

## Session 3: Probability Distributions II

# Exercise Solutions

For questions 1 and 2, recall that, for offspring genotypes from a heterozygous cross:

Carrier = Aa with  $\Pr(Aa) = \frac{1}{2}$

Unaffected = AA with  $\Pr(AA) = \frac{1}{4}$

Affected = aa with  $\Pr(aa) = \frac{1}{4}$

Consider a scenario with  $n=3$  offspring.

### Question 1

What is the probability that all three offspring will be carriers?

$$\begin{aligned} P(Y_1 = 0, Y_2 = 3, Y_3 = 0) &= \frac{3!}{0!3!0!} p_1^0 p_2^3 p_3^0 \\ &= \frac{3 \cdot 2 \cdot 1}{3 \cdot 2 \cdot 1} (0.25)^0 (0.5)^3 (0.25)^0 \\ &= 0.125 \end{aligned}$$

R code:

```
dmultinom(x=c(0, 3, 0), prob=c(0.25, 0.5, 0.25))
```

### Question 2

What is the probability that two offspring will be affected and one will be a carrier?

$$\begin{aligned} P(Y_1 = 0, Y_2 = 1, Y_3 = 2) &= \frac{3!}{0!1!2!} p_1^0 p_2^1 p_3^2 \\ &= \frac{3 \cdot 2 \cdot 1}{2 \cdot 1} (0.25)^0 (0.5)^1 (0.25)^2 \\ &= 0.09375 \end{aligned}$$

R code:

```
dmultinom(x=c(0, 1, 2), prob=c(0.25, 0.5, 0.25))
```

## Exercises

For the following questions, calculate the specified probabilities for the standard Normal random variable  $Z \sim N(0,1)$ . You can use an online standard Normal CDF calculator.

### Question 3

$$P(Z \leq 1.65) = \mathbf{0.9505}$$

R code:

```
pnorm(1.65, mean = 0, sd = 1)
```

### Question 4

$$P(Z \geq 0.5) = \mathbf{0.3085}$$

R code:

```
1 - pnorm(0.5, mean = 0, sd = 1)
```

### Question 5

$$P(-1.96 \leq Z \leq 1.96) = 0.975 - 0.025 = \mathbf{0.95}$$

R code:

```
pnorm(1.96, mean = 0, sd = 1) - pnorm(-1.96, mean = 0, sd = 1)
```