Advanced Bayesian Phylogenetics: Recombination

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• Clinical implications of intra-host recombination

Mechanisms and Hot-Spots?



 Probability of strand-slippage/jumping may be function of genomic 1° or 2° structure

Clinical Relevance of Hot-Spots

- In vivo evidence
- In vitro recomb. rates 50× greater in env than gag
- Development of multiple drug resistance (Kitchen *et al.*, 2006)
- Drug choice

Phylogenetic Recombination

Detection

Recombination ⇒ genomic break-points with incongruent

colorigies:

Image: Colorigies

Image:

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• Variable dimensional model \Rightarrow reversible jump MCMC

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Putative A/G Inter-Subtype Recombinants

Data:

- 42 unrelated (hopefully) recombinants from LANL
- Of African origins
- Same subtypes to maximize power



Subset of independent analyses

How to **pool** information?

- Sparse "observations" (# break-points << seq. length)
- Neighboring sites should have similar probabilities

Joint Analysis via Gaussian Markov Random Fields

A GMRF to smooth and estimate **population-level** recombination log-odds (probabilities):



Normally distributed vector

$$\mathbf{x} \sim \mathcal{N}(\boldsymbol{\nu}, \mathbf{Q}^{-1})$$

is a GMRF wrt graph $\mathcal{G} = (\mathcal{V}, \mathcal{E})$ when $\mathbf{Q} > 0$ and $Q_{ij} \neq 0$ iff $(i, j) \in \mathcal{E}$

- Q can be huge, but very sparse
- Fast numerical methods available, make the approach feasible (Rue *et al.*, 2001, 2004)

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GMRF as an Improper Prior

Field (population-level log-odds) γ :

$$oldsymbol{\gamma} | \omega \sim \mathcal{N}(\prime, ilde{\mathbf{Q}}^{-1}), ext{ where } ilde{\mathbf{Q}}^{-1} = \mathbf{Q} + \epsilon \mathbf{I}$$

Impropriety: 1^{st} -order random-walk field defined on differences. Baseline $\propto 1$. Normally, not a problem (Sun, 1999).

- Think of break-points as "success counts" $\mathbf{C} = (C_1, \dots, C_S)$ in binomial trials
- What if $C_s = 0$ or $C_s = 42$ for all s?

Prior: Random-walk precision $\omega \sim \Gamma(\cdot, \cdot)$. Express prior belief via $p_i/p_j \leq 7$ -fold (Bernardinelli, 1995; Moumen, 2001)

Non-linearly Constrained GMRFs

The number of break-points $M \sim \text{approximately Poisson}(\delta)$ with $\delta = \sum_{s=1}^{S} p_s$ (le Cam, 1960) for each recombinant.

Aim: $\Pr(M > 0) \approx 1 - e^{\delta} = c = 0.5.$

Problem: Sum-of-p constraint is **non-linear** in the field (γ):

$$\sum_{s=1}^{S} \frac{e^{\gamma_s}}{1 + e^{\gamma_s}} = -\ln(1 - c)$$
(1)

Solution: Linearize constraint via Taylor expansion about arbitrary point v, then constraint \Rightarrow "re-centering" proposal γ^* from unconstrained GMRF. How to choose v?



Preliminary in vitro Strand **Transfer Assay** Minutes of Reverse Transcription 0 2 4 8 16 32 64 100.0 ranefa -0- gag -0- pol 80.0 gag Recombination Frequency 60.0 40.0 0 2 4 8 16 32 64 20.0 40 60 10 20 30 50 70 0 Transfe pol Minutes of Reverse Transcription -Full • Results support gag hot-spot. First de novo elucidation of HIV recombination mechanism with computational

methods?