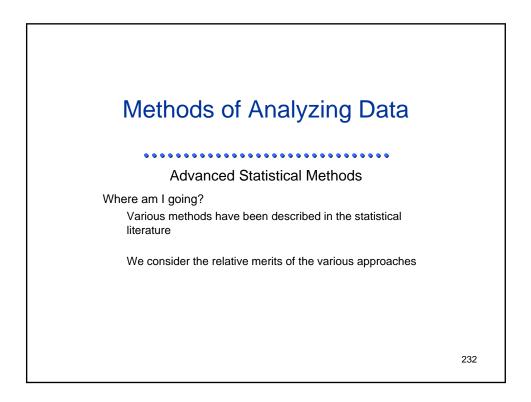


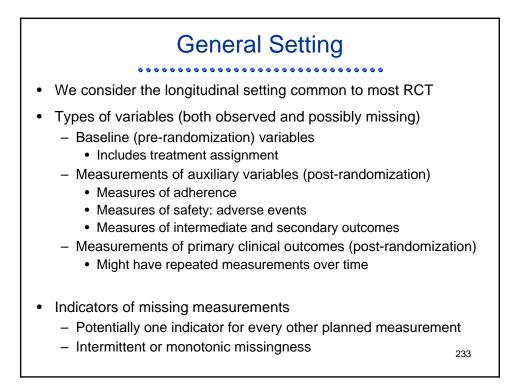


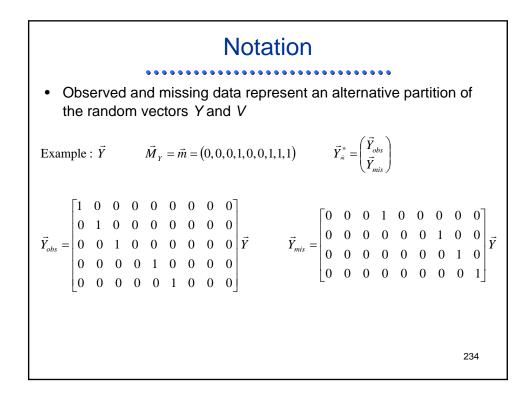


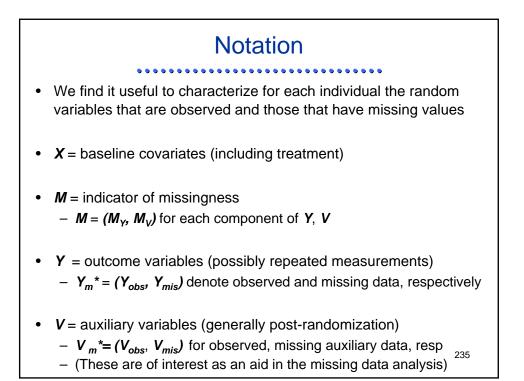


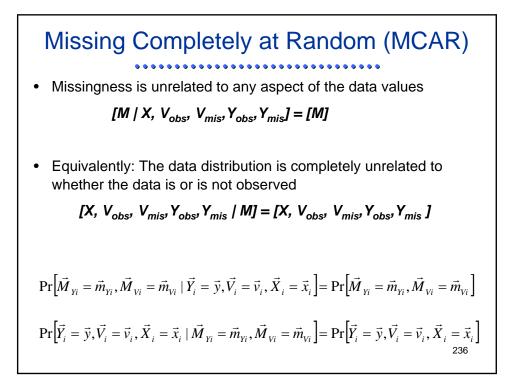


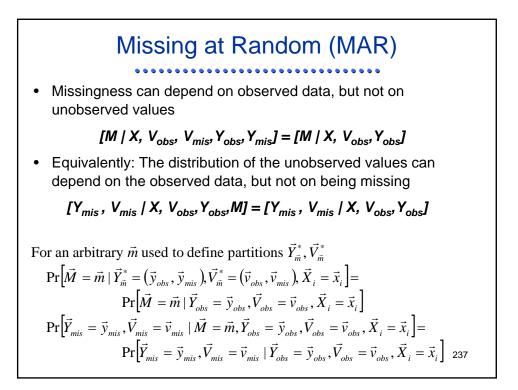




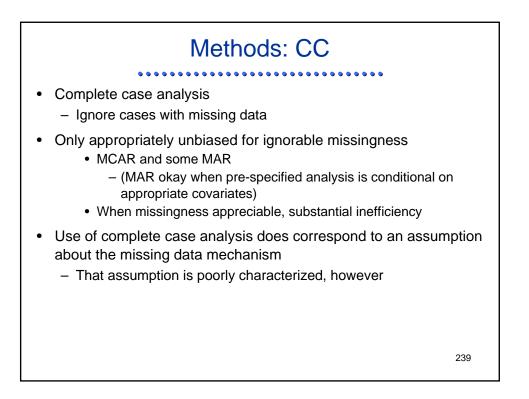


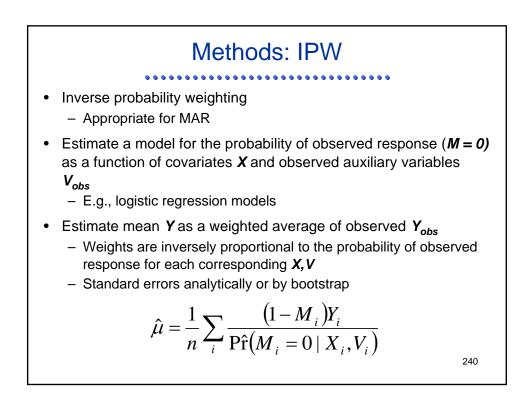


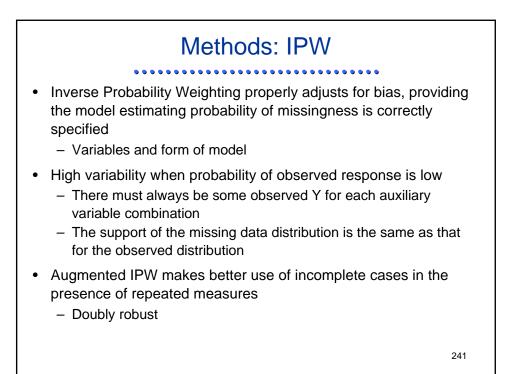


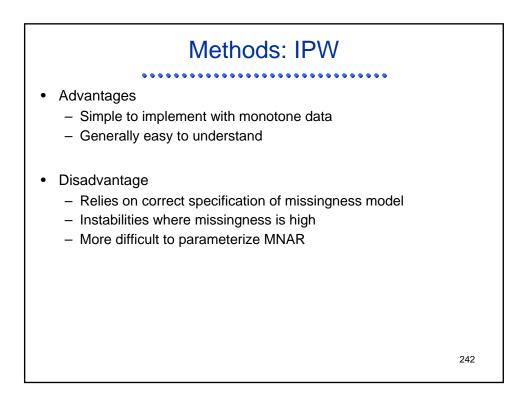


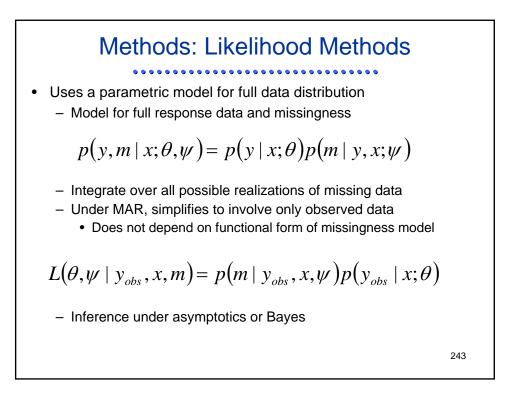
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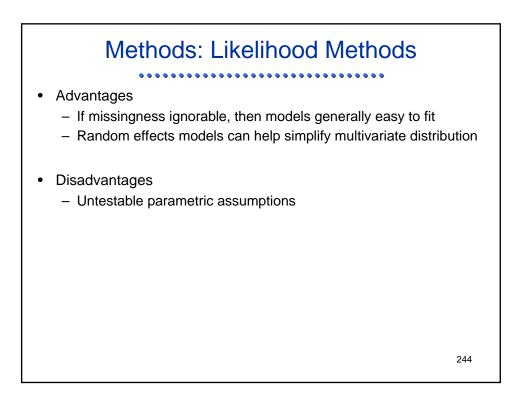


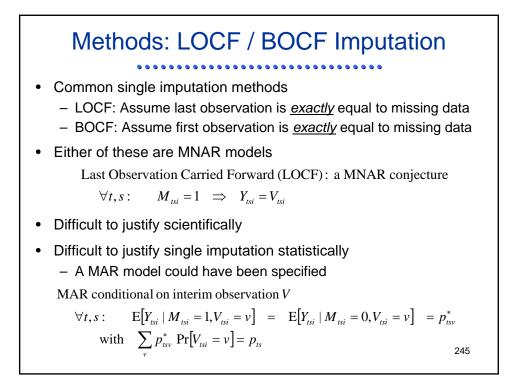


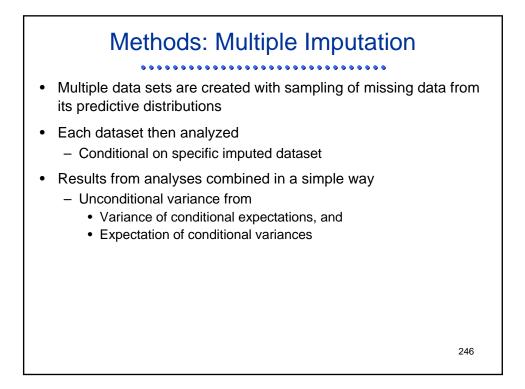


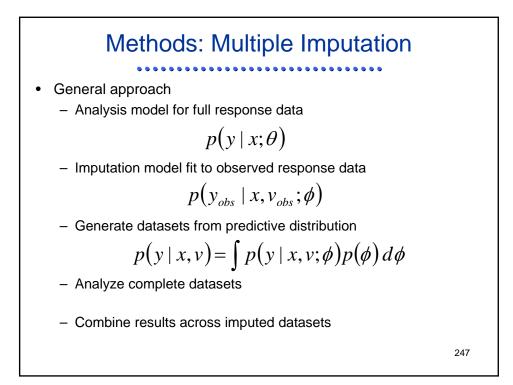


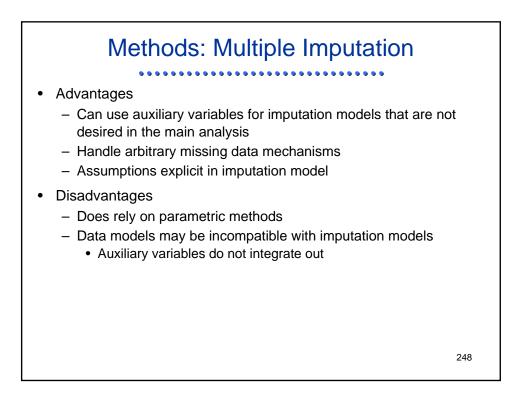


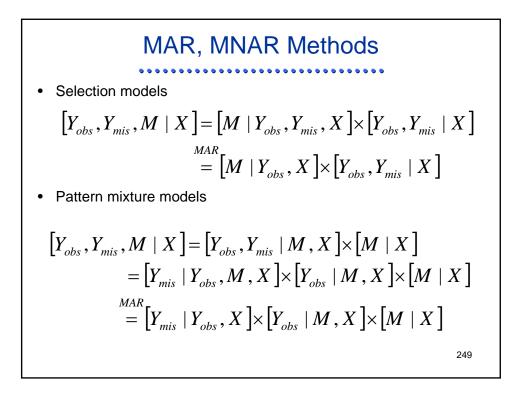


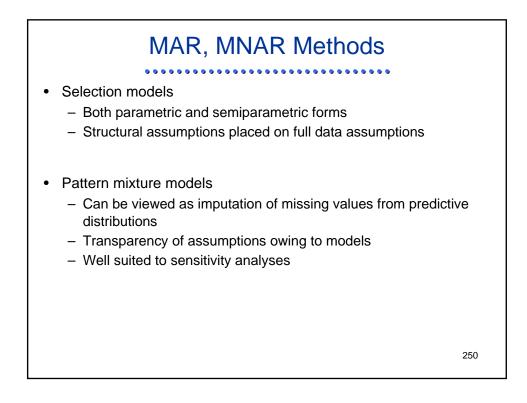


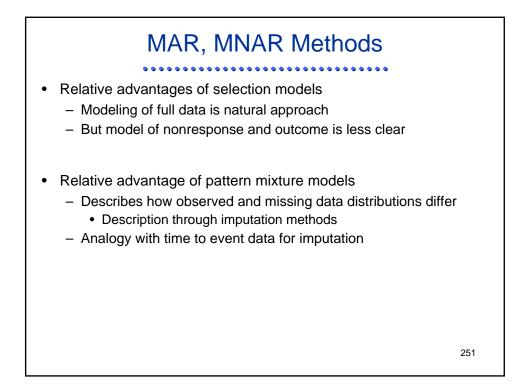


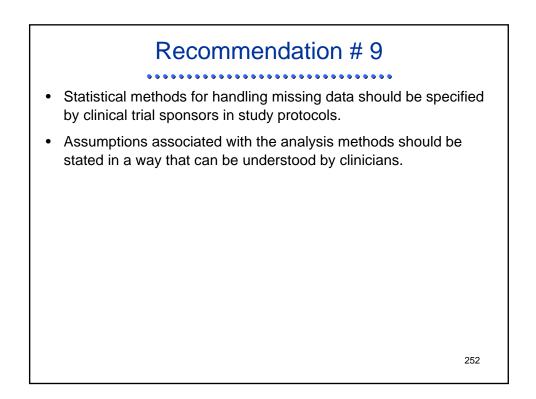


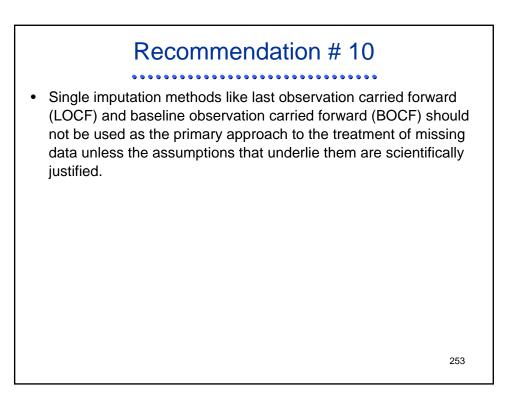


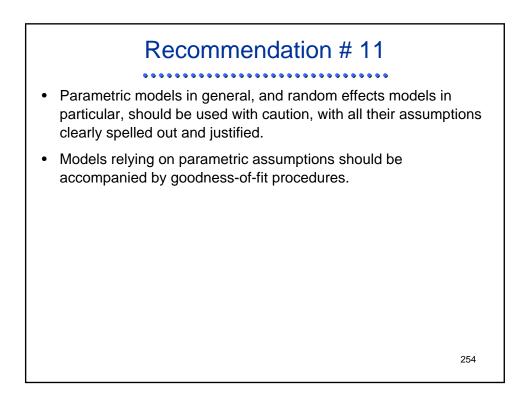


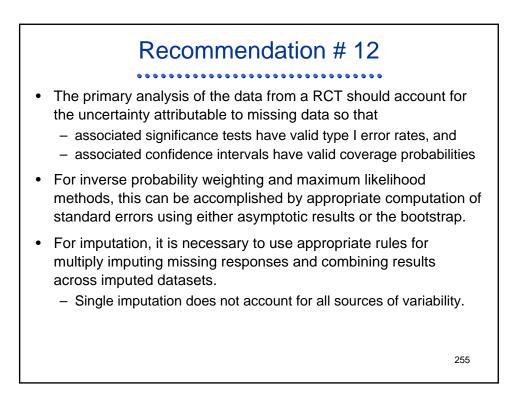


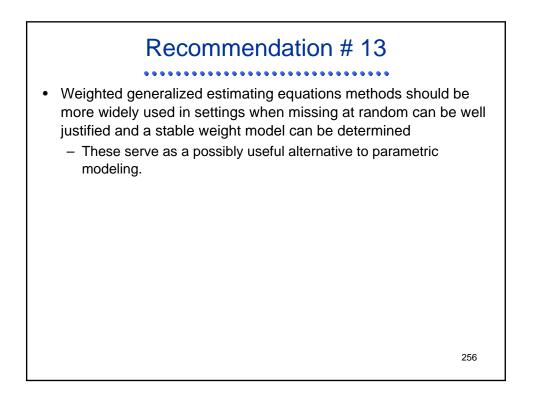


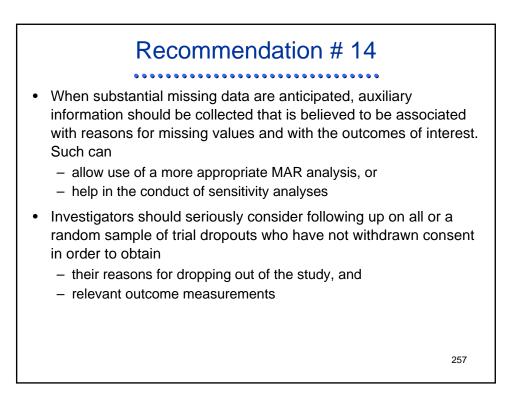


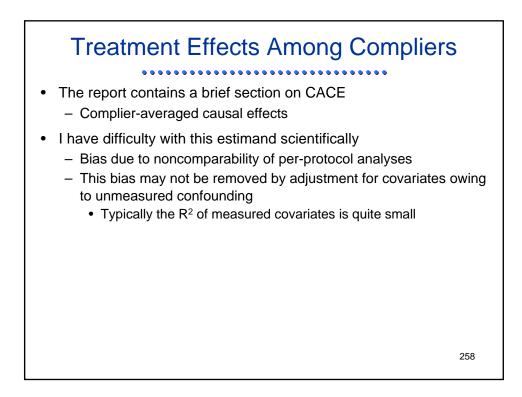


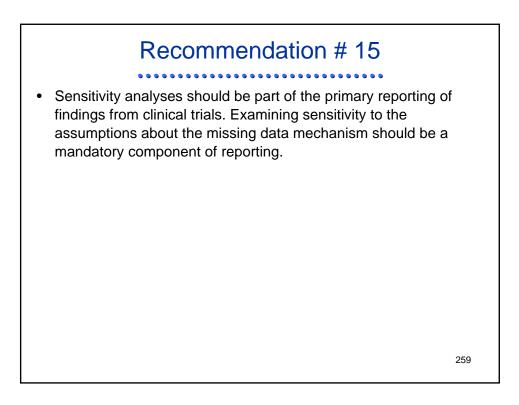


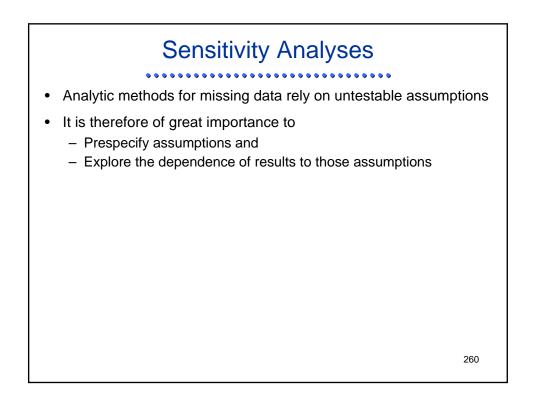


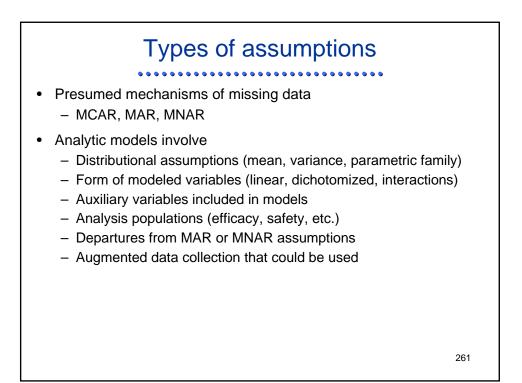


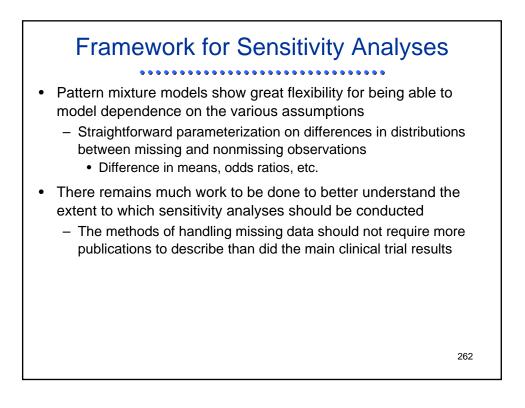


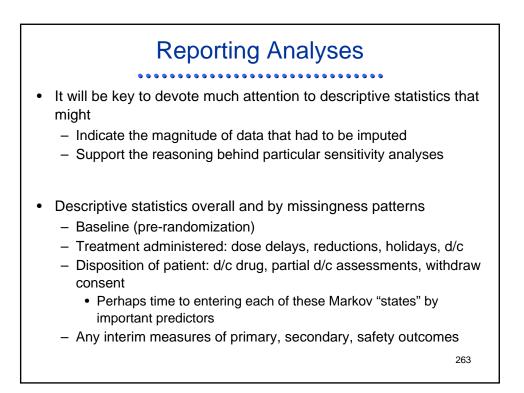


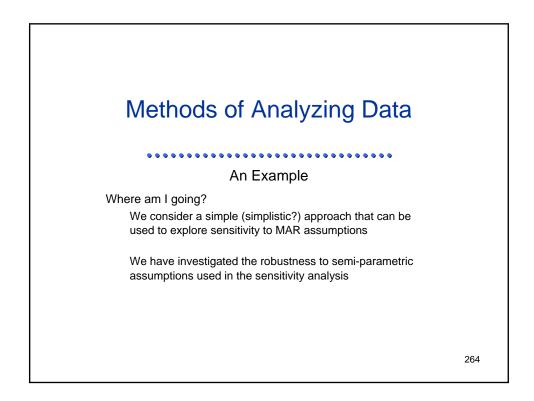


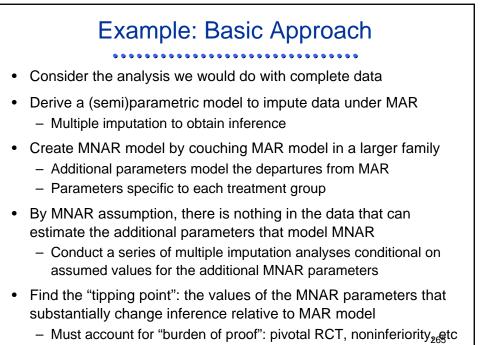




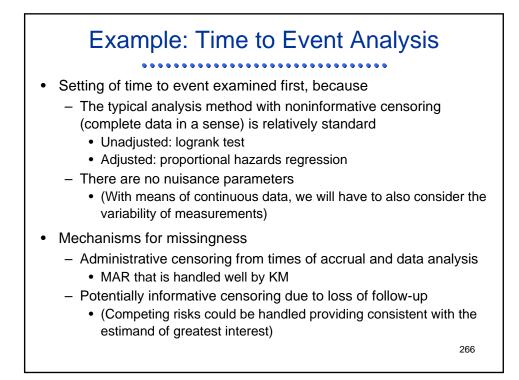


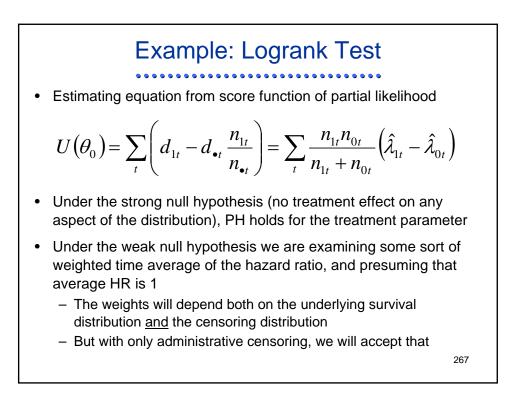


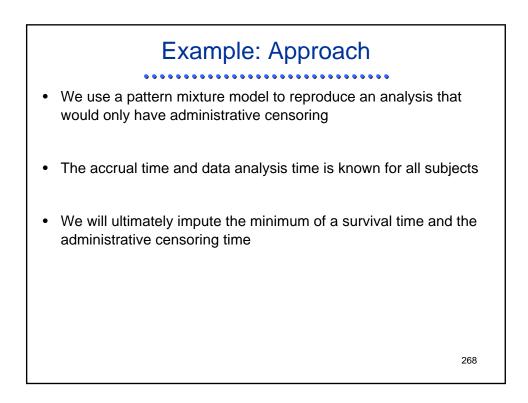


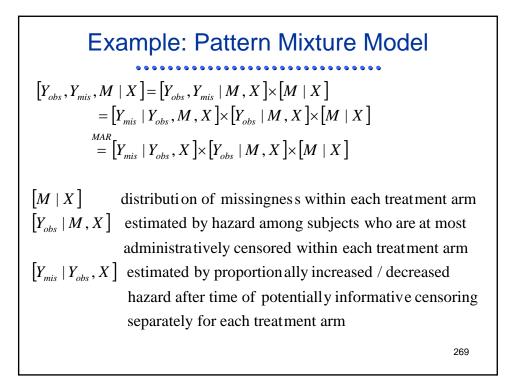


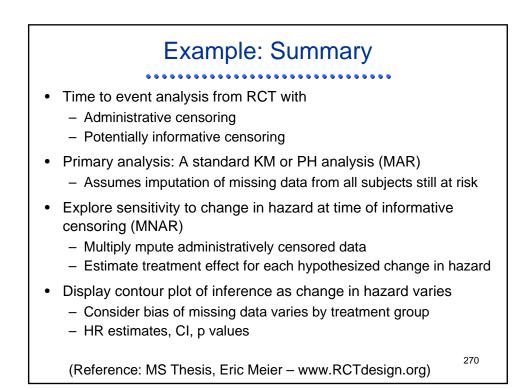
- Secondarily assess reasonableness of that tipping point

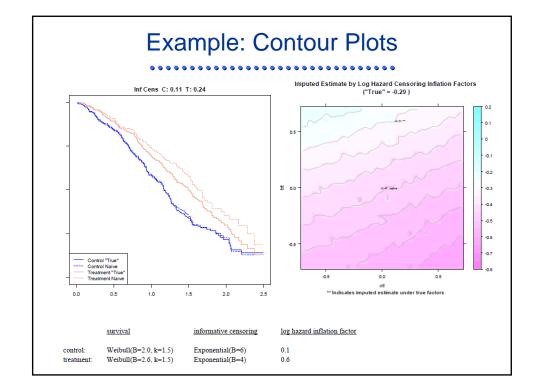


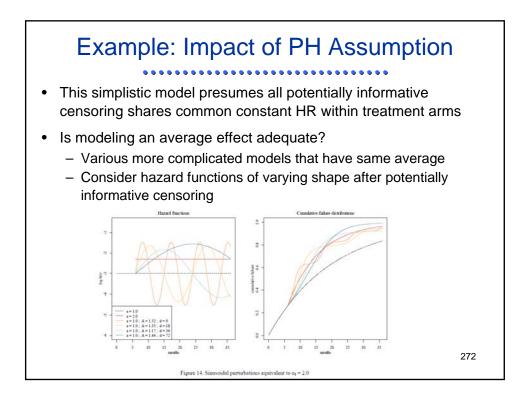












 Example: Impact of PH Assumption Generally reasonable (though slightly low) coverage probability across a wide variety of scenarios 									
	Estimated Treatment log(HR)								
Sœnario	Mean "True"	"True" Cl Coverage Rate	Mean "True" Cl Width	Mean Naïve	Naïve CI Coverage Rate	Mean Naïve Cl Width	Mean Imputed	Imputed CI Coverage Rate	Mean Imputed Cl Width
base	-0.272	0.950	0.422	-0.392	0.834	0.480	-0.273	0.930	0.458
а	-0.276	0.961	0.422	-0.393	0.846	0.480	-0.273	0.941	0.458
b	-0.280	0.948	0.423	-0.393	0.849	0.480	-0.272	0.932	0.458
С	-0.280	0.946	0.423	-0.393	0.849	0.480	-0.272	0.932	0.458
d	-0.267	0.954	0.421	-0.392	0.826	0.480	-0.273	0.930	0.458
е	-0.278	0.951	0.423	-0.392	0.845	0.480	-0.273	0.929	0.458
									273

