Bayesian Adaptive Clinical Trial Design

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Day 2



ESSET Code

Definitions, Trial Parameters

```
rm(list=ls())
## All times in months
library(VGAM)
v = list(
 ### Event, success probabilities for IV, IV+2nd therapy, Oral, Oral + 2nd therapy
  S3 = c(\#\# \text{ There are success rates for the three groups})
     0.50,
               # fPHT
                           Response Rates
     0.50,
               # LVT
     0.50
               # VPA
  ),
  Maximum sample size & max sample size for Stage 1
 MaxN = 795,
 # Priors
                              Priors
  a = rep(1, 3),
  b = rep(1, 3),
 # First look and look every
  firstlook = 300,
  firststop = 400
                              Sample Size &
  lookevery = 100,
 # Min to randomized
                              Timing of Looks
 minpr = 0.05,
 # simulations
 nsims = 1000,
  badlim = 0.25,
 # critv to (a) for 'best'
 #
            (b) for 'worst
 #
            (c) to stop for futility (i.e Pred prob a winner or loser id'd)
            (d) for worse than 25%
 critv = c(.975, .975, 0.05, 0.05)
)
```

Critical values for stopping

```
simtrials <- function(v){</pre>
 co <- ppcutoffs(v$critv[3])</pre>
                                                     Creates a big matrix to
 #out.mat
                                                     store simulation results
 # (1) N
 \# (2-4) N per group
 # (5-7) Rank as 1, 2, 3 (according to prob best)
 # (8) Sig best (1 2 or 3 or 0 if none)
 # (9) Sig worst (1 2 or 3 or 0 if none)
 # (10) Final conclusion
 #
             1 = overall futility stop,
 #
             2 = stop early for winner
 #
             3 = stop early for winner & loser
 #
             4 = stop early for loser and futility (not possible in ours)
 #
              5 = max overall futility
 #
             6 = \max and loser
 #
             7 = \max and winner
 #
             8 = max & winner & loser
 # (11-13) Final Pr(best)
 # (14-16) Final Pr(2nd)
 # (17-19) Final Pr(worst)
    (20-22) Successes per group
 #
    (23-25) Ever drop arm? (rand goes to 0 at any pt)
 #
```

```
Simulate group assignment
out.mat <- matrix(NA, nrow=v$nsims, ncol=25)</pre>
                                                        & response to tx
  for(s in 1:v$nsims){
    ad <- c(1,1,1)
    ## Rand assignment for first FirstLook pts & generate outcome
    group <- rep(NA, v$MaxN)</pre>
    group[1:v$firstlook] <- rand.new(v$firstlook, c(1,1,1))</pre>
    y \leq rep(NA, v \leq MaxN)
    v[1:v$firstlook] <- sim.endpoint(group[1:v$firstlook], v$S3)</pre>
    look1 <- interim(v$firstlook, y, group, v, co)</pre>
#
    print(round(look1,3))
                                                         First interim look
    # Track if arm every dropped
    ad <- ad * as.numeric(look1[12:14]>0)
    n.now <- v$firstlook</pre>
    print(c(s,n.now))
                                                        Simulate group assignment
## Now loop through Stage 1
    while (look1[1]==1) {
                                                        & response to tx
      new <- min(v$MaxN-n.now, v$lookevery)</pre>
      group[(n.now+1):(n.now+new)] <- rand.new(new, look1[12:14])</pre>
      y[(n.now+1):(n.now+new)] <- sim.endpoint(group[(n.now+1):(n.now+new)], v$S3)</pre>
      look1 <- interim(n.now+new, y, group, v, co)</pre>
#
      print(round(look1,3))
                                                    Do interim looks
      ad <- ad * as.numeric(look1[12:14]>0)
      n.now <- n.now+new
      print(c(s,n.now))
    }
```

```
mx <- look1[3:5]; mn <- look1[6:8]</pre>
   winner <- ifelse(max(mx) > v$critv[1], (1:3)[mx==max(mx)], 0)
   loser <- ifelse(max(mn) > v critv[2], (1:3)[mn==max(mn)], 0)
  if(look1[2]==1){
                                                See if best or worst identified
      whystop <- 1 ## futility</pre>
    }else if(look1[2]==3){
      if(loser>0){
        whystop <-3
      }else{
        whystop <-2
                                                     See if stopping rules met
      }
    }else if(look1[2]==2){
      if(winner==0 & loser==0) { whystop <- 5}</pre>
      else if(winner>0 & loser>0){ whystop <- 8}</pre>
      else if(winner>0)
                                 { whystop <-7 }
      else if(loser>0)
                                 { whystop <-6 }
      else{print("error why stop at max?")}
                                                               Print out simulation
      else{print("error, why did trial stop?")}
                                                               results
out.mat[s,1:25] <- c(n.now, look1[18:20], order(mx), winner, loser,</pre>
                whystop,look1[c(3,4,5,9,10,11,6,7,8,15,16,17)],1-ad)
   out.mat <- data.frame(out.mat)</pre>
   names(out.mat) <- c("N", "N1", "N2", "N3",...</pre>
    return(out.mat)
```

}

```
rand.new <- function(N, p, minp){
    ### Returns randomization codes (1:3) for N patients
    ### requires prob vector, p, of lenght 3.
    ### If
    if(prod(p ==c(1,1,1))==1){
        out <- rep(sample(1:3,3), ceiling(N/3))
        out <- out[1:N]
    }else{
        out <- rep(sample(1:3, N, prob=p, replace=T))
    }
    return(out)
}</pre>
```

Takes how many patients to simulate, N Rand prob , p And Min rand prob minp

```
## Simulates data for new patients using inputs group assignement and success rate
(length 3)
sim.endpoint <- function(group, successrate){
   out <- rbinom(length(group), 1, successrate[group])
}</pre>
```

Simulate a success or failure for each based given their group assignment group is vector of 1,2 or 3 successrate is length 3

Predictive Probability Cutoffs Lookup Matrix

```
### Creates a lookup matrix to make the predictive probability stopping algorithm
go faster.
### Creates a 99.9% confidence interval, then basically sees if its' highly
likely that the stop rate is less than the cutoff
ppcutoffs <- function(critv){</pre>
    whenstop <- cbind(rep(0,1000),rep(0,1000))</pre>
    for(i in 50:1000){
    x <- ceiling(critv*i)</pre>
    while(as.numeric(binom.test(x,i,conf.level=0.999)$conf.int[1])<critv){</pre>
    x < - x+1
    whenstop[i,1] <- x
    }
    when stop [1:49,1] < - when stop [50,1]
    for(i in 50:1000){
    x <- ceiling(critv*i)</pre>
    while(as.numeric(binom.test(x,i,conf.level=0.999)$conf.int[1])>=critv){
    x <- x-1
    }
    whenstop[i,2] <- x
    }
    return(whenstop)
}
```

```
interim <- function(N, y, group, v, co){</pre>
                                                           Does interim analysis
  ## Runs trial returns:
  # (1) go (0=stop, 1=keep going)
                                                           Calc posteriors, new
  # (2) why stop (1=3-way fut, 2=max n, 3=1 winner)
                                                           rand probs,
  \# (3-5) Pr each is best
  # (6-8) Pr each is worst
                                                           Pred prob of success
  # (9-11) x/N for each group
  # (12-14) rand probs
                                                           at max
  ns <- table(factor(group[1:N], levels=1:3))</pre>
  tab <- table(factor(group[1:N],levels=1:3), factor(y[1:N], levels=0:1))</pre>
  post1 <- rbeta(10000, v$a[1]+tab[1,2], v$b[1]+tab[1,1])</pre>
  post2 <- rbeta(10000, v$a[2]+tab[2,2], v$b[2]+tab[2,1])</pre>
                                                                    Calc posteriors
  post3 <- rbeta(10000, v$a[3]+tab[3,2], v$b[3]+tab[3,1])</pre>
  vr <- as.numeric(( (v$a+tab[,2])*(v$b+tab[,1])) / ((v$a+v$b+ns)^2 * (v$a+v$b+ns+1)))</pre>
  top <- apply(cbind(post1,post2,post3), 1, max)</pre>
  bot <- apply(cbind(post1,post2,post3), 1, min)</pre>
  best <- c(mean(post1==top), mean(post2==top), mean(post3==top))</pre>
  worst <- c(mean(post1==bot), mean(post2==bot), mean(post3==bot)) Calc prob each is
  middle <- 1-best-worst
                                                                   best & worst
  toobad <- 1-c(pbeta(v$badlim, v$a[1]+tab[1,2], v$b[1]+tab[1,1]),</pre>
              pbeta(v$badlim, v$a[2]+tab[2,2], v$b[2]+tab[2,1]),
              pbeta(v$badlim, v$a[3]+tab[3,2], v$b[3]+tab[3,1]))
                                                                    Calc Pr(p<0.25)
  wt <- sqrt(best * vr / as.numeric(ns)); wt <- wt/sum(wt)</pre>
  wt[wt < v$minpr] <- 0; wt[toobad < v$critv[4]] <- 0</pre>
  if(sum(wt) > 0){
                                                               Calc new rand prob
  wt <- wt/sum(wt)</pre>
   }
```

```
sumtrial <- function(outmat){</pre>
  mat <- matrix(nrow=4, ncol=9)</pre>
  out <- table(factor(outmat[,10], levels=1:8))</pre>
#
               Ntotal SDN phat Rank1 Rank2 Rank3 SigBest SigWorst Drop
#
       fPHT
                                            Takes the results of 'simtrials' and
#
       LVT
#
       VPA
                        _ _
                                            Produces prettier output
#
       Total
  mat[1:3,1] <- apply(outmat[,2:4], 2, mean) ### Average Patients per arm</pre>
  mat[1:3,2] <- apply(outmat[,2:4], 2, sd) ### SD patients per arm</pre>
  mat[1:3,3] \leq c(mean(outmat[,20]/outmat[,2]), mean(outmat[,21]/outmat[,3]),
                                                ### Average successes per arm
mean(outmat[,22]/outmat[,4]))
  mat[1,4:6] <- table(factor(outmat[,5], levels=3:1))/dim(outmat)[1] ## Avg Pr Best</pre>
  mat[2,4:6] <- table(factor(outmat[,6], levels=3:1))/dim(outmat)[1] ## Avg Pr middle</pre>
  mat[3,4:6] <- table(factor(outmat[,7], levels=3:1))/dim(outmat)[1] ## Avg Pr Worst</pre>
  mat[1:3,7] <- table(factor(outmat[,8], levels=1:3))/dim(outmat)[1] ## Pr Sig Best</pre>
  mat[1:3,8] <- table(factor(outmat[,9], levels=1:3))/dim(outmat)[1] ## Pr Sig Worst</pre>
  mat[1:3,9] <- apply(outmat[,23:25], 2, mean)</pre>
                                                                          ## Pr Ever Dropped
  mat[4,1] <- mean(outmat[,1])  ### Mean total sample size</pre>
  mat[4,2] <- sd(outmat[,1])  ### SD total sample size</pre>
  mat[4,3] <- mean(rowSums(outmat[,20:22]) / rowSums(outmat[2:4])) ### Mean response rate</pre>
per arm
  mat[4, 4:6] <- NA
  mat[4,7] <- sum(mat[1:3,7])  ### Total prob ID a sig best</pre>
  mat[4,8] <- sum(mat[1:3,8]) ### Total prob ID a sig worst</pre>
  mat[4,9] <- NA
  mat <- data.frame(mat)</pre>
  names(mat) <- c("N", "SD", "Phat", "Best", "Mid", "Worst", "SigBest", "SigWorst", "Drop")</pre>
  dimnames(mat)[[1]] <- c("fPHT","LVT","VPA","Total")</pre>
  return(list(out, mat))
```

}

```
#####PRED PROBS; only do if all 3 arms left
   if((N >= v$firststop) & (N < v$MaxN) & (prod(wt>0)> 0)){
     drop <- 0
     left <- v$MaxN - N
                                                     Calc pred prob of success
     left <- ceiling(rep(left/3, 3))</pre>
     ns.total <- ns+left</pre>
                                                     At Max N
     winlose <- 0
     counter <-1
     while((winlose < co[counter,1]) & (winlose >= co[counter,2]) & (counter < 1000)){</pre>
       y.end <- tab[,2] + rbetabin.ab(3, left, v$a+tab[,2], v$b+tab[,1])</pre>
       post1f <- rbeta(10000, v$a[1]+y.end[1], v$b[1]+ns.total[1]-y.end[1])</pre>
       post2f <- rbeta(10000, v$a[2]+y.end[2], v$b[2]+ns.total[2]-y.end[2])</pre>
       post3f <- rbeta(10000, v$a[3]+y.end[3], v$b[3]+ns.total[3]-y.end[3])</pre>
       topf <- apply(cbind(post1f,post2f,post3f), 1, max)</pre>
       botf <- apply(cbind(post1f,post2f,post3f), 1, min)</pre>
       bestf <- c(mean(post1f==topf), mean(post2f==topf), mean(post3f==topf))</pre>
       worstf <- c(mean(post1f==botf), mean(post2f==botf), mean(post3f==botf))</pre>
       winlose <- winlose + ifelse((max(bestf)>v$critv[1]) | (max(worstf)>v$critv[2]),
1, 0)
       counter < - counter + 1
#
        print(c(winlose/counter, counter))
     }
     ppwin <- winlose/counter</pre>
   }else{
     drop <-1
     ppwin <- v$critv[3]+1 # If missing just make bigger than the crit value.
   }
```

```
## Stopping:
if(N < v$firststop){</pre>
  go <- 1
  whystop <- NA
}else if(N >= v$MaxN){
  go <- 0
  whystop <-2
}else if(max(best) > v$critv[1]){
  go <- 0
  whystop <-3
}else if(ppwin < v$critv[3]){</pre>
  qo <- 0
  whystop <-1
}else if(wt[1]==0 & wt[2]==0 & wt[3]==0){
  go <- 0
 whystop <-1
}else{
  qo <- 1
 whystop <- NA
}
```

```
Track IF stop
And WHY stop
```

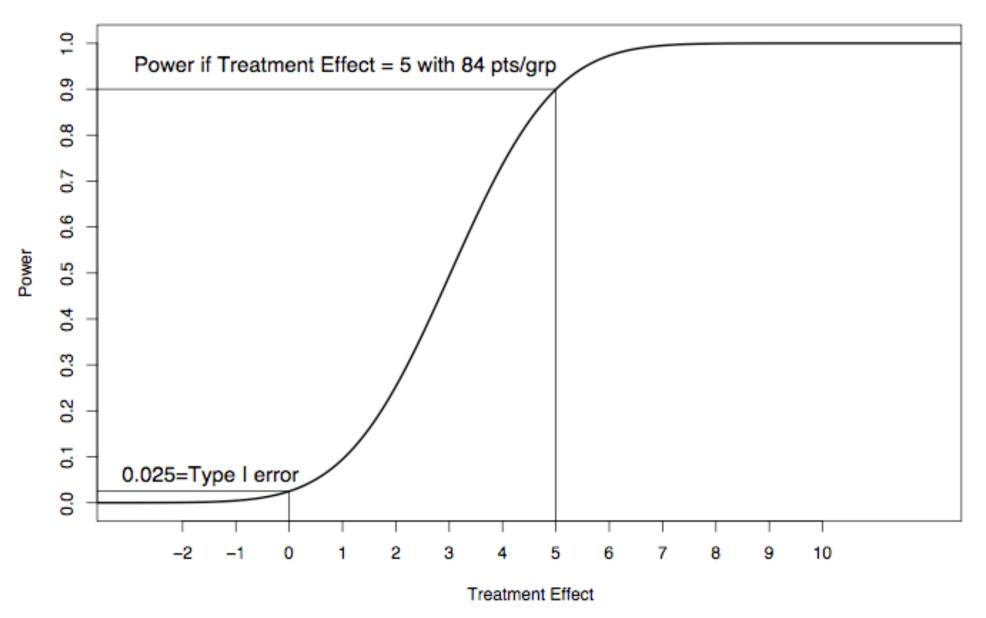
```
return(as.numeric(c(go, whystop, best, worst, middle, wt, tab[,2], ns, ppwin, drop)))
```

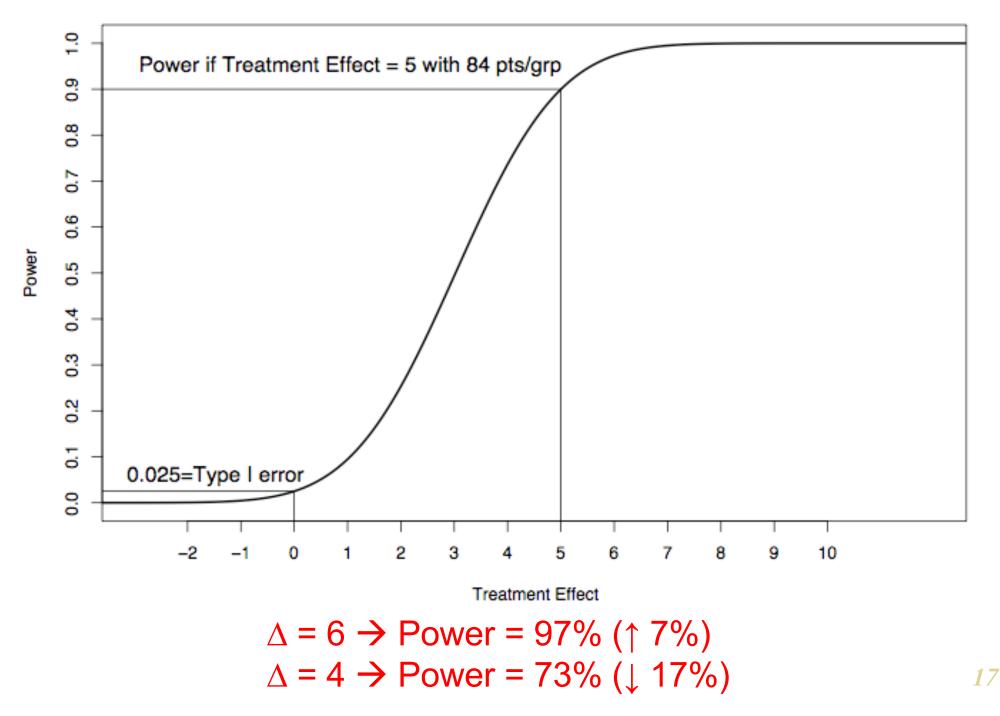
}

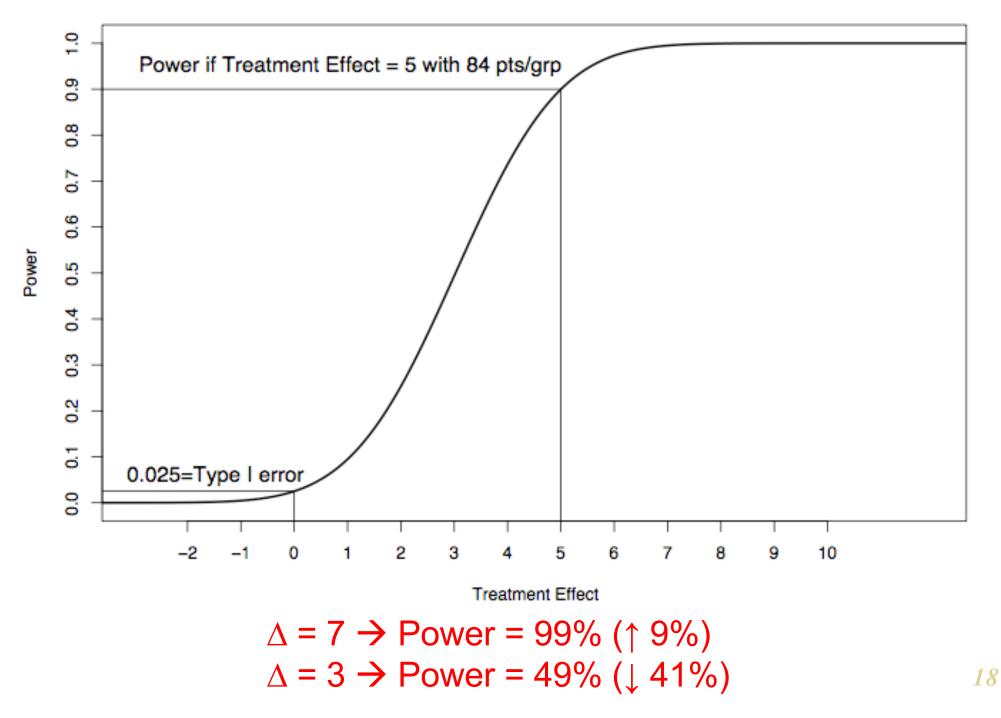
Predictive Probabilities

Power vs. Prob of Success

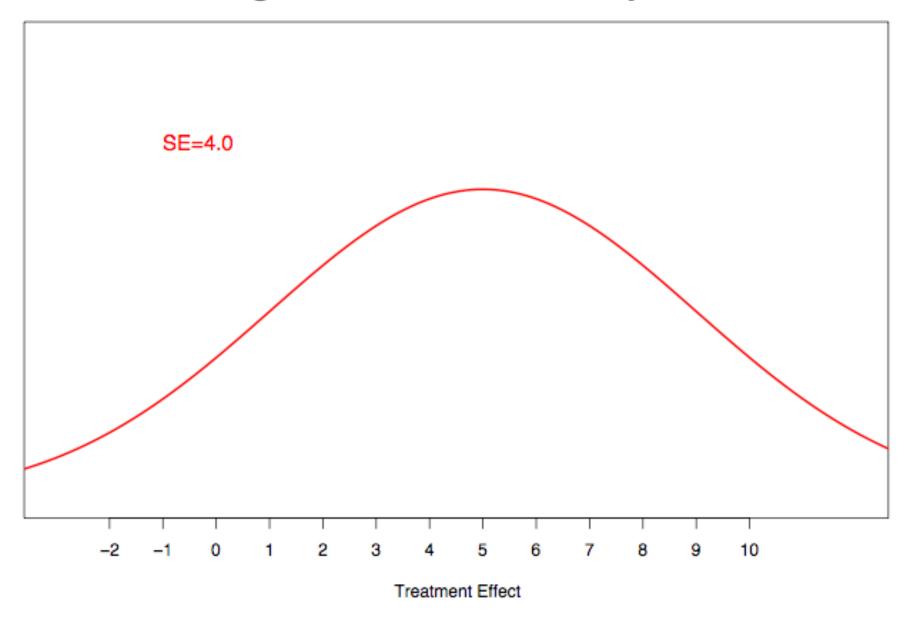
- Doctor comes to you.
- Claims her treatment increases IQ by 5 points
- SD = 10
- "How many patients do I need to have 90% power to demonstrate superiority?"



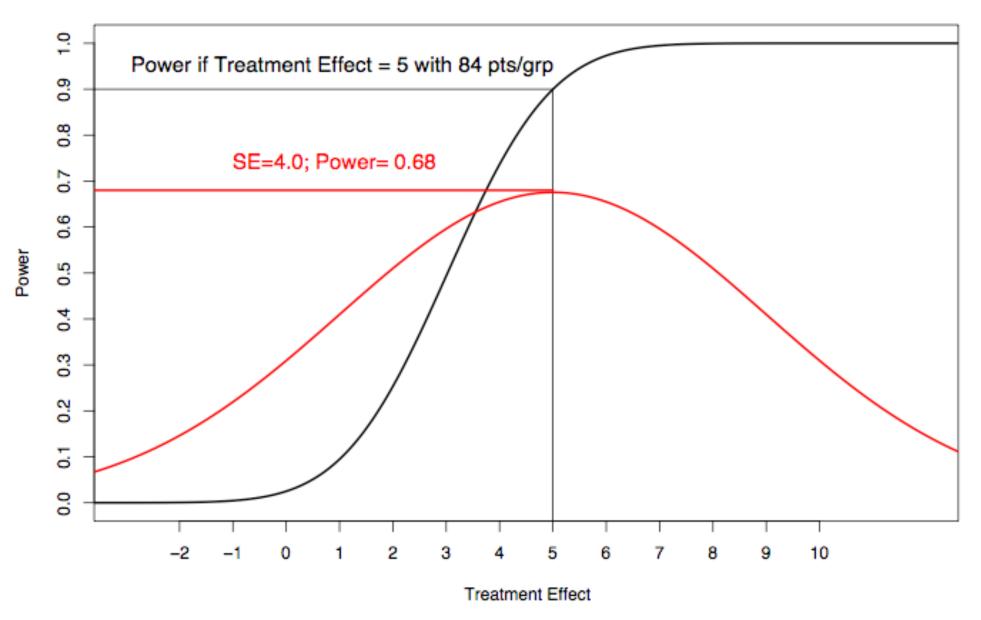




We've ignored the error in the pilot data



Estimate 5.0 (95% CI -3 to 13)



Probability of success < Power due to Jensen's inequality $_{20}$

Simple Trial

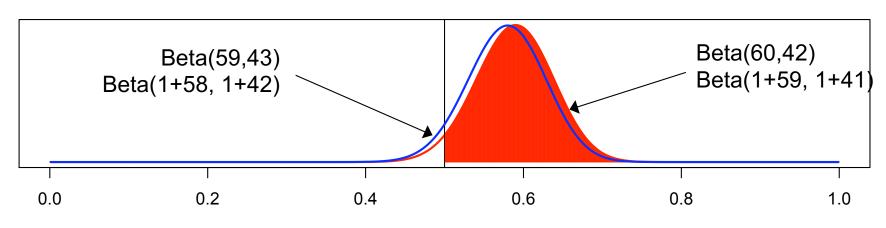
- Binomial data
- One-armed trial
- n = 100
- Need to show p > 0.5
- $H_0: p \le 0.5$
- H_a: p > 0.5
- FYI: 59/100 → Frequentist p-value = 0.044
 & 1-sided 95% CI (0.503 1.00)

Phase 3 & Priors

- Simple Trial:
 - Binary data. Observe $x \sim Bin(100,p)$
 - Need to show Pr(p > 0.5 | x out of 100) > 0.95
 - Assume $p \sim Beta(1,1)$ prior
 - $-\Pr(p \ge 0.5 \mid 59 \text{ out of } 100) = 0.963$

1-sided p-value < 0.05 approx posterior > 0.95

 $-\Pr(P > 0.5 | 58 \text{ out of } 100) = 0.944$

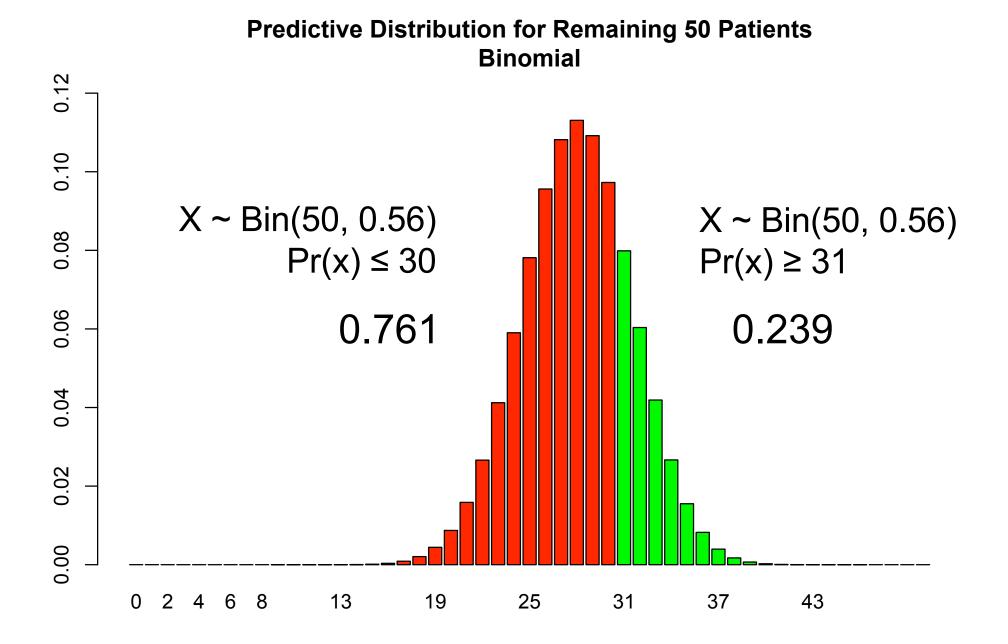


Phase 3 & Priors

- Simple Trial:
 - Binary data. Observe $x \sim Bin(100,p)$
 - Need to show Pr(p > 0.5 | x out of 100) > 0.95
 - Assume $p \sim Beta(1,1)$ prior
 - $-\Pr(p > 0.5 | 59 \text{ out of } 100) = 0.963$
 - Pr(P > 0.5 | 58 out of 100) = 0.944
- $Pr(X \ge 59 | p = 0.50) = 0.044$
 - Simple binomial calculation
 - This is Type I error and is < 5%
 - Bayesian trial
 - Good frequentist properties

Predictive Probabilities

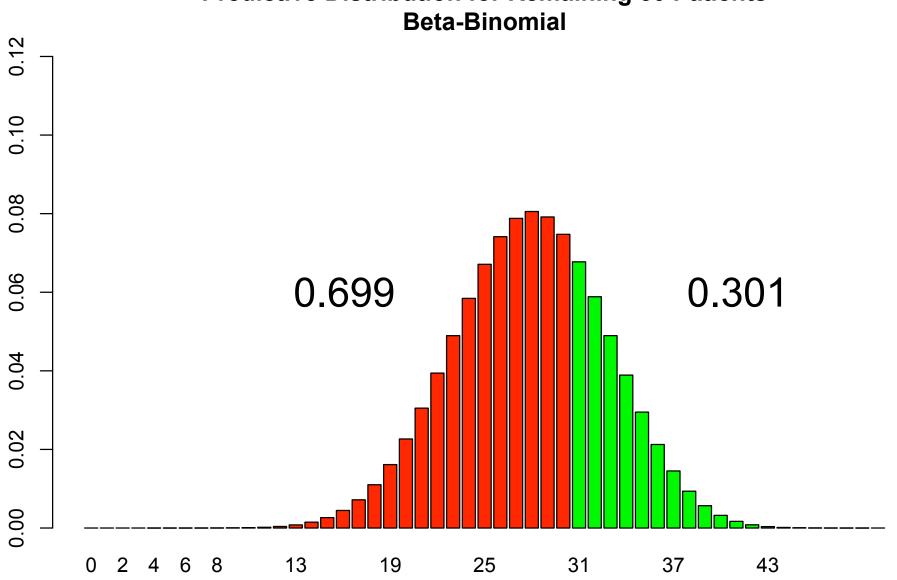
- Simple Trial:
 - Binary data. Observe $x \sim Bin(100, p)$
 - Need to show Pr(p > 0.5 | x out of 100) > 0.95
 - Assume $p \sim \text{Beta}(1,1)$ prior
 - $-\Pr(p > 0.5 \mid 59 \text{ out of } 100) = 0.963$
 - $-\Pr(p > 0.5 \mid 58 \text{ out of } 100) = 0.944$
- Observe data half way through
 - See 28/50 successes
 - Need to see 31/50 to meet threshold
 - What is predictive probability of trial success?



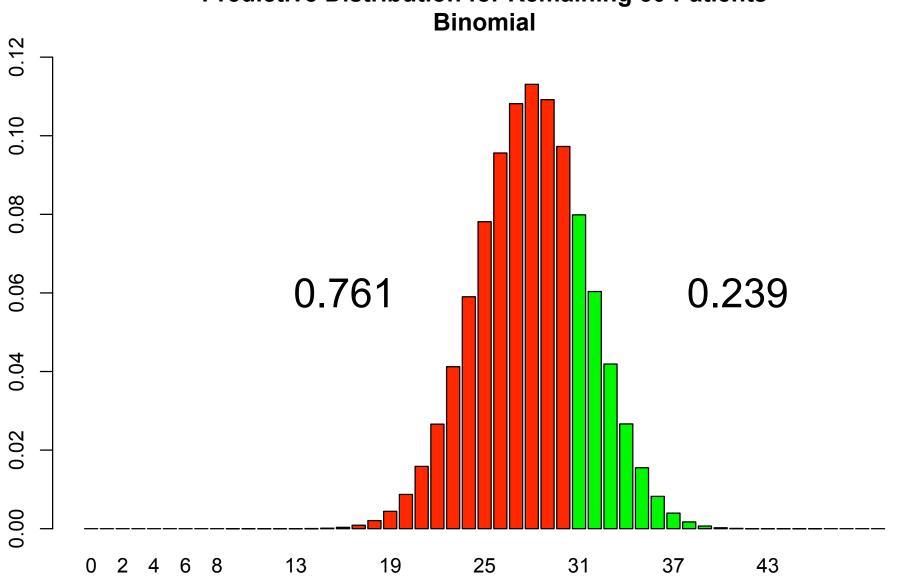
Predictive Probabilities

- Know we need $x \ge 59$ at trial's end
- Have $x_1 = 28$
- Need $x_2 \ge 31$
- $p \sim \text{Beta}(1+28, 1+22)$
- $x_2 \sim \text{Binomial}(50, p)$
- $x_2 \sim \text{Beta-binomial}(50, \alpha = 29, \beta = 23)$

$$\Pr(\text{Win Trial}) = \sum_{x_2=31}^{30} \left\{ \binom{50}{x_2} \frac{B(x_2+29,50-x_2+23)}{B(29,22)} \right\} = 0.301$$



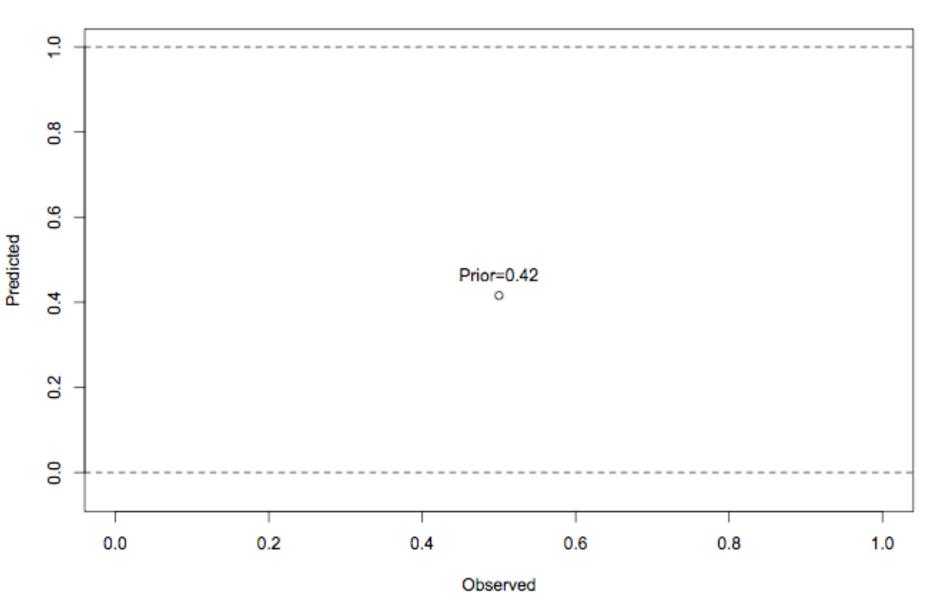
Predictive Distribution for Remaining 50 Patients



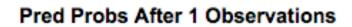
Predictive Distribution for Remaining 50 Patients

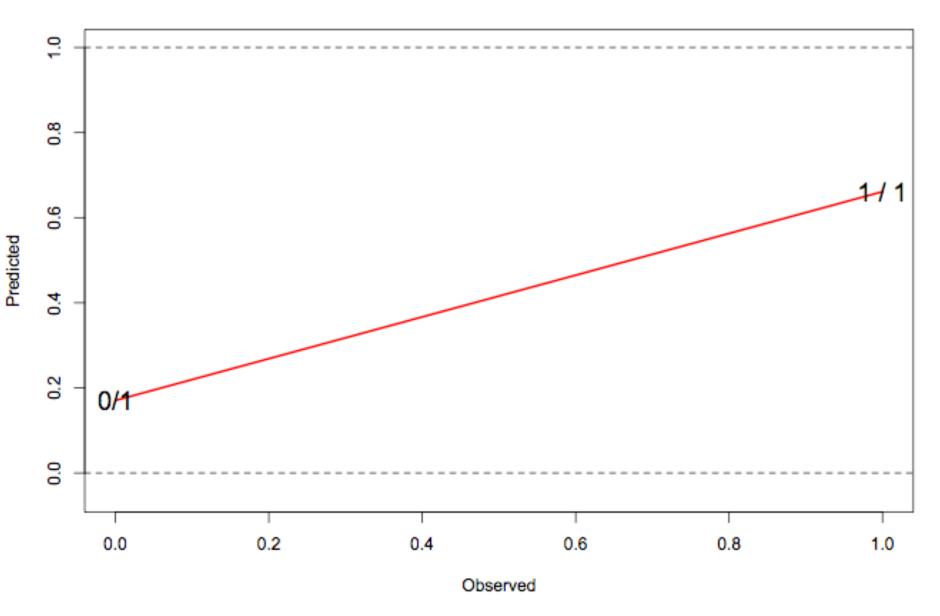
R code for predictive probability

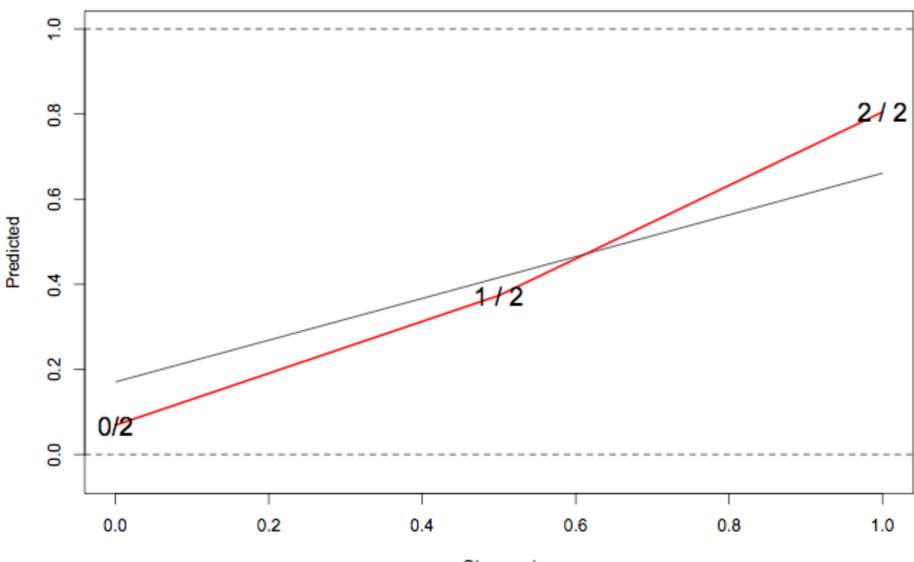
```
> ### VIA SIMULATION
> alpha <- 1; beta <- 1</pre>
> x <- 28; N <- 50
>
> p <- rbeta(1000000, alpha+x, beta+N-x)
> x.new <- rbinom(1000000, 50, p)</pre>
>
> mean(x.new >= 31)
[1] 0.301132
>
>
>
> ### VIA DIRECT CALCULATION
> N.new <- 50
> x.new <- 0:50
> prob <- choose(N.new,x.new) *</pre>
       beta(alpha+x+x.new,(beta+N-x)+(N-x.new)) /
+
+
          beta(alpha+x, (beta+N-x))
> sum(prob)
[1] 1
> sum(prob[x.new >= 31])
[1] 0.3010906
> barplot(prob, names.arg=0:50, col=c(rep(2,31), rep(3,20)),
         main="Predictive Distribution for Remaining 50 patients")
+
```



Pred Probs After 0 Observations

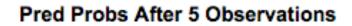


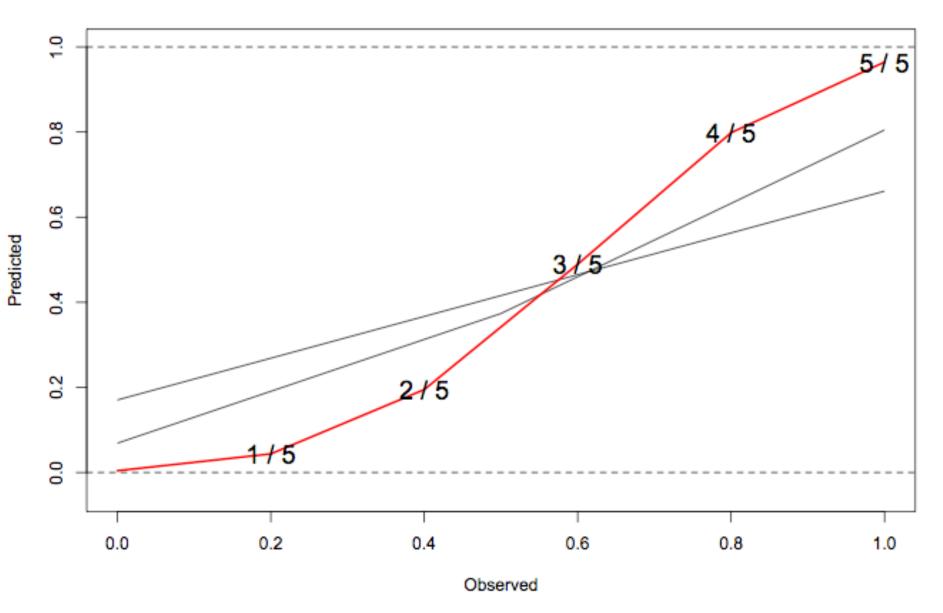


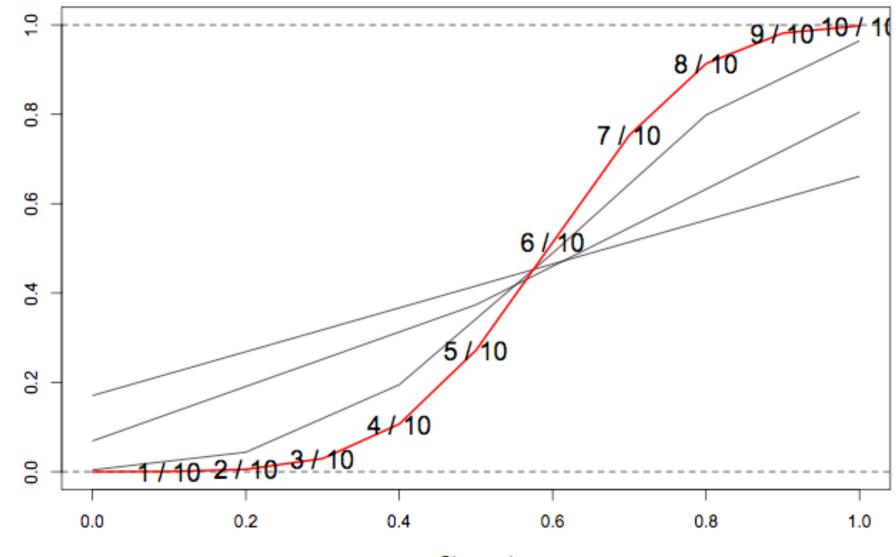


Pred Probs After 2 Observations

Observed



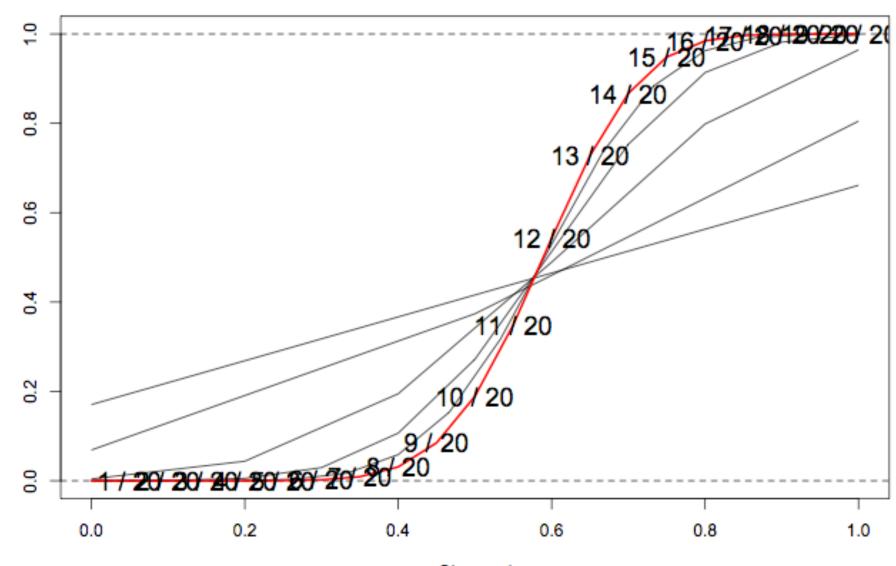




Predicted

Pred Probs After 10 Observations

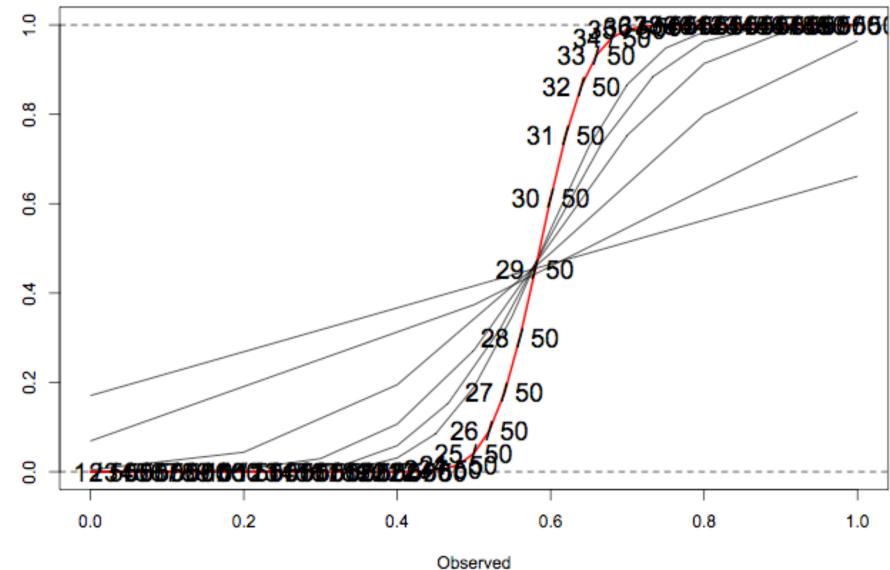
Observed

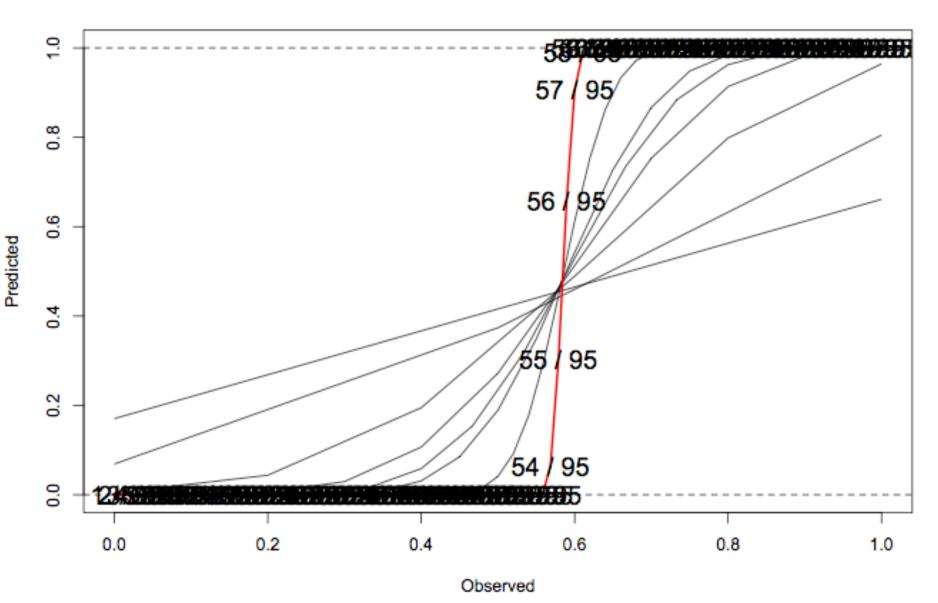


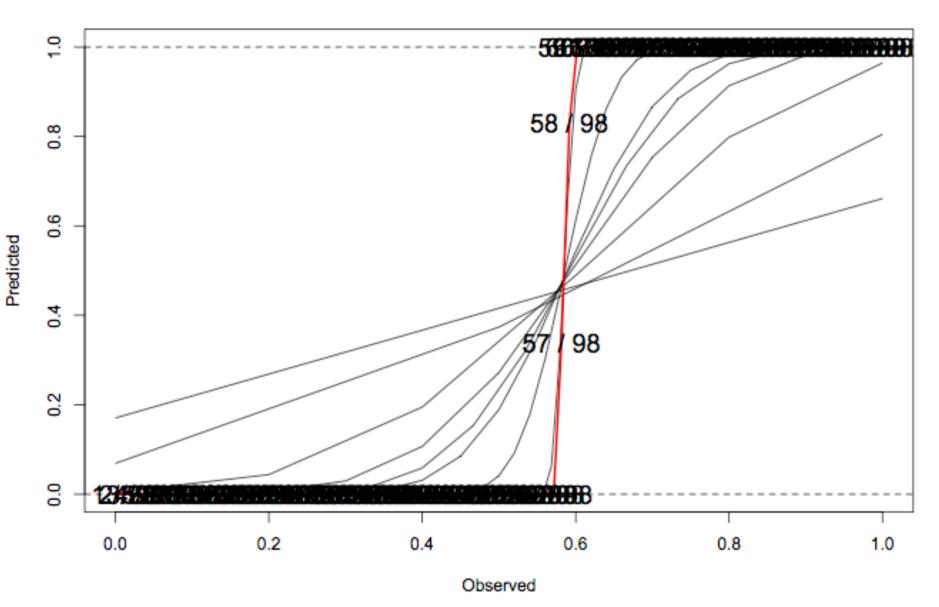
Predicted

Pred Probs After 20 Observations

Observed

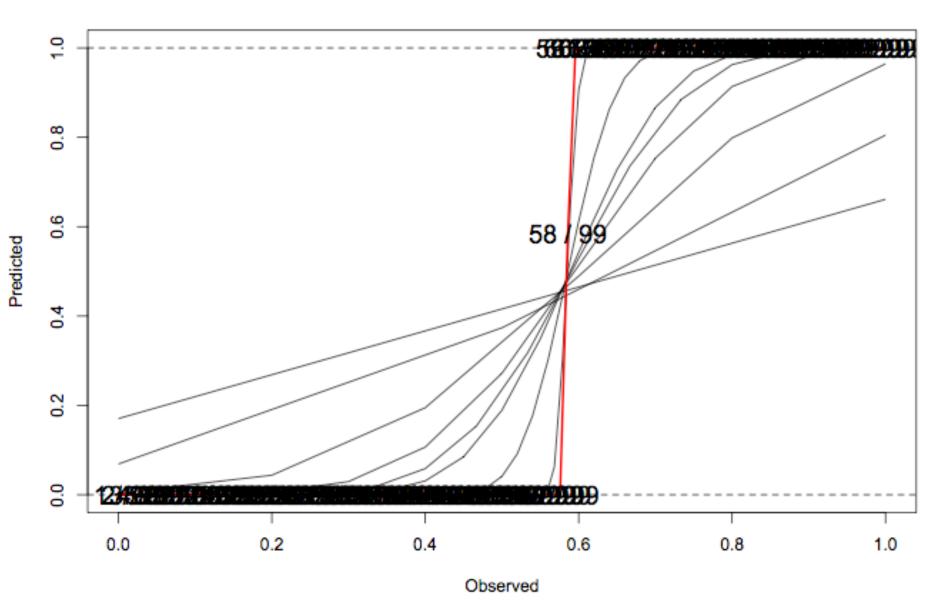






Pred Probs After 98 Observations

38



Pred Probs After 99 Observations

- Observe 12 / 20 (60%)
 - Need 47 / 80 successes; 59% or better rest of way
 - p-value = 0.25, Pr(p > 0.5) = 0.81
 - Predictive probability of success (a) 100 = 0.54

• Observe 12 / 20 (60%)

- Need 47 / 80 successes; 59% or better rest of way

- p-value = 0.25, $\Pr(p > 0.5) = 0.81$
- Predictive probability of success @ 100 = 0.54
- Observe 28 / 50 (56%)
 - Need 31/50 successes; 62% or better rest of way
 - p-value = 0.24, $\Pr(p > 0.5) = 0.80$
 - Predictive probability of success @ 100 = 0.30

• Observe 12 / 20 (60%)

- Need 47 / 80 successes; 59% or better rest of way

- p-value = 0.25, Pr(p>0.5) = 0.81
- Predictive probability of success @ 100 = 0.54
- Observe 28 / 50 (56%)
 - Need 31/50 successes; 62% or better rest of way
 - p-value = 0.24, Pr(p > 0.5) = 0.80
 - Predictive probability of success (a) 100 = 0.30
- Observe 41 / 75 (54.7%)
 - Need 18/25 successes; 72% or better rest of way
 - p-value = 0.24, Pr(p > 0.5) = 0.79
 - Predictive probability of success @ 100 = 0.086

• Observe 12 / 20 (60%)

- Need 47 / 80 successes; 59% or better rest of way

- -p-value = 0.25, $\Pr(p > 0.5) = 0.81$
- Predictive probability of success @ 100 = 0.54
- Observe 28 / 50 (56%)
 - Need 31/50 successes; 62% or better rest of way
 - -p-value = 0.24, $\Pr(p > 0.5) = 0.80$
 - Predictive probability of success @ 100 = 0.30
- Observe 41 / 75 (54.7%)
 - Need 18/25 successes; 72% or better rest of way
 - -p-value = 0.24, Pr(p>0.5) = 0.79
 - Predictive probability of success (a) 100 = 0.086

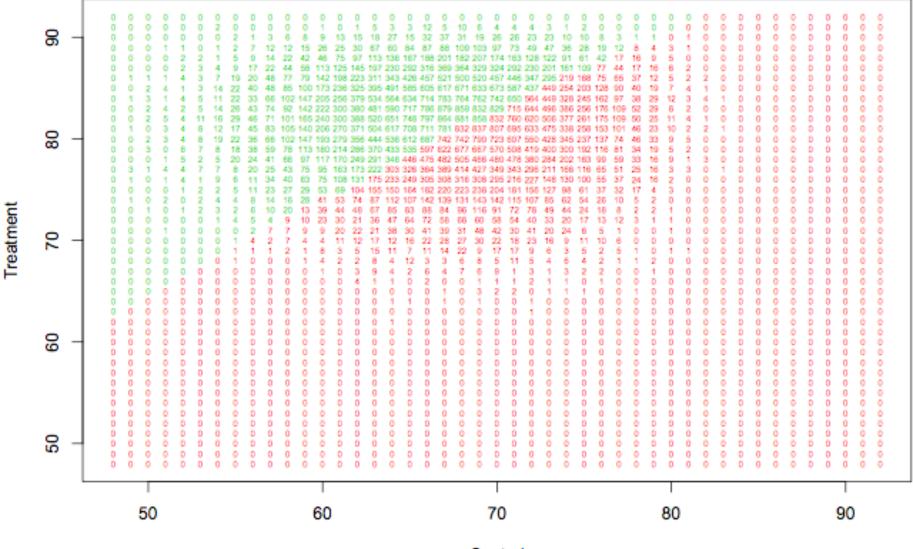
Another trial

- $N_G = 100$ in Treatment & Control Group
- Testing $p_t > p_c$ using Fisher's Exact Test @ 0.025
- Observe
 - 34/50 in Control Group
 - 41/50 in Treatment Group
- What is predictive probability of success?

```
alpha < -1; beta < -1
xc <- 34; nc <- 50
xt <- 41; nt <- 50
pc <- rbeta(100000, alpha+xc, beta+nc-xc)</pre>
pt <- rbeta(100000, alpha+xt, beta+nt-xt)</pre>
xc.total <- xc + rbinom(100000, 50, pc)
xt.total <- xt + rbinom(100000, 50, pt)</pre>
p.values <- rep(NA,100000)
for(i in 1:100000){
  p.values[i] <- fisher.test(</pre>
      matrix(c(xc.total[i], 100-xc.total[i],
                xt.total[i], 100-xt.total[i]),nrow=2),
                alternative="less")$p.value
}
> mean(p.value<0.025)</pre>
[1] 0.549
```

GREEN numbers are when it's statistically superior RED are cases not significant

Predictive Probability = 0.549



Example: Phase 2 Trials

Phase 2 Trials

- Early phase results
 - Animal studies showed promise for disease
 - Phase 1 showed non-toxic in healthy humans
- Questions for Phase 2
 - Does the treatment work in humans
 - Which dose is best
 - Which dose(s) to take to Phase 3
 - Is an dose with promising efficacy also safe
 - What is likelihood of Phase 3 success

Adaptive Randomization Strategies

- Bandits
- Play the Winner
- Randomized Play the Winner
- Randomize ~ Pr(Best Treatment)
- Randomize ~ f(Pr(Best Treatment))
- Randomize ~ Dose that gives the most information
- One of these with constraints

Adaptation

- Multiple trial characteristics may be changed during the course of the trial based on accumulating data
- Must pre-prescribe changes
 - Available Doses
 - Randomization proportions
 - Time of interim analyses
 - Maximum sample size
 - Dose dropping rules
 - Allow doses to re-enter?

Example In Uterine Cancer

- Phase 2 dose finding trial
- 3-armed RCT
 - Control chemotherapy
 - Control + experimental treatment q2w
 - Control + experimental treatment q1w
- Goals
 - Treat patients effectively & ethically
 - Learn about experimental treatment
 - Explore adaptive designs
 - This company's first attempt at an adaptive design

Trial Setup

- Primary Outcome
 - Progression Free Survival (PFS)
 - $-\lambda_c = Rate of PFS$ in Control population
 - $-\lambda_2 = Rate of PFS in Control + q2w population$
 - $-\lambda_1 = Rate of PFS in Control + q1w population$
- Expectation
 - Control mean PFS = 303 days, median = 210
 - Accrual
 - 1 patient every 3 days for first 45 pts (135 days)
 - 1 patient every 2 days thereafter
- Need to beat control by 10% to be marketable

Factors to Consider

- Statistical Model
 - Parametric dose-response curve, non-parametric, independent arms
 - Historical vs. vague priors
- How many doses
- Maximum sample size
- Timing of first interim analysis
- Timing of subsequent interim analyses
 - Time based or patient based
- Randomization scheme
- Rules to drop doses
- Rules to allow doses to re-enter
- Rules to stop for futility
- Rules to stop for success
- How long to track patients after last patient enrolled

Statistical Model

- Assume time-to-progression exponential
- Priors on rates:

 $\lambda_{c,} \lambda_{2,} \lambda_{1} \sim \Gamma(1, 303 \text{ days})$

• Posteriors

 λ_d | Data ~ $\Gamma(1 + \#$ Progressors, 303+Exposure Time)

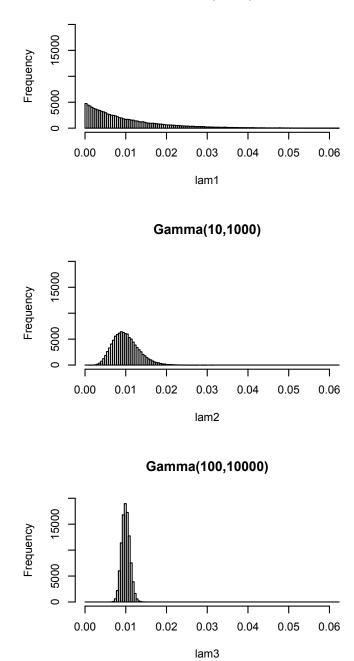
Also calculate probability each dose is best
 "best" = has lowest PFS rate

$$-p_{c} = \Pr(\lambda_{c} < \lambda_{2} & \lambda_{c} < \lambda_{1})$$
$$-p_{2} = \Pr(\lambda_{2} < \lambda_{c} & \lambda_{2} < \lambda_{1})$$
$$-p_{1} = \Pr(\lambda_{1} < \lambda_{c} & \lambda_{1} < \lambda_{2})$$

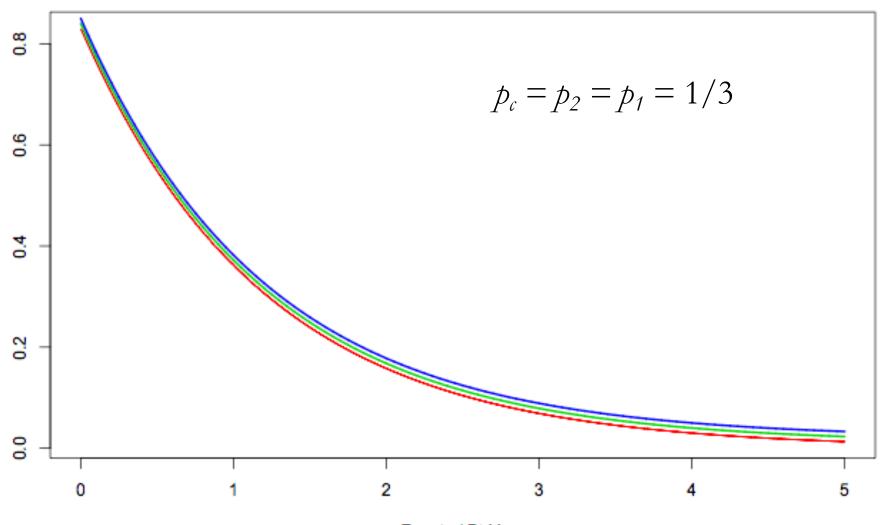
Example

```
> lam1 <- rgamma(100000, 1, 100)
> lam2 <- rgamma(100000, 10, 1000)
> lam3 <- rgamma(100000, 100, 10000)
> par(mfrow=c(3,1))
```

```
> mean(lam1 < lam2 & lam1 < lam3)
[1] 0.5738
> mean(lam2 < lam1 & lam2 < lam3)
[1] 0.24854
> mean(lam3 < lam1 & lam2 > lam3)
[1] 0.17766
```





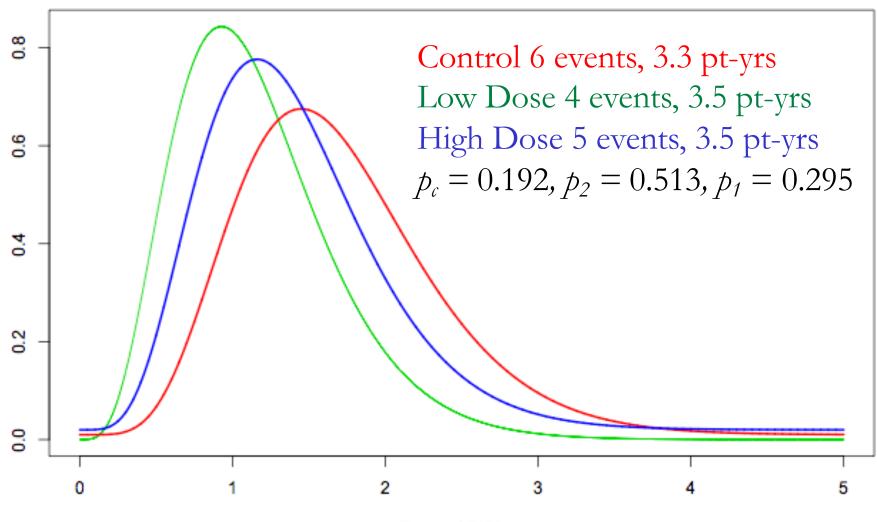


Events / Pt-Year

Statistical Summary

- Primary Outcome: Progression free survival
 λ_t = PFS rate for Treatment *t*; *t* = A, B, C
- Statistical Assumptions and Modeling
 - PFS distributed $y_{i,t} \sim \text{Exp}(\lambda_t)$; t = A, B, C
 - Priors: λ_A, λ_B, λ_C ~ Γ(1, 303)
 Equals 1 subject with mean 303 days
 median = 210 days
 Median = Mean × log(2) for gamma dist
 Posteriors:
 - $\lambda_t \mid data \sim \Gamma(1 + \# \text{Events}_t, 303 + \text{Exposure}_t)$

Posteriors

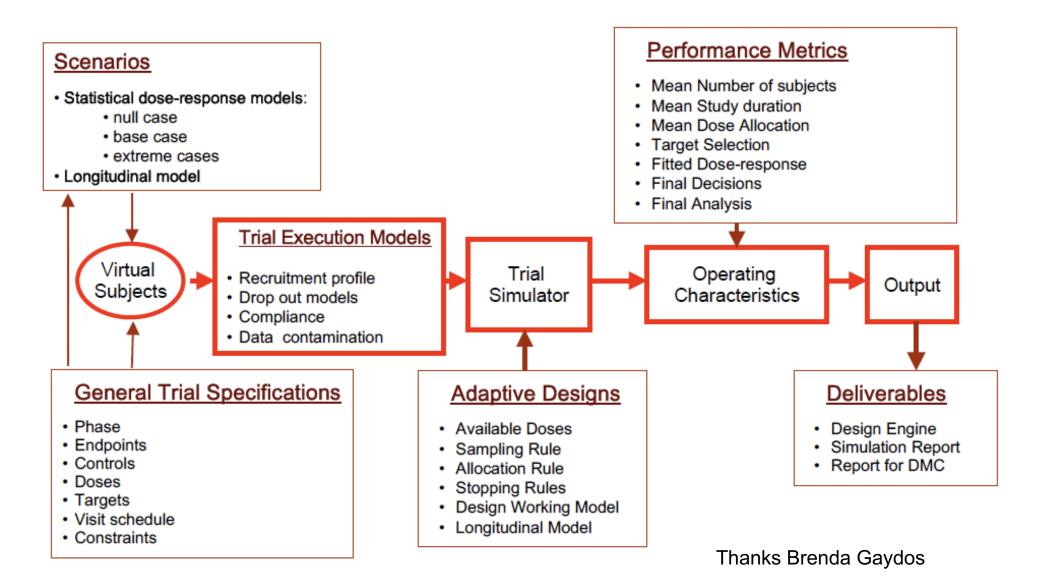


Events / Pt-Year

Complication I'll ignore

- In fact there were 2 types of patients platinum sensitive & platinum refractory
- Expect mean TTP shorter for refractory TTP in refractory = 2/7 that of sensitive
- Model event rates as $\gamma \lambda_d$ for refractory assume γ same across groups
- Prior on $\log(\gamma) \sim N(0, 10^2)$
- Means we no longer have conjugate priors must use Metropolis-Hastings algorithm

Simulation Plan

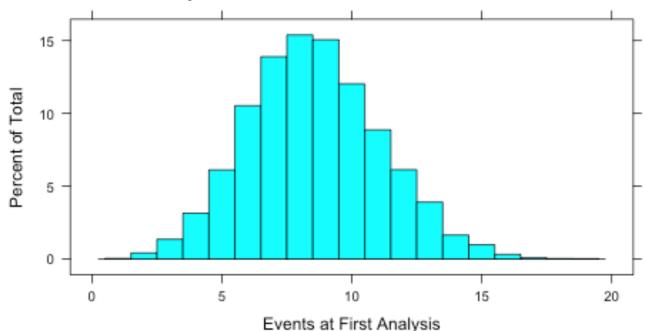


Maximum Sample Size

- Oftentimes determined by company resources
- Considered 150 & 195

Timing of interim analyses

- Expected accrual rate = 3 days per patient
 - 45 patients take 135 days
 - With expected $\lambda_c = 1/303$
 - Expect 8.5 events by 135 days
 - Median 8, IQR 7-10



Randomization

- Randomize first 45 patients 15:15:15
- Start interim analysis after 45th patient enrolled
- Repeat interim analyses every 15 patients
 - Approximately every 1 month with expected accrual
 - This timing worked logistically
 - Allowed blocks of 15 to ensure patients on each dose
- Open question: How to randomize?

Randomization Options

- Let r_d = randomization probability to dose d
- Let *p_d* = probability arm *d* has lowest (best) progression rate
- Randomization weighting by *C*

$$r_d = \frac{p_d^C}{p_1^C + p_2^C + p_3^C + \dots + p_D^C}$$

Randomization Options $r_{d} = \frac{p_{d}^{C}}{p_{1}^{C} + p_{2}^{C} + p_{3}^{C} + \dots + p_{D}^{C}}$

- C = 0, equal randomization ($r_d = 1$ /Number of Groups)
- C = 1, proportional to probability best $(r_d = p_d)$
- $C \ge 1$
 - strongly favor 1 arm earlier in the trial, even when treatments are equal
 - more subjects likely assigned to the best treatment
 - $C \rightarrow$ big means assign all to best treatment, play the leader
- 0 < C < 1
 - weakly favor better
 - fewer subjects likely assigned to best treatment
 - more even distribution early in trials
 - randomization less affected by early events
- C = n/N, trial begins with c = 0 and ends with c = 1

- When to Stop for Success?
 - If $p_2 > 0.95$, stop for success
 - If $p_1 > 0.95$, stop for success
 - Take successful dose to Phase III
- What if experimental doses equally effective?

- When to Stop for Success?
 - If $p_2 > 0.95$, stop for success
 - If $p_1 > 0.95$, stop for success
 - Take successful dose to Phase III

• What if experimental doses equally effective?

• Instead use if $p_C < 0.10$ or 0.05 to success stop?

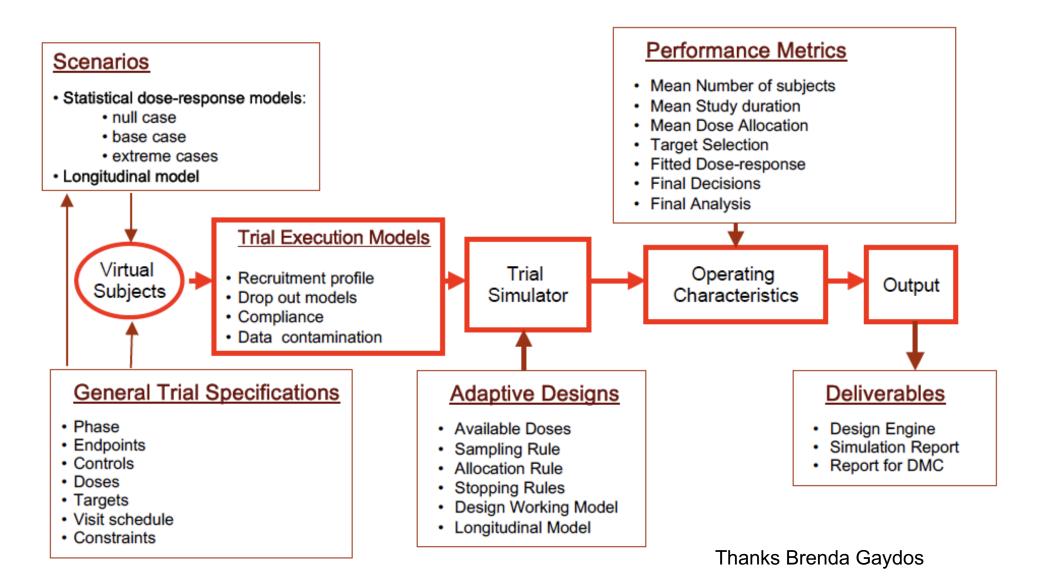
- When to Stop for Futility?
 - If $p_2 < 0.05$ drop q2w arm
 - If $p_1 < 0.05$ drop q1w arm
 - If both arms dropped, trial ends
 - Allow dropped arms to re-enter?

- When to Stop for Futility?
 - If $p_2 < 0.05$ drop q2w arm
 - If $p_1 < 0.05$ drop q1w arm
 - If $Pr(\lambda_c / \lambda_2 > 1.10 \mid \text{Data}) < 0.05 \text{ drop q2w arm}$
 - If $Pr(\lambda_c / \lambda_1 > 1.10 | \text{Data}) < 0.05 \text{ drop q1w arm}$
 - If both arms dropped, trial ends
 - Allow dropped arms to re-enter? Yes

Post Accrual Tracking

- Choose to track patients for 1-year post accrual
- 70% chance last patient will have event $1-e^{-365/303} = 0.70$
- Under assumed accrual rates & N=195, 83% of patients will have events if $\lambda = 1/303$.

Simulation Plan



At each interim analysis

1. Calculate:

Posteriors $\lambda_t \mid data; t \in A, B, C$ $p_t = P(\text{Treatment t is 'Best' treatment } \mid data)$ $e.g. p_B = P(\lambda_B \le \lambda_A \& \lambda_C \mid data)$ P(Treatment t is $\ge 10\%$ better than A | data)

- 2. Check superiority and futility stopping/dropping rules
- 3. Randomize next 15 subjects with probability p_t
- 4. Repeat steps 1-4 up to 195 subjects

Simulation Output

- Doing Case =
 9

 Control
 Mean TTP =
 303.00

 Control + q2w
 Mean TTP =
 606.00

 Control + q1w
 Mean TTP =
 606.00
- Stop for Success0.168Stop for Futility0.004Stop for Cap0.828

NameMeanN%NSDNBestWinBeatPControl30.48500.21410.89270.0030.0000.000Control + q2w55.87900.39219.55260.4920.0590.682Control + q1w56.24100.39419.08590.5050.0570.690

Total N = 142.605 SD= 20.247Pr(Either Beats Placebo) = 0.853

Max N = 150

Doing Case =	1	
Control	Mean TTP =	303.00
Control + q2w	Mean TTP =	303.00
Control + q1w	Mean TTP =	303.00

Stop for Success 0.049 Stop for Futility 0.073 Stop for Cap 0.878

NameMean N% NSD NBestWin Beat PControl47.65700.33418.00270.3420.0000.000Control + q2w47.00400.33019.24680.3100.0060.051Control + q1w47.94400.33619.32730.3480.0080.052

Total N = 142.605 SD= 22.106 Pr(Either Beats Placebo) = 0.081

Doing Case = 9 Control Mean TTP = 303.00 Control + q2w Mean TTP = 606.00

Control + q1w Mean TTP = 606.00

Stop for Success 0.168 Stop for Futility 0.004 Stop for Cap 0.828

NameMean N% NSD NBestWin Beat PControl**30.4850**0.21410.89270.0030.0000.000Control + q2w55.87900.39219.55260.4920.0590.682Control + q1w56.24100.39419.08590.5050.0570.690

Total N = 142.605 SD= 20.247 Pr(Either Beats Placebo) = **0.853**

Max N = 195

1	
Mean TTP =	303.00
Mean TTP =	303.00
Mean TTP =	303.00
	Mean TTP =

Stop for Success 0.070 Stop for Futility 0.103 Stop for Cap 0.827

NameMean N% NSD NBestWin Beat PControl60.31000.33325.43700.3310.0000.000Control + q2w60.90400.33628.13040.3460.0090.063Control + q1w59.97100.33127.78300.3230.0060.061

Total N = 181.185 SD= 35.625 Pr(Either Beats Placebo) = 0.102

Doing Case =9ControlMean TTP =303.00Control + q2wMean TTP =606.00Control + q1wMean TTP =606.00

Stop for Success 0.208 Stop for Futility 0.002 Stop for Cap 0.790

NameMean N% NSD NBestWin Beat PControl**35.1840**0.19513.79920.0010.0000.000Control + q2w72.17800.40027.50210.4910.047**0.757**Control + q1w72.98300.40527.18350.5080.053**0.766**

Total N = 180.345 SD= 33.923 Pr(Either Beats Placebo) = **0.907**

Max N = 195, Firstlook=45

Doing Case =	T	
Control	Mean TTP =	303.00
Control + q2w	Mean TTP =	303.00
Control + q1w	Mean TTP =	303.00

Stop for Success0.070Stop for Futility0.103Stop for Cap0.827

NameMean N% NSD NBestWin Beat PControl60.31000.33325.43700.3310.0000.000Control + q2w60.90400.33628.13040.3460.0090.063Control + q1w59.97100.33127.78300.3230.0060.061

Total N = **181.185** SD= 35.625 Pr(Either Beats Placebo) = 0.102

Doing Case =9ControlMean TTP =303.00Control + q2wMean TTP =606.00Control + q1wMean TTP =606.00

Stop for Success 0.208 Stop for Futility 0.002 Stop for Cap 0.790

NameMean N% NSD NBestWin Beat PControl35.18400.19513.79920.0010.0000.000Control + q2w72.17800.40027.50210.4910.0470.757Control + q1w72.98300.40527.18350.5080.0530.766

Total N = **180.345** SD= 33.923 Pr(Either Beats Placebo) = **0.907**

Max N = 195, Firstlook=90

 Doing Case =
 1

 Control
 Mean TTP =
 303.00

 Control + q2w
 Mean TTP =
 303.00

 Control + q1w
 Mean TTP =
 303.00

Stop for Success0.057Stop for Futility0.089Stop for Cap0.854

NameMean N% NSD NBestWin Beat PControl61.47500.33219.49080.3480.0000.000Control + q2w62.23400.33621.21990.3220.0050.042Control + q1w61.64600.33321.27510.3300.0060.041

Total N = **185.355** SD= 27.081 Pr(Either Beats Placebo) = 0.071

Doing Case =9ControlMean TTP =303.00Control + q2wMean TTP =606.00Control + q1wMean TTP =606.00

Stop for Success 0.199 Stop for Futility 0.000 Stop for Cap 0.801

NameMean N% NSD NBestWin Beat PControl41.0450**0.224**9.09060.0010.0000.000Control + q2w70.8100**0.387**20.64640.4990.0440.806Control + q1w71.1900**0.389**20.78050.5000.0460.809

Total N = **183.045** SD= 28.766 Pr(Either Beats Placebo) = 0.931

$\begin{array}{rcl} \text{Max N} = & 195, \ c = 1 \\ \text{Doing Case} = & 1 \\ \text{Control} & \text{Mean TTP} = & 303.00 \\ \text{Control} + & q2w & \text{Mean TTP} = & 303.00 \\ \text{Control} + & q1w & \text{Mean TTP} = & 303.00 \end{array}$	$\begin{array}{rcl} Max & N &=& 195, & c &=& 0\\ Doing Case &=& & 1\\ Control & Mean TTP &=& 303.00\\ Control + q2w & Mean TTP &=& 303.00\\ Control + q1w & Mean TTP &=& 303.00 \end{array}$
Stop for Success0.070Stop for Futility0.103Stop for Cap0.827	Stop for Success 0.063 Stop for Futility 0.118 Stop for Cap 0.819
Name Mean N % N SD N Best Win Beat P Control 60.3100 0.333 25.4370 0.331 0.000 0.000 Control + q2w 60.9040 0.336 28.1304 0.346 0.009 0.063 Control + q1w 59.9710 0.331 27.7830 0.323 0.006 0.061 Total N = 181.185 SD= 35.625 Pr(Either Beats Placebo) = 0.102	Name Mean N % N SD N Best Win Beat P Control 60.0350 0.333 12.3501 0.352 0.000 0.000 Control + q2w 60.0350 0.333 12.3501 0.331 0.009 0.044 Control + q1w 60.0350 0.333 12.3501 0.317 0.008 0.048 Total N = 180.105 SD= 37.050 Pr(Either Beats Placebo) = 0.083
Doing Case =9ControlMean TTP = 303.00 Control + q2wMean TTP = 606.00 Control + q1wMean TTP = 606.00	Doing Case =9ControlMean TTP = 303.00 Control + q2wMean TTP = 606.00 Control + q1wMean TTP = 606.00
Stop for Success0.208Stop for Futility0.002Stop for Cap0.790	Stop for Success0.195Stop for Futility0.004Stop for Cap0.801
Name Mean N % N SD N Best Win Beat P Control 35.1840 0.195 13.7992 0.001 0.000 0.000 Control + q2w 72.1780 0.400 27.5021 0.491 0.047 0.757 Control + q1w 72.9830 0.405 27.1835 0.508 0.053 0.766 Total N = 180.345 SD= 33.923	NameMean N% NSD NBestWin Beat PControl60.39500.33311.07790.0030.0000.000Control + q2w60.39500.33311.07790.4880.0460.828Control + q1w60.39500.33311.07790.5090.0470.828Total N =181.185SD=33.234
Pr(Either Beats Placebo) = 0.907	Pr(Either Beats Placebo) = 0.931

$\begin{array}{rcl} \text{Max N} &=& 195, \ c &=& 1\\ \text{Doing Case} &=& 1\\ \text{Control} && \text{Mean TTP} &=& 303.00\\ \text{Control} &+& q2w && \text{Mean TTP} &=& 303.00\\ \text{Control} &+& q1w && \text{Mean TTP} &=& 303.00 \end{array}$	$\begin{array}{rcl} \text{Max N} &=& 195, \text{ c} &=& \infty \\ \text{Doing Case} &=& 1 \\ \text{Control} & \text{Mean TTP} &=& 303.00 \\ \text{Control} + q2w & \text{Mean TTP} &=& 303.00 \\ \text{Control} + q1w & \text{Mean TTP} &=& 303.00 \end{array}$
Stop for Success 0.070 Stop for Futility 0.103 Stop for Cap 0.827	Stop for Success 0.047 Stop for Futility 0.092 Stop for Cap 0.861
Name Mean N % N SD N Best Win Beat P Control 60.3100 0.333 25.4370 0.331 0.000 0.000 Control + q2w 60.9040 0.336 28.1304 0.346 0.009 0.063 Control + q1w 59.9710 0.331 27.7830 0.323 0.006 0.061 Total N = 181.185 SD= 35.625 Pr(Either Beats Placebo) = 0.102	Name Mean N % N SD N Best Win Beat P Control 60.4500 0.330 43.6835 0.347 0.000 0.000 Control + q2w 61.6800 0.336 45.8555 0.339 0.009 0.061 Control + q1w 61.2900 0.334 45.4790 0.314 0.002 0.057 Total N = 183.420 SD= 32.733 Pr(Either Beats Placebo) = 0.092
Doing Case = 9 Control Mean TTP = 303.00 Control + q2w Mean TTP = 606.00 Control + q1w Mean TTP = 606.00	Doing Case =9ControlMean TTP = 303.00 Control + q2wMean TTP = 606.00 Control + q1wMean TTP = 606.00
Stop for Success0.208Stop for Futility0.002Stop for Cap0.790	Stop for Success0.201Stop for Futility0.003Stop for Cap0.796
Name Mean N % N SD N Best Win Beat P Control 35.1840 0.195 13.7992 0.001 0.000 0.000 Control + q2w 72.1780 0.400 27.5021 0.491 0.047 0.757 Control + q1w 72.9830 0.405 27.1835 0.508 0.053 0.766 Total N = 180.345 SD= 33.923	Name Mean N % N SD N Best Win Beat P Control 24.1950 0.134 18.5007 0.004 0.000 0.000 Control + q2w 78.3450 0.435 51.8603 0.498 0.049 0.570 Control + q1w 77.7000 0.431 50.7603 0.498 0.043 0.561 Total N = 180.240 SD= 34.519
Pr(Either Beats Placebo) = 0.907	Pr(Either Beats Placebo) = 0.772

Max N = 195, $c = \infty$	Max N = 195, c = ∞ , every 1
Doing Case = 1	Doing Case = 1
Control Mean TTP = 303.00	Control Mean TTP = 303.00
Control + q2w Mean TTP = 303.00	Control + q2w Mean TTP = 303.00
Mean TTP = 303.00	Control + q1w Mean TTP = 303.00
Stop for Success0.047Stop for Futility0.092Stop for Cap0.861	Stop for Success 0.099 Stop for Futility 0.120 Stop for Cap 0.781
Name Mean N %N SD N Best Win Beat P	Name Mean N % N SD N Best Win Beat P
Control 60.4500 0.330 43.6835 0.347 0.000 0.000	Control 55.6170 0.319 40.6723 0.311 0.000 0.000
Control + q2w 61.6800 0.336 45.8555 0.339 0.009 0.061	Control + q2w 61.1370 0.350 45.0447 0.352 0.006 0.047
Control + q1w 61.2900 0.334 45.4790 0.314 0.002 0.057	Control + q1w 57.8350 0.331 44.5945 0.337 0.006 0.049
Total N = 183.420 SD= 32.733	Total N = 174.589 SD= 44.094
Pr(Either Beats Placebo) = 0.092	Pr(Either Beats Placebo) = 0.081
Doing Case =9ControlMean TTP = 303.00 Control + q2wMean TTP = 606.00 Control + q1wMean TTP = 606.00	Doing Case =9ControlMean TTP = 303.00 Control + q2wMean TTP = 606.00 Control + q1wMean TTP = 606.00
Stop for Success 0.201	Stop for Success 0.263
Stop for Futility 0.003	Stop for Futility 0.004
Stop for Cap 0.796	Stop for Cap 0.733
Name Mean N % N SD N Best Win Beat P	Name Mean N % N SD N Best Win Beat P
Control 24.1950 0.134 18.5007 0.004 0.000 0.000	Control 23.5280 0.136 17.2205 0.004 0.000 0.000
Control + q2w 78.3450 0.435 51.8603 0.498 0.049 0.570	Control + q2w 75.4290 0.435 49.9018 0.514 0.043 0.582
Control + q1w 77.7000 0.431 50.7603 0.498 0.043 0.561	Control + q1w 74.5200 0.430 50.4509 0.482 0.046 0.581
Total N = 180.240 SD= 34.519	Total N = 173.477 SD= 42.012
Pr(Either Beats Placebo) = 0.772	Pr(Either Beats Placebo) = 0.770

$\begin{array}{rcl} \text{Max N} &=& 195, \ c &=& 1\\ \text{Doing Case} &=& 1\\ \text{Control} && \text{Mean TTP} &=& 303.00\\ \text{Control} &+& q2w && \text{Mean TTP} &=& 303.00\\ \text{Control} &+& q1w && \text{Mean TTP} &=& 303.00 \end{array}$	$\begin{array}{rcl} Max & N &=& 195, & c &=& n/N \\ \hline Doing Case &=& 1 \\ Control & Mean TTP &=& 303.00 \\ Control + q2w & Mean TTP &=& 303.00 \\ Control + q1w & Mean TTP &=& 303.00 \end{array}$
Stop for Success0.070Stop for Futility0.103Stop for Cap0.827	Stop for Success 0.070 Stop for Futility 0.106 Stop for Cap 0.824
Name Mean N % N SD N Best Win Beat P Control 60.3100 0.333 25.4370 0.331 0.000 0.000 Control + q2w 60.9040 0.336 28.1304 0.346 0.009 0.063 Control + q1w 59.9710 0.331 27.7830 0.323 0.006 0.061 Total N = 181.185 SD= 35.625 Pr(Either Beats Placebo) = 0.102	Name Mean N % N SD N Best Win Beat P Control 61.3110 0.340 19.6030 0.335 0.000 0.000 Control + q2w 59.4440 0.330 22.8840 0.344 0.006 0.048 Control + q1w 59.6200 0.331 22.5230 0.321 0.007 0.049 Total N = 180.375 SD= 36.095 Pr(Either Beats Placebo) = 0.083
Doing Case =9ControlMean TTP = 303.00 Control + q2wMean TTP = 606.00 Control + q1wMean TTP = 606.00	Doing Case = 9 Control Mean TTP = 303.00 Control + q2w Mean TTP = 606.00 Control + q1w Mean TTP = 606.00
Stop for Success0.208Stop for Futility0.002Stop for Cap0.790	Stop for Success0.212Stop for Futility0.001Stop for Cap0.787
Name Mean N % N SD N Best Win Beat P Control 35.1840 0.195 13.7992 0.001 0.000 0.000 Control + q2w 72.1780 0.400 27.5021 0.491 0.047 0.757 Control + q1w 72.9830 0.405 27.1835 0.508 0.053 0.766 Total N = 180.345 SD= 33.923 Pr(Either Beats Placebo) = 0.907	Name Mean N % N SD N Best Win Beat P Control 40.8990 0.226 12.3915 0.000 0.000 0.000 Control + q2w 70.4020 0.389 21.1026 0.523 0.055 0.810 Control + q1w 69.4940 0.384 20.5548 0.477 0.063 0.804 Total N = 180.795 SD= 33.749 Pr(Either Beats Placebo) = 0.937

$\begin{array}{rcl} \text{Max N} &=& 195, \ c &=& 1\\ \text{Doing Case} &=& 1\\ \text{Control} && \text{Mean TTP} &=& 303.00\\ \text{Control} &+& q2w && \text{Mean TTP} &=& 303.00\\ \text{Control} &+& q1w && \text{Mean TTP} &=& 303.00 \end{array}$	$\begin{array}{rcl} Max & N &=& 195, & c &=& n/N \\ \mbox{Doing Case} &=& 1 \\ \mbox{Control} & & Mean TTP &=& 303.00 \\ \mbox{Control} + q2w & & Mean TTP &=& 303.00 \\ \mbox{Control} + q1w & & Mean TTP &=& 303.00 \end{array}$
Stop for Success0.070Stop for Futility0.103Stop for Cap0.827	Stop for Success 0.070 Stop for Futility 0.106 Stop for Cap 0.824
Name Mean N % N SD N Best Win Beat P Control 60.3100 0.333 25.4370 0.331 0.000 0.000 Control + q2w 60.9040 0.336 28.1304 0.346 0.009 0.063 Control + q1w 59.9710 0.331 27.7830 0.323 0.006 0.061 Total N = 181.185 SD= 35.625 Pr(Either Beats Placebo) = 0.102	Name Mean N % N SD N Best Win Beat P Control 61.3110 0.340 19.6030 0.335 0.000 0.000 Control + q2w 59.4440 0.330 22.8840 0.344 0.006 0.048 Control + q1w 59.6200 0.331 22.5230 0.321 0.007 0.049 Total N = 180.375 SD= 36.095 Pr(Either Beats Placebo) = 0.083
Doing Case = 9 Control Mean TTP = 303.00 Control + q2w Mean TTP = 606.00 Control + q1w Mean TTP = 606.00	Doing Case = 9 Control Mean TTP = 303.00 Control + q2w Mean TTP = 606.00 Control + q1w Mean TTP = 606.00
Stop for Success0.208Stop for Futility0.002Stop for Cap0.790	Stop for Success 0.212 Stop for Futility 0.001 Stop for Cap 0.787
Name Mean N % N SD N Best Win Beat P Control 35.1840 0.195 13.7992 0.001 0.000 0.000 Control + q2w 72.1780 0.400 27.5021 0.491 0.047 0.757 Control + q1w 72.9830 0.405 27.1835 0.508 0.053 0.766 Total N = 180.345 SD= 33.923	Name Mean N & N SD N Best Win Beat P Control 40.8990 0.226 12.3915 0.000 0.000 0.000 Control + q2w 70.4020 0.389 21.1026 0.523 0.055 0.810 Control + q1w 69.4940 0.384 20.5548 0.477 0.063 0.804 Total N = 180.795 SD= 33.749
Pr(Either Beats Placebo) = 0.907	Pr(Either Beats Placebo) = 0.937

Design Parameters

- First look @ 45
- Interim analyses every 15 patients
- Maximum = 195 patients
- Success
 - If $P_2 > 0.95$, stop for success
 - If $P_1 > 0.95$, stop for success
 - Take successful dose to Phase III
- Futility
 - If $Pr(\lambda_c / \lambda_2 > 1.10 \mid \text{Data}) < 0.05 \text{ drop q2w arm}$
 - If $Pr(\lambda_c / \lambda_1 > 1.10 | \text{Data}) < 0.05 \text{ drop q1w arm}$
 - If both arms dropped, trial ends

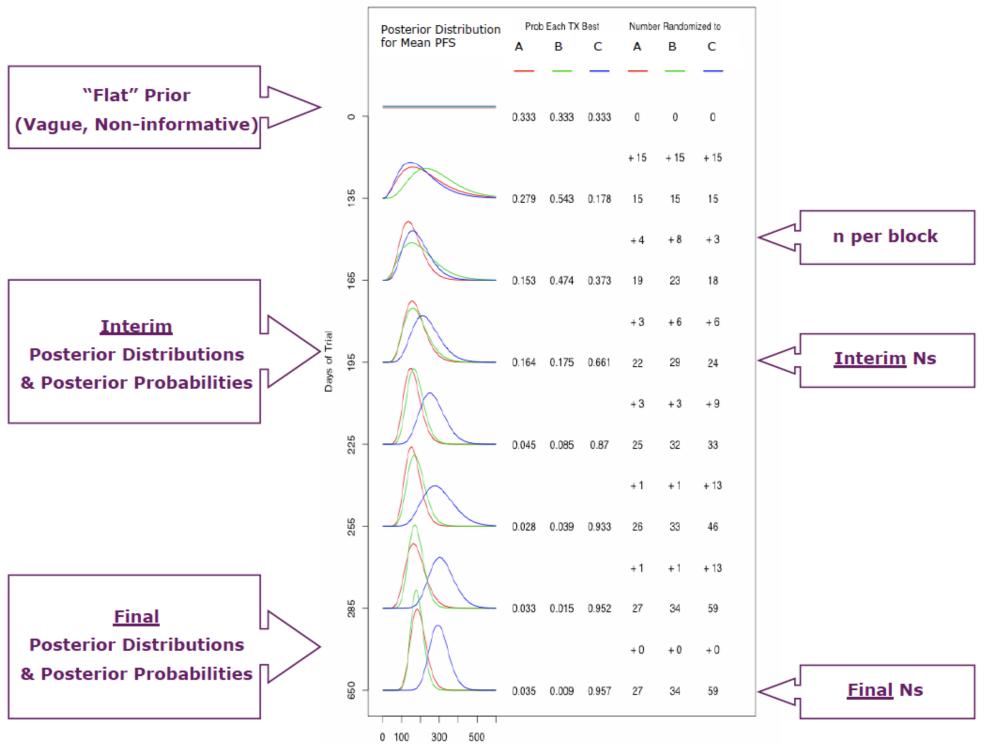
Show Individual Trials

• Best way to illustrate the adaptive design is to show example trials to collaborators

Show Individual Trials

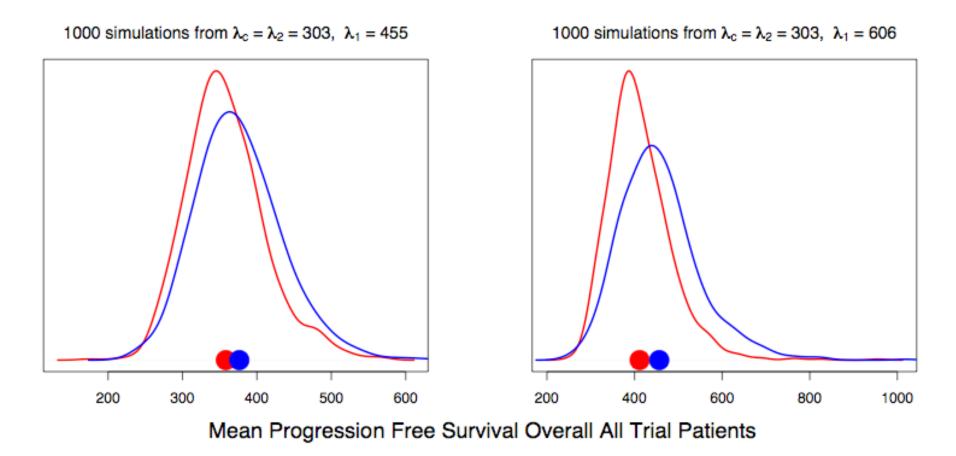
• Best way to illustrate the adaptive design is to show example trials to collaborators

• GREAT for debugging!



Output I Shared (Make it prettier)

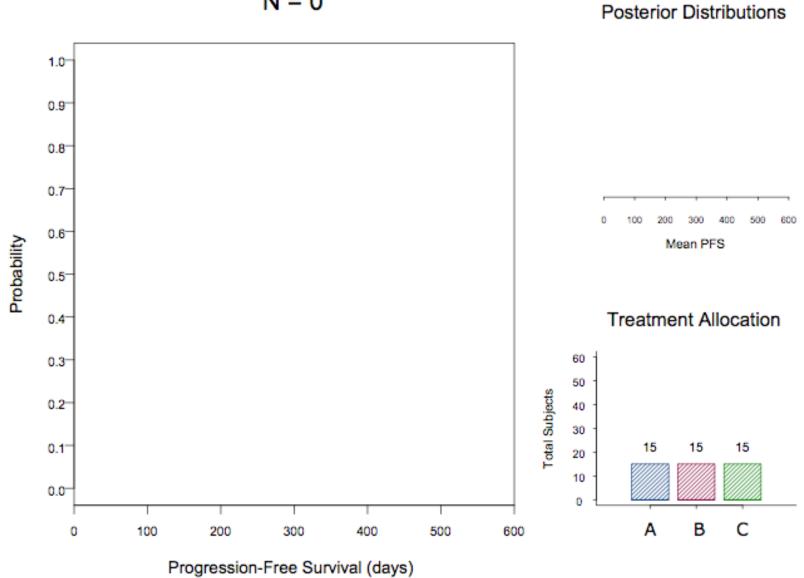
	Mean		Mean		Pr(Beat		
Treatment	PFS	⁰∕₀∆	Ν	SD	Pr(Best)	Pr(Win)	Control)
Control	303		59.7	25.3	0.343	0.000	
+q2w	303	$\mathrm{No}\Delta$	59.7	28.4	0.322	0.007	0.054
+q1w	303	$\mathrm{No}\Delta$	60.0	28.5	0.335	0.008	0.053
	Pr(Stop for Success) = 0.071						
			179.4	38.7	Pr(Stop for Futility) = 0.117		
Fully Adaptive Trial			1/9.4	30.7	Pr(Stop	for Max N)	= 0.813
	Pr(Either Beats Control) = 0.090						
Mean Mean Pr(Be					Pr(Beat		
Treatment	PFS	%∆	Ν	SD	Pr(Best)	Pr(Win)	Control)
Control	303		34.0	14.2	0.001	0.000	
+q2w	455	+50%	56.9	27.0	0.099	0.002	0.462
+q1w	606	+100%	79.4	28.6	0.900	0.351	0.881
Pr(Stop for Success) = 0.345						= 0.345	
		170 2	42.0	Pr(Stop for Futility) = 0.004			
Fully Adaptive Trial		170.3	43.2	Pr(Stop	for Max N)	= 0.650	
					\ F		
					(



C=1	C=0		C=1	C=0
141.0	140.4	Ν	135.3	135.5
40.4	40.3	Pr(q1w Beat Placebo)	75.2	75.2
47.2	33.0	% to Best Dose	51.7	33.0
374	354	Overall Mean PFS	460	404
60.3	39.7	Pr(Avg. Patient Lives Longer)	64.3	35.7

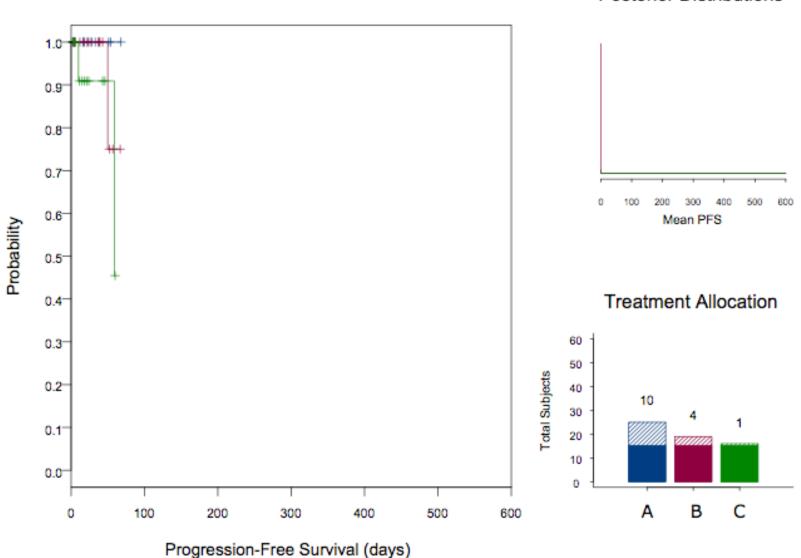
The trial is over!

This is how it really went.



N = 0

Expected @ Day 135; Actual Day 67



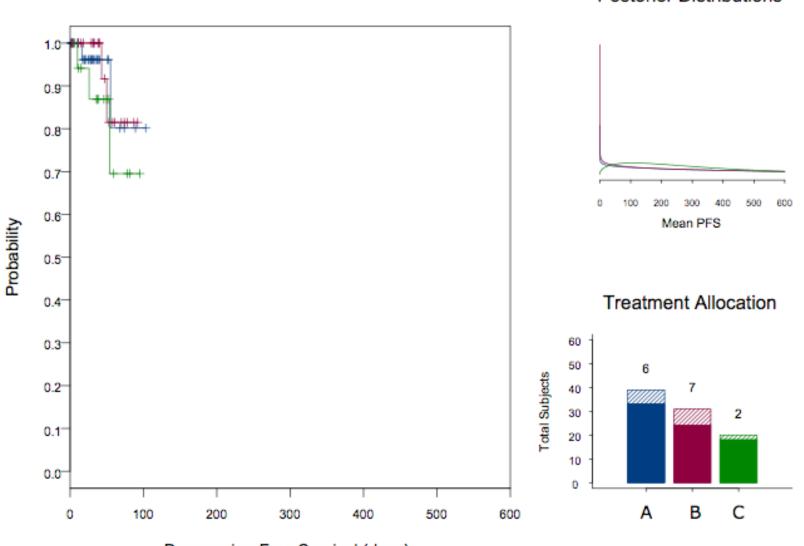
N = 45

Expected @ Day 165; Day 87

1.0 0.9 0.8 0.7 600 100 200300 400 500 0.6 Probability Mean PFS 0.5 Treatment Allocation 0.4 60 0.3 50 Total Subjects 8 0.2 40 5 30 2 0.1 20 10 0.0-0 С В А 100 200 300 500 400 600 0 Progression-Free Survival (days)

N = 60

Expected @ Day 195; Day 106

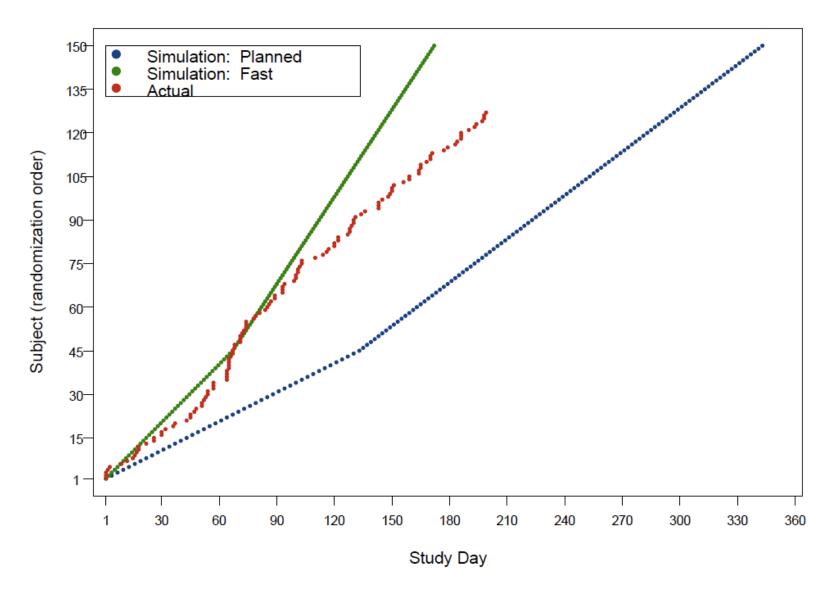


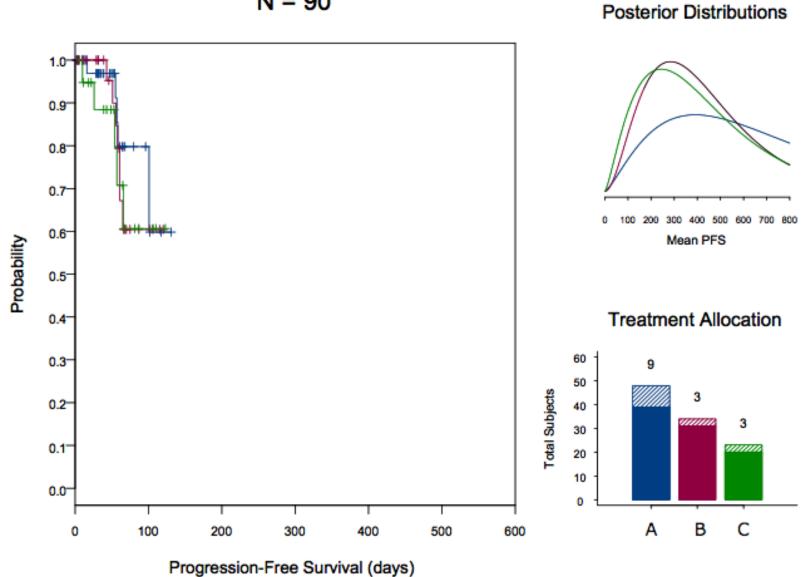
N = 75

Posterior Distributions

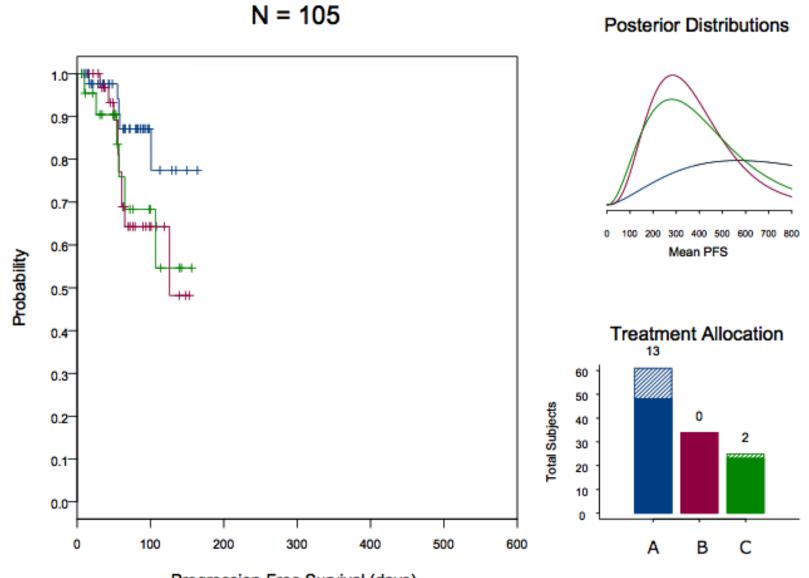
Progression-Free Survival (days)

Accrual Rate

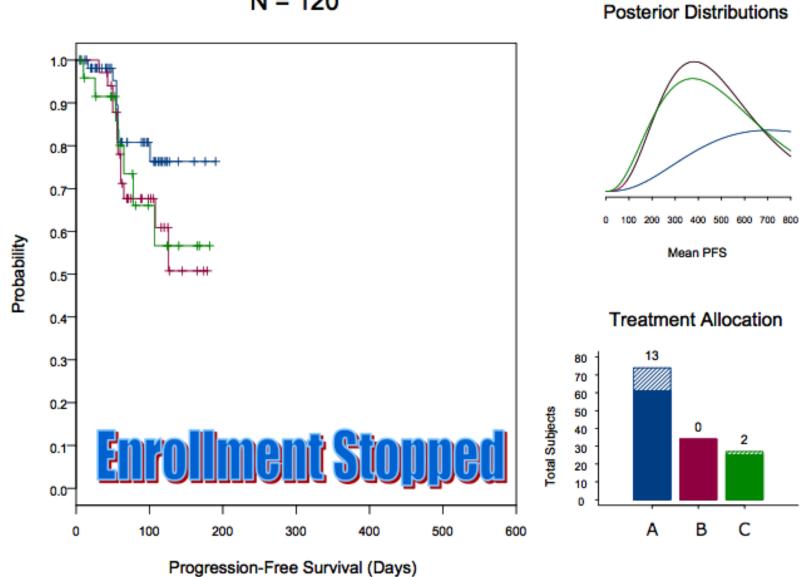




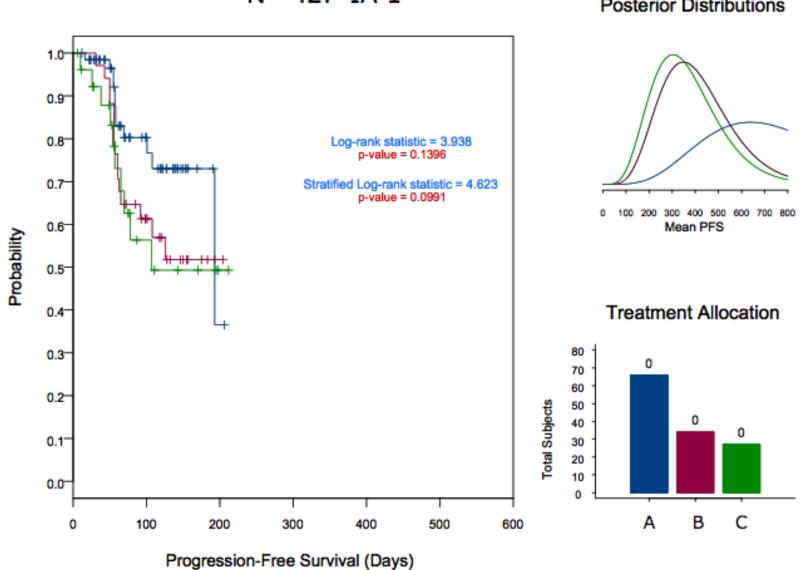
N = 90

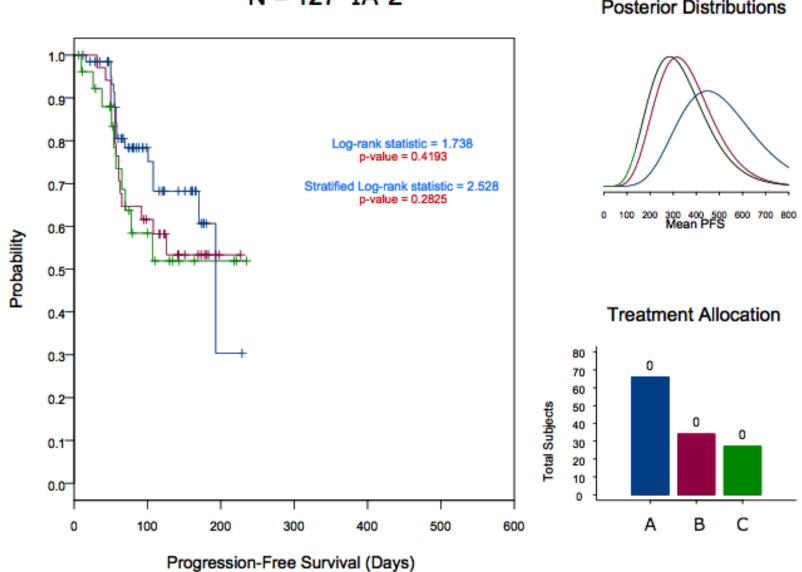


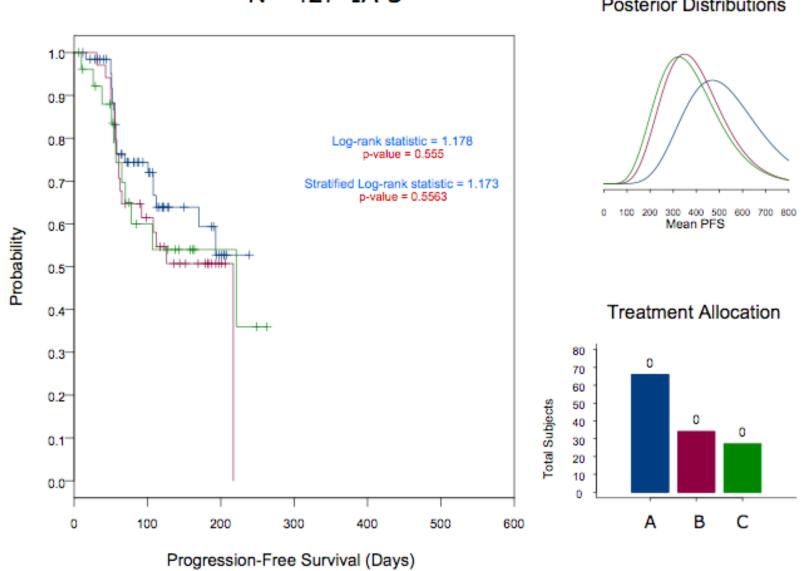
Progression-Free Survival (days)

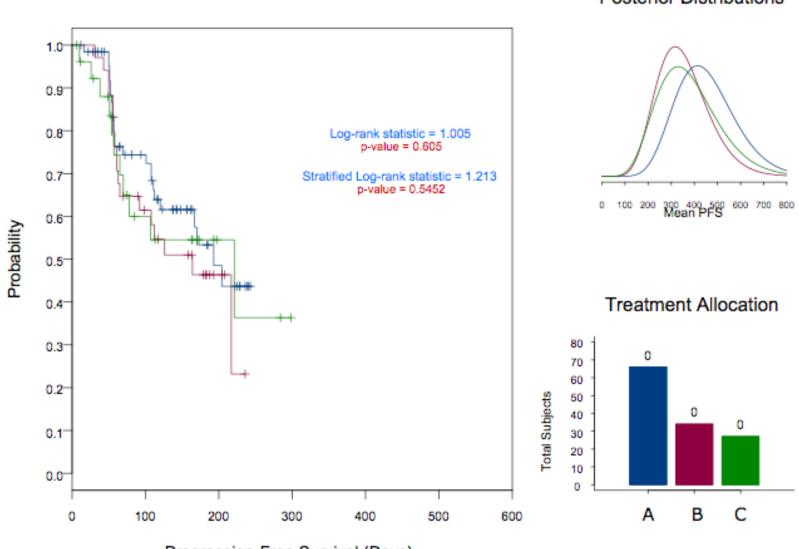


N = 120



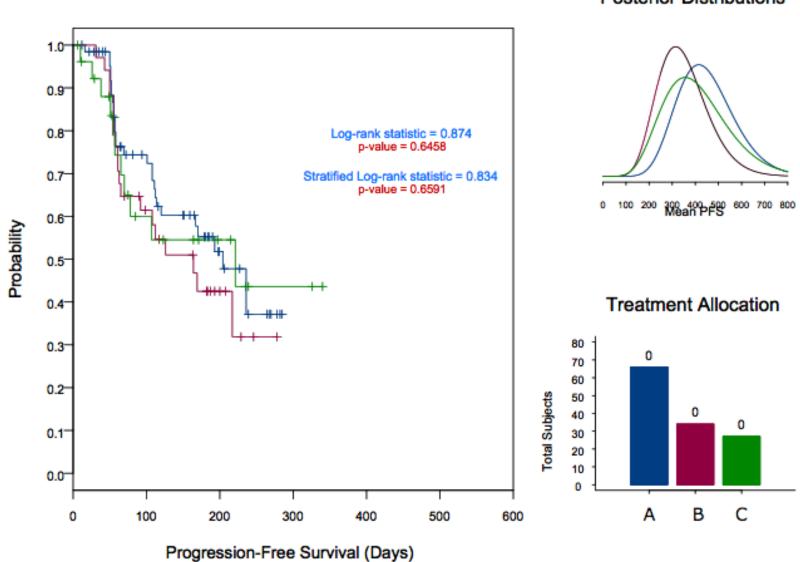






Progression-Free Survival (Days)

N = 127 IA 4

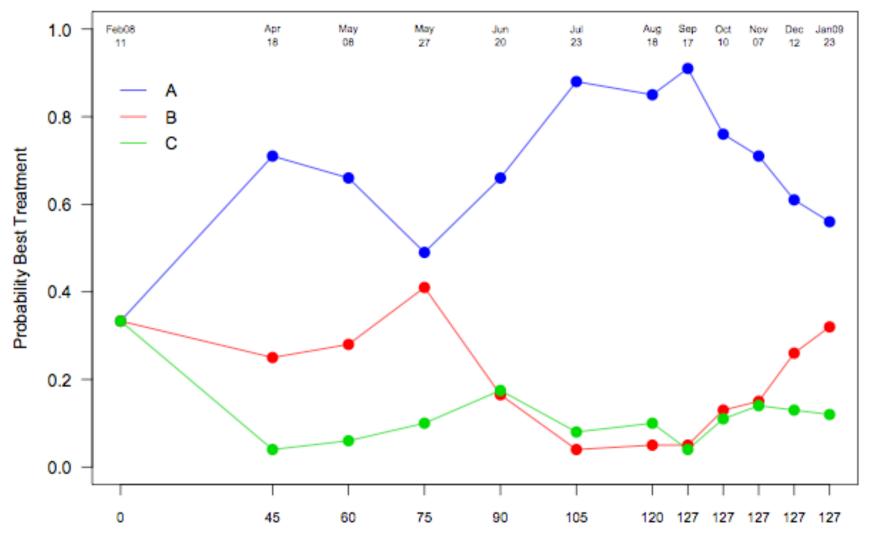


Lessons Learned $R_{j} = \frac{p_{j}^{c}}{p_{1}^{c} + p_{2}^{c} + p_{3}^{c} + \dots + p_{G}^{c}}$

 R_j : randomization probability of treatment *j* p_j : posterior probability treatment *j* is the best treatment.

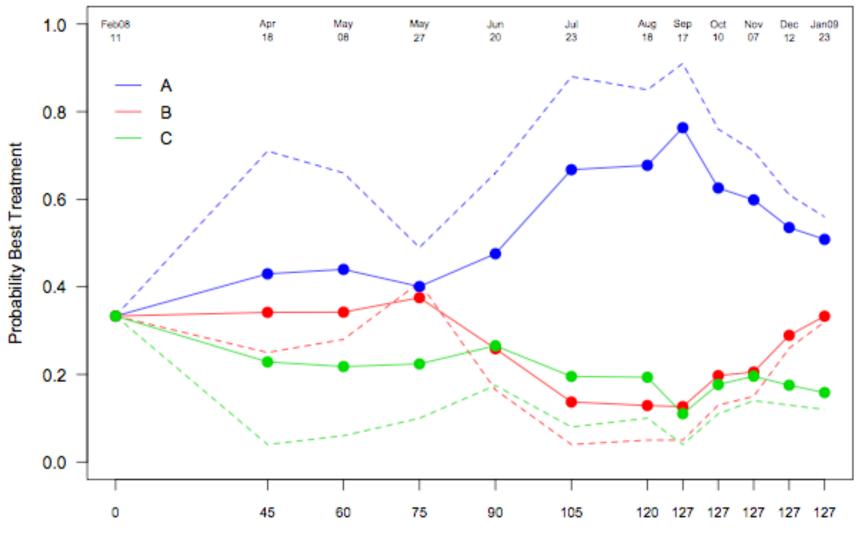
- c = 0, equal randomization ($R_j = 1/G$)
- c = 1, proportional randomization $(R_j = p_j)$
- $c \ge 1$
 - more likely to favor 1 arm earlier in the trial, even when treatments are equal
 - more subjects likely assigned to the best treatment
- c < 1
 - randomization less likely to favor one arm earlier in the trial
 - fewer subjects likely assigned to best treatment
- c = n/N, trial begins with c = 0 and ends with c = 1

Randomization Assignments



Sample Size, n

Randomization using c = n/N



Sample Size, n

Summary

Example: A Prospective Bayesian Adaptive Trial with Hierarchical Borrowing from a Prior Single Arm Study

With Kristine Broglio

EXCITE Trial Background

- Patients with peripheral artery disease and instent restenosis
- Randomized trial of
 - Control: Balloon angioplasty
 - Treatment: Laser ablation
- Primary Efficacy: Freedom from target lesion revascularization at 6 months
- Primary Safety: Freedom from major adverse events at 30 days

Original Study Design

- Sponsor seeks 510(k) approval
- Maximum of 318 subjects
- Hypotheses:
 - Efficacy superiority (2.5% Type I error)
 - Safety noninferiority 10% margin (5% Type I error)
- OBF interim analysis at 33% information

Adjunct Analysis

- Randomized trial had slow enrollment
- PATENT: A single arm trial of the laser ablation in Europe completed
- Sponsor asks: can we use the single arm trial to supplement the randomized trial?

PATENT Trial

- One arm trial
- Efficacy
 - 80 evaluable patients
 - 79% success rate (63/80)
- Safety
 - 90 evaluable patients
 - 4.4% event rate (4/90)

Hierarchical Borrowing

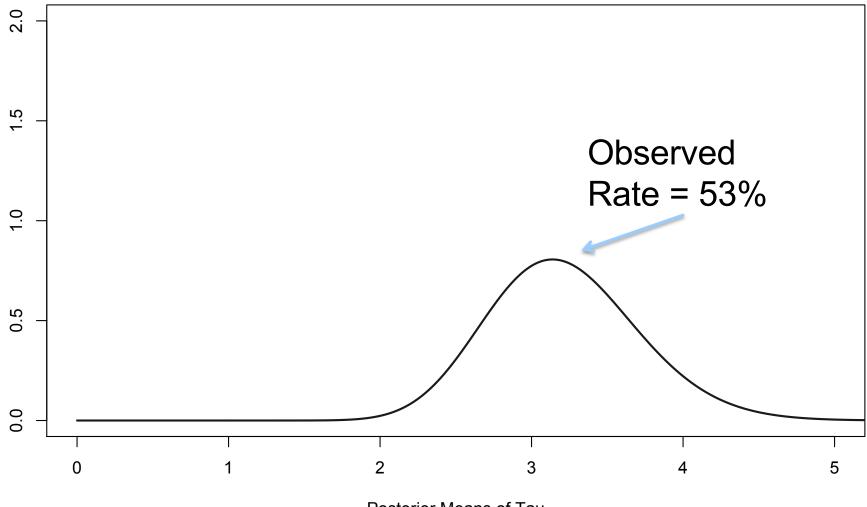
- Define *p*₀ as the proportion successes in EXCITE and *p*₁ as the proportion successes in PATENT
- Model the log-odds of success

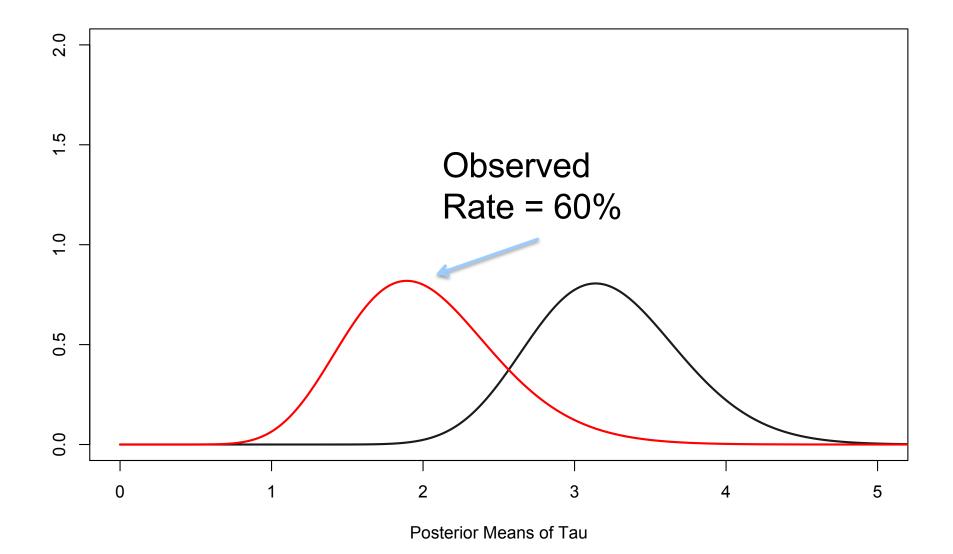
$$\gamma_i = \log\left(\frac{p_i}{1 - p_i}\right) i = 0,1$$

- Assume $\gamma_i \sim N(\mu, \tau^2)$
- Place hyperpriors on μ and τ^2

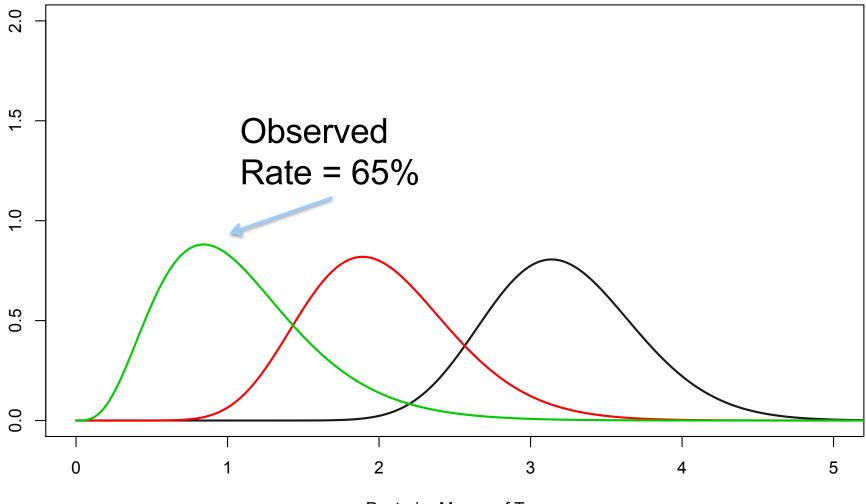
Hierarchical Borrowing

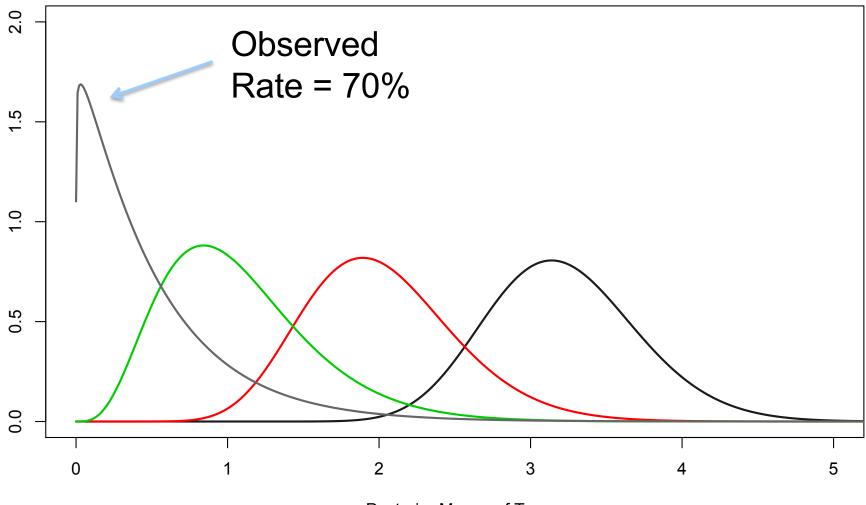
- τ^2 is between study variability
 - $-\tau^2 = 0$ corresponds to $\gamma_0 = \gamma_1$ or simple pooling
 - $-\tau^2 =$ gigantic corresponds to no borrowing
 - τ^2 estimated based on the observed data
 - Estimating τ^2 with 2 studies is hard & means the prior is always informative
 - Allows for a dynamic amount of borrowing
 - $\tau^2 \sim IG(0.025, 0.0000025).$
 - Today I'd use $\tau^2 \sim U(0,5)$ or $\tau^2 \sim U(0,20)$

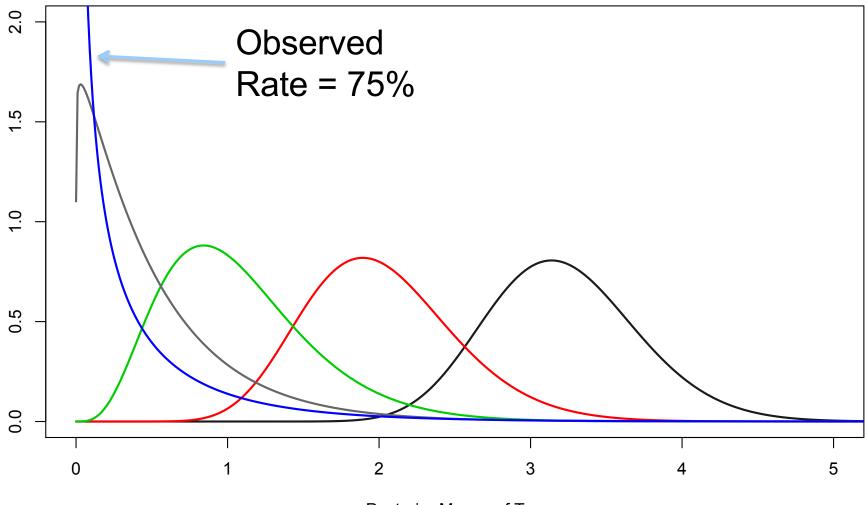


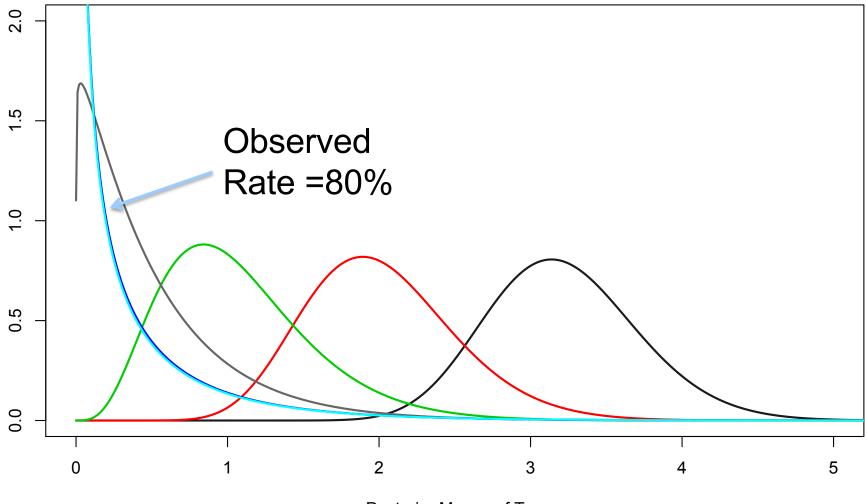


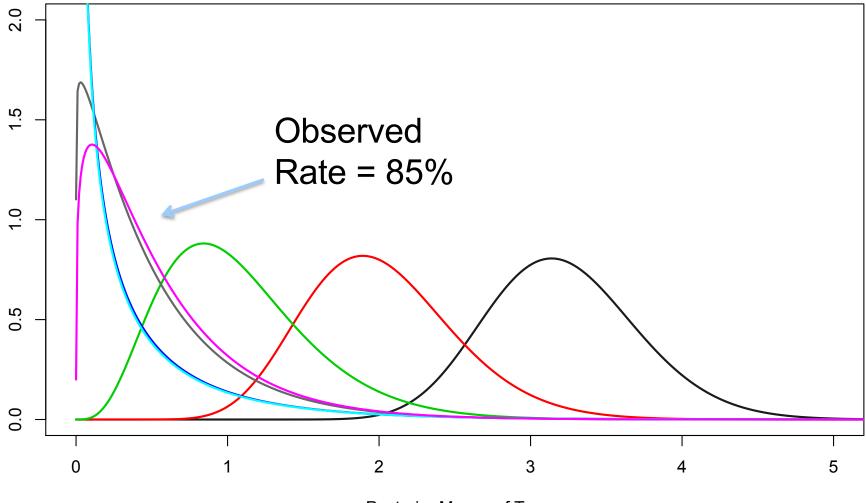
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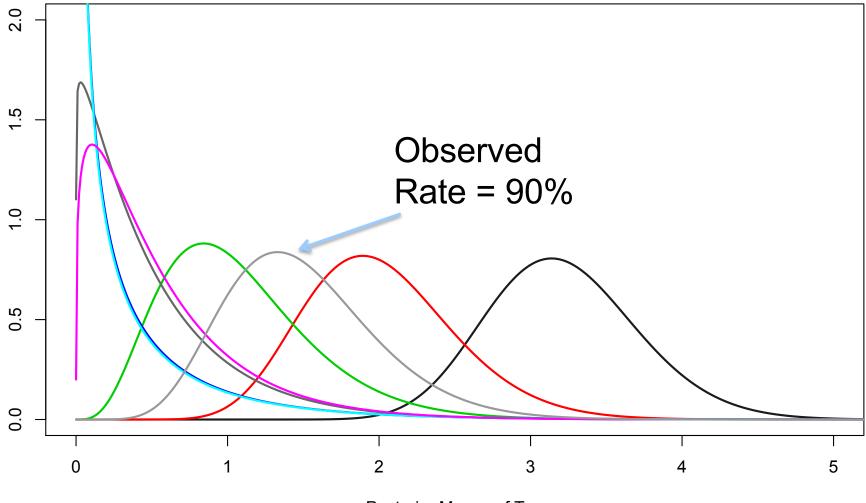




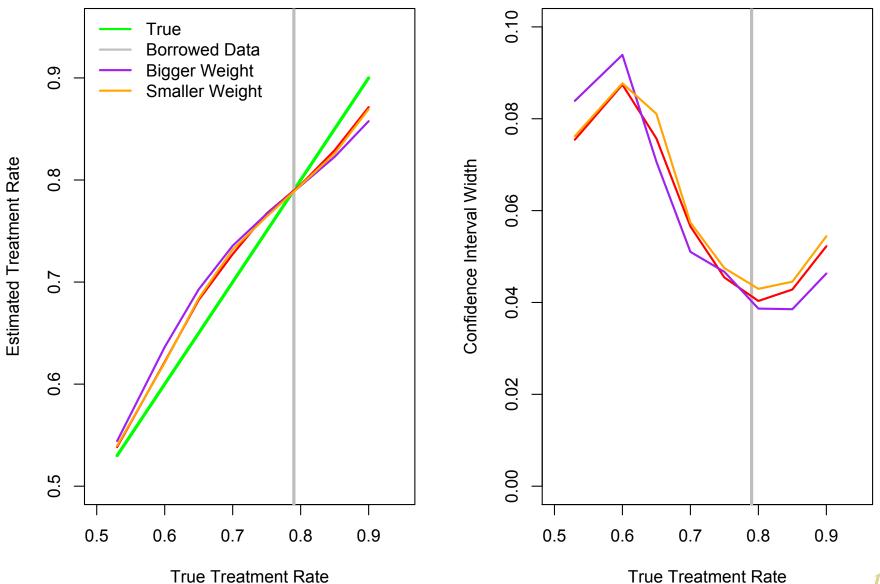








Estimation



120

Adjunct Analysis Plan

- Simulations explored
 - Timing of adjunct analyses
 - Amount of borrowing (Weaker \rightarrow Stronger)
 - Thresholds for claiming success at each look
 - Accrual rates
- Simulations showed control of overall onesided Type I error < 5% (both endpoints)

Adjunct Analysis Plan

• Adjunct analyses based on the number of patients <u>enrolled</u>

			Critical Values for Success	
Analysis	Expected Completers: Laser	Expected Completers: Balloon	Probability of Superiority for Efficacy	Probability of Non- Inferiority for Safety
200 Patients	89	44	0.998	0.998
250 Patients	119	58	0.9975	0.9975
300 Patients	149	74	0.995	0.995
Final Analysis	190	95	0.979	0.979

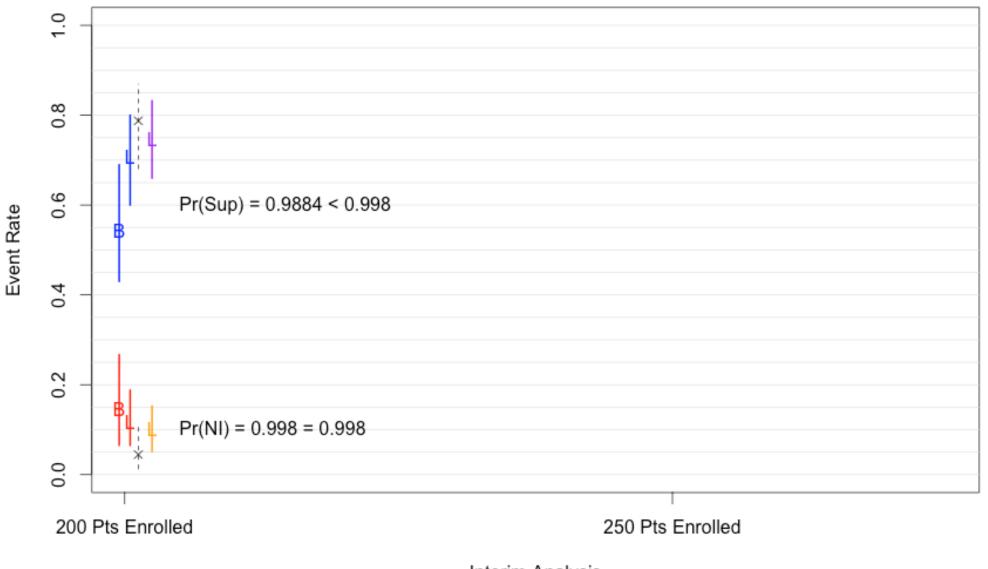
ACTUAL TRIAL EXECUTION



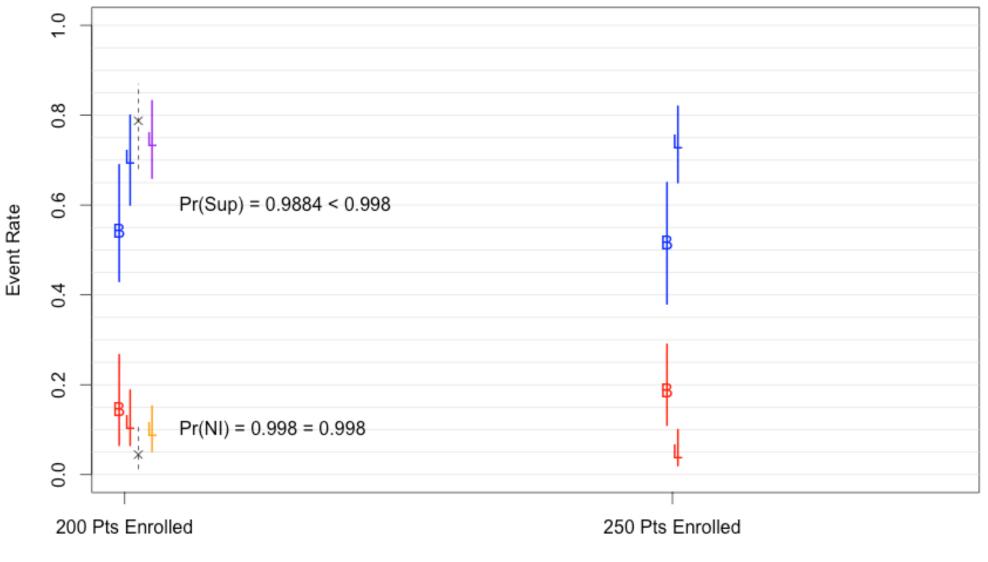
Interim Analysis



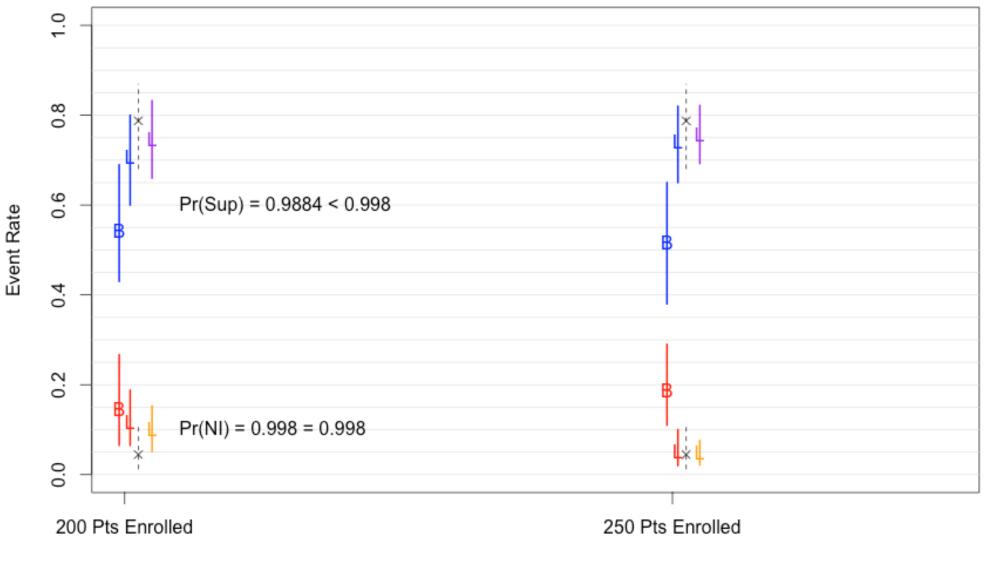




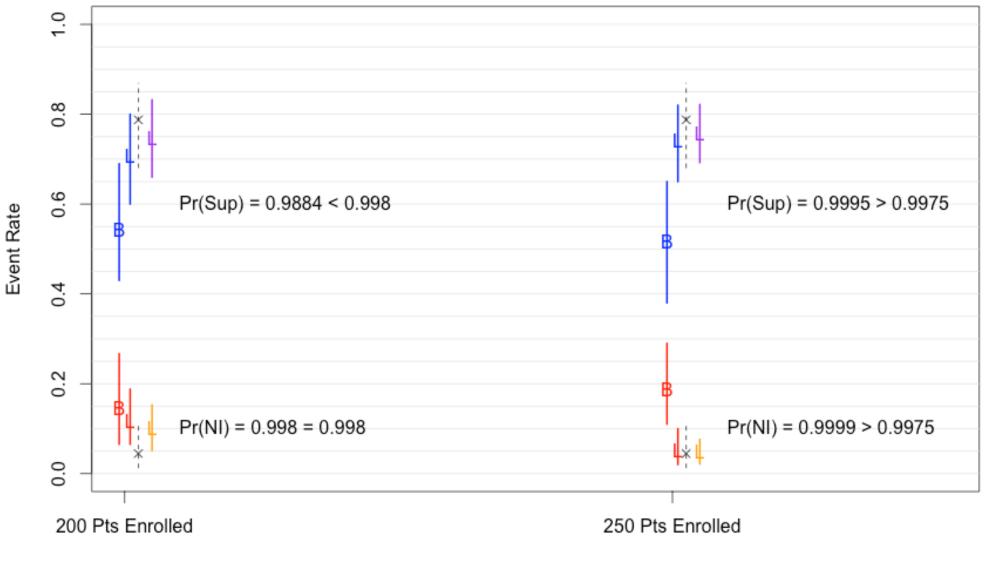
Interim Analysis













Compare to the O'Brien Fleming

Interim Analysis	% Information	Nominal P-Value	Observed P-Value
200 Pts	44%	0.0011	0.1005
250 Pts	60%	0.0043	0.006
300 Pts	78%	0.0105	
Final	100%	0.0208	

Conclusions

- Study met the adjunct analysis success criteria in Feb 2014
- 510K approval given in July 2014
- Randomized data showed a benefit in terms of efficacy and safety
- Borrowing from prior data increased precision
- Borrowing via prospectively defined rule
- Borrowing dependent on similarity of new trial with previous trial
- Allowed stopping earlier than an OBF bound

Platform Trials

& Master Protocols

Woodcock & Lavange, NEJM 2017

- High-quality evidence is what we use to guide medical practice. The standard approach to generating this evidence — a series of clinical trials, each investigating one or two interventions in a single disease — has become ever more expensive and challenging to execute. As a result, important clinical questions go unanswered.
- A methodologic innovation responsive to this need involves coordinated efforts to evaluate more than one or two treatments in more than one patient type or disease within the same overall trial structure. Such efforts are referred to as master protocols, defined as one overarching protocol designed to answer multiple questions.

Woodcock & Lavange, NEJM 2017

• Master protocols may involve one or more interventions in multiple diseases or a single disease, as defined by current disease classification, with multiple interventions, each targeting a particular biomarkerdefined population or disease subtype. Included under this broad definition of a master protocol are three distinct entities: umbrella, basket, and platform trials (Table 1 and Figs. 1 and 2). All constitute a collection of trials or substudies that share key design components and operational aspects to achieve better coordination than can be achieved in single trials designed and conducted independently.

Master Protocols

- May or may not compare treatment across groups
 - One structure, but each TX vs. common control
 - Reported as multiple trials (e.g. 1 per intervention)Sites have one set of rules, execute like 1 trial
- Intensive pretrial discussion among sponsors
 - data use, publication rights, and the timing of regulatory submission
- Matchmaker

- Therapies to targeted subpopulations

Master Protocols

Table 1. Types of Master Protocols.				
Type of Trial	Objective			
Umbrella	To study multiple targeted therapies in the context of a single disease			
Basket	To study a single targeted therapy in the context of multiple diseases or disease subtypes			
Platform	To study multiple targeted therapies in the context of a single disease in a perpetual manner, with therapies allowed to enter or leave the platform on the basis of a decision algo- rithm			

Master Protocols

Areas of Innovation

Infrastructure

Common screening platform for biomarker identification Governance

Steering committee Adjudication committee Data monitoring committee Central institutional review board Trial networks and clinical centers Processes Randomization Data and safety capture and management Quality-control oversight

Trial Design

Adaptive randomization and other adaptive design features Longitudinal modeling to determine probabilities of success or failure

Shared control patients

Natural-history cohort Biomarker qualification

Figure 3. Areas of Innovation in Master Protocols.

- Master protocols come in different sizes and shapes but share many commonalities.
- Increased planning efforts and coordination to satisfy the objectives of different stakeholders.
- Maximum information is obtained from the research effort
- Infrastructure required for implementation increases data quality and trial efficiencies, as compared with those in stand-alone trials.
- Can last many years, even decades, with innovations from the laboratory translating quickly to clinical evaluation.

Platform Trials

Asking the Right Question

Current Clinical Trials

Is this drug effective and safe?

More precisely

What is the probability of the observed data assuming the treatment is no good?

Asking the Right Question

- Current Clinical Trials
 - Is this drug effective and safe compared to a placebo?
 - Is this drug effective & safe compared to the SOC
- Correction Question
 - What is the best treatment for this Patient?
 - What is the best treatment for this type of patient?

Traditional Trial Design

- Single treatment vs. Control
- Homogenous patient population
- 1 or 2 questions per 1 trial
- Start with assuming a particular control group effect and a particular (usually optimistic) treatment group effect
- Assume 'average' effect relevant to all patients
- Calculate a sample size as if we know the true effect

Platform Trial

- An experimental infrastructure to evaluate multiple treatments, often for a group of diseases, and intended to function continually and be productive beyond the evaluation of any individual treatment
 - Designed around a group of related diseases rather than a single treatment
 - Disease focused not treatment focused
 - Dynamic list of available treatments, assigned with responseadaptive randomization
 - Preferred treatments may depend on health system, patient, or disease-level characteristics

VIEWPOINT

The Platform Trial An Efficient Strategy for Evaluating Multiple Treatments

Scott M. Berry, PhD Berry Consultants LLC, Austin, Texas; and Department of

Biostatistics, University of Kansas Medical Center, Kansas City.

Jason T. Connor, PhD Berry Consultants LLC, Austin, Texas; and University of Central Florida College of Medicine, Orlando.

Roger J. Lewis, MD, PhD

Department of Emergency Medicine, Harbor-UCLA Medical Center, Torrance, California; and Berry Consultants LLC, Austin, Texas. The drug development enterprise is struggling. The development of new therapies is limited by high costs, slow progress, and a high failure rate, even in the late stages of development. Clinical trials are most commonly based on a "one population, one drug, one disease" strategy, in which the clinical trial infrastructure is created to test a single treatment in a homogeneous population.

This approach has been largely unsuccessful for multiple diseases, including sepsis, dementia, and stroke. Despite promising preclinical and early human trials, there have been numerous negative phase 3 trials of treatments for Alzheimer disease¹ and more than 40 negative phase 3 trials of neuroprotectants for stroke.² Effective treatments for such diseases will likely require combining treatments to affect multiple targets in complex cellular pathways and, perhaps, tailoring treatments to subgroups defined by genetic, proteomic, metabolomic, or other markers.³

There has been increasing interest in efficient trial strategies designed to evaluate multiple treatments and combinations of treatments in beterogeneous patient benefits when evaluating potentially synergistic combination treatments (eg, treatment A, treatment B, treatment C, and all combinations) if the starting point is the testing of each treatment in isolation.

What Is a Platform Trial?

A platform trial is defined by the broad goal of finding the best treatment for a disease by simultaneously investigating multiple treatments, using specialized statistical tools for allocating patients and analyzing results. The focus is on the disease rather than any particular experimental therapy. A platform trial is often intended to continue beyond the evaluation of the initial treatments and to investigate treatment combinations, to quantify differences in treatment effects in subgroups, and to treat patients as effectively as possible within the trial. Although some of the statistical tools used in platform trials are frequently used in other settings and some less so, it is the integrated application of multiple tools that allows a platform trial to address its multiple goals. The **Table** summarizes the general differences between a traditional clinical trial and a platform trial



From: The Platform Trial: An Efficient Strategy for Evaluating Multiple Treatments

JAMA. Published online March 23, 2015. doi:10.1001/jama.2015.2316

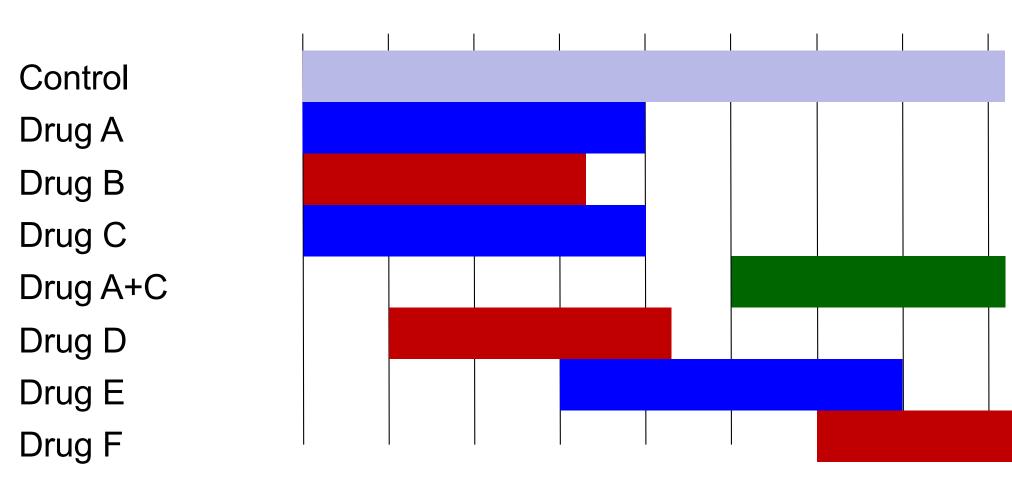
Table. General Characteristics of Traditional and Platform Trials^a

Characteristic	Traditional Trial	Platform Trial
Scope	Efficacy of a single agent in a homogeneous population	Evaluating efficacy of multiple agents in a heterogeneous population; explicitly assumes treatment effects may be heterogeneous
Duration	Finite, based on time required to answer the single primary question	Potentially long-term, as long as there are suitable treatments requiring evaluation
No. of treatment groups	Prespecified and generally limited	Multiple treatment groups; the number of treatment groups and the specific treatments may change over time
Stopping rules	The entire trial may be stopped early for success or futility or harm, based on the apparent efficacy of the single experimental treatment	Individual treatment groups may be removed from the trial, based on demonstrated efficacy or futility or harm, but the trial continues, perhaps with the addition of new experimental treatment(s)
Allocation strategy	Fixed randomization	Response-adaptive randomization
Sponsor support	Supported by a single federal or industrial sponsor	The trial infrastructure may be supported by multiple federal or industrial sponsors or a combination

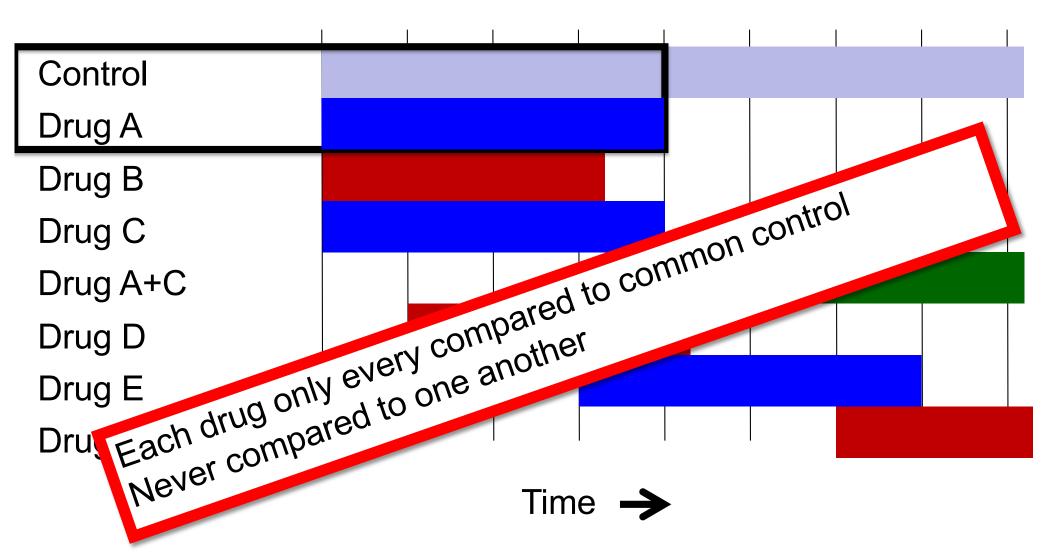
^a Platform trials and similar trials may also be called basket, bucket, umbrella, or standing trials.

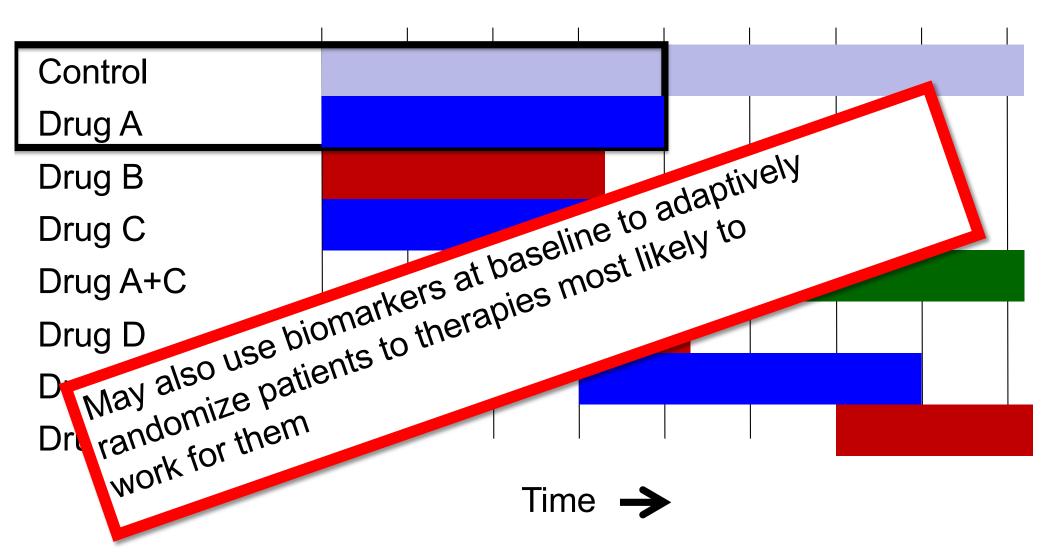
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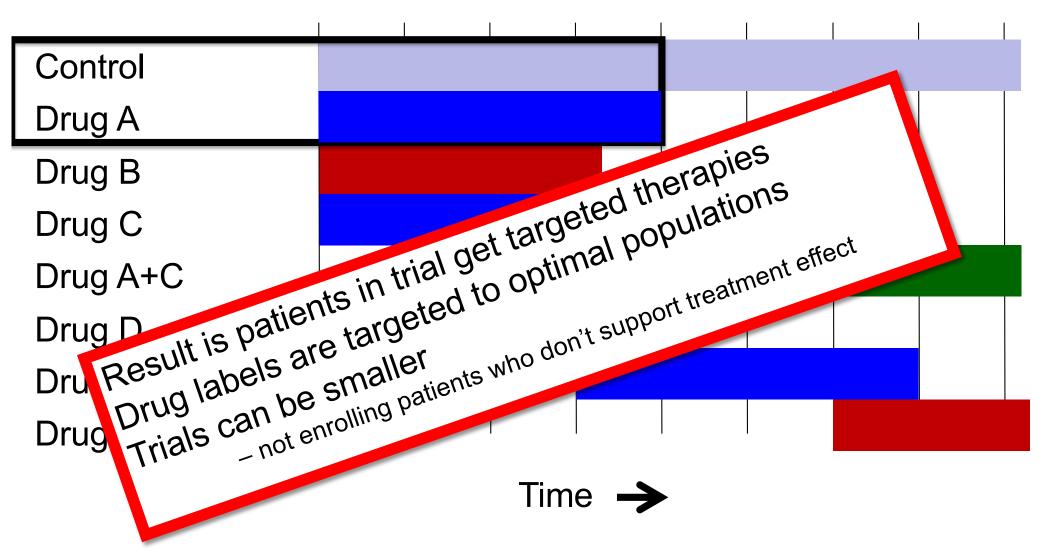
General Characteristics of Traditional and Platform Trials^a

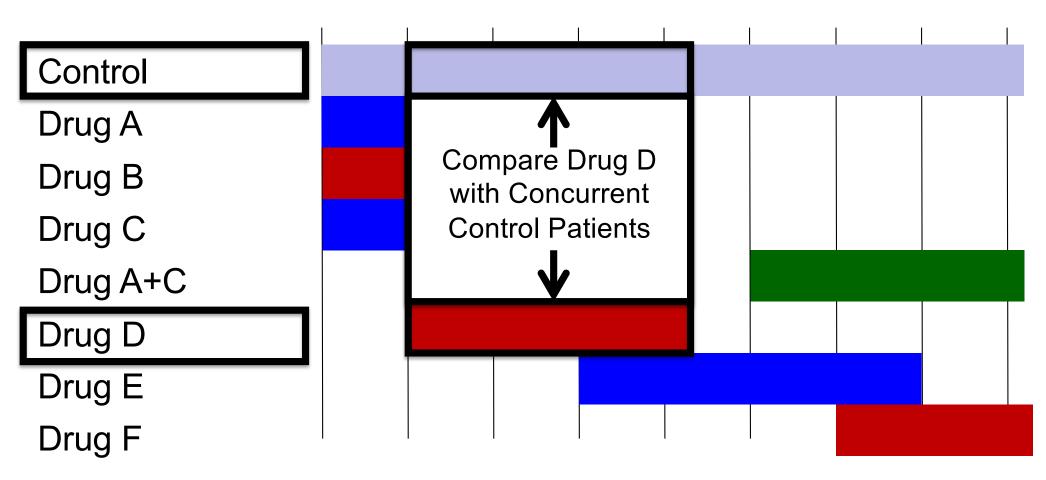








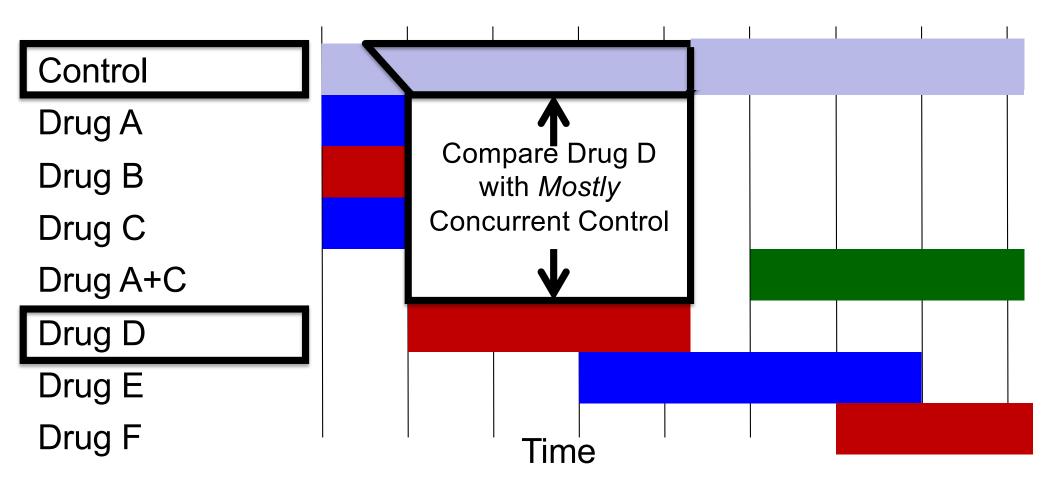






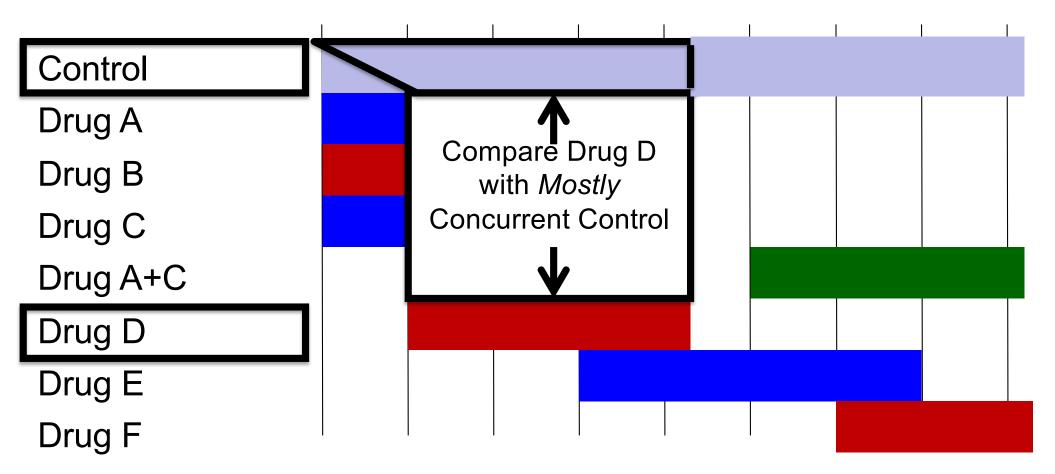
Time Machine

Model how controls change over time, if similar, then use some controls outside concurrent window



Time Machine

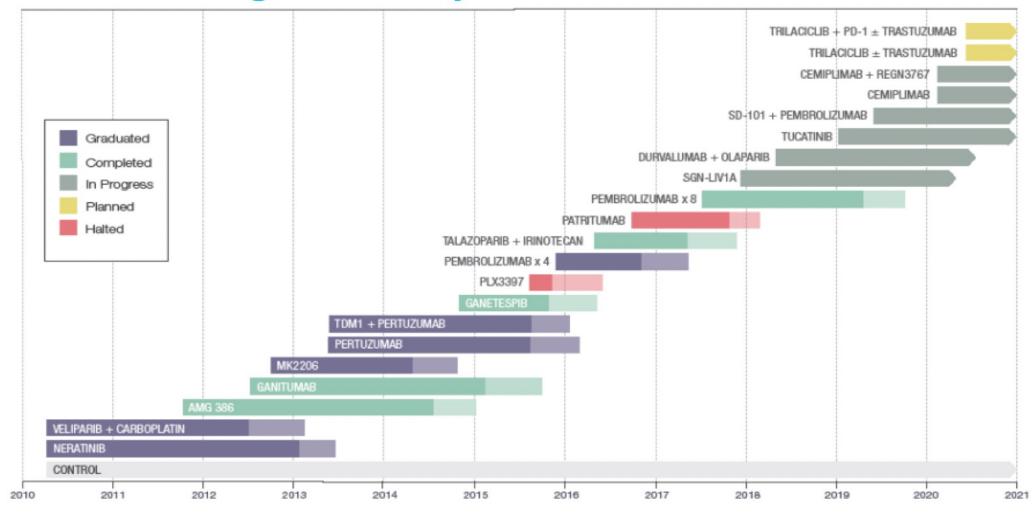
If controls change little over time, then use more weight from non-concurrent controls, increases power & efficiency



I-SPY2

ULLEU

I-SPY 2 Agent History



Used with permission from Dr. Laura Esserman, I-SPY2 PI

Platform Trials are Happening

- Cancer
 - I-SPY2 in Breast Cancer
 - GBM AGILE in Glioblastoma multiforme
 - LUNG-MAP in Lung Cancer
 - PANCAN in Pancreatic Cancer
- Alzheimer's
 - EPAD: European Prevention of Alzheimer's Dementia
 - DIAN: Dominantly Inherited Alzheimer's Network
- ALS
 - Healey ALS Platform Trial, Phase 2/3 with 5 drugs

Platform Trials are Happening

- Infection diseases
 - Gates Foundation sponsored Ebola design
 - NIH Ebola design
 - PREPARE: European Consortium for Disease Preparedness
 - Pandemic flu, Butler at al Lancet, Jan 2020
 - REMAP CAP (Community Acquired Pneumonia) ongoing, REMAPCAP.org
- COVID-19
 - RECOVERY
 - ACTT by NIAID -- the Remdesivir trial
 - SOLIDARITY by WHO, 4 arms
 - REMAP-COVID by International consortium critical care trial
 - PRINCIPLE in UK, pre-hospital trial
 - ISPY-COVID: UCSF & WISDOM Network, Phase 2
 - ACTIV by NIH

Characteristics of Modern Platform Trials	Cancer Trials						r's	
	I-SPY 2	MICAT	BATTLE	LUNG-MAP	UK MATRIX	GBM-AGILE	Alzheimer's	Ebola
Screen markers for all pts	~	~	~	~	~	~		
Master protocol	~	~	~	~	~	<	~	/
Many regimens	~	~	~	~	~	~	~	<
Combination therapies	~	~	~			~	~	<
Sequential therapies		~				~		
Assembly line	~	~			~	~	~	/
Learn off-target effects	~	~	~			~		
Pair regimens/biomarkers	~	~	~			~		
Common control arm	~	~				~	~	/
Adaptive randomization	~	~	~			~	~	/
Adaptive sample size	~	~				~	~	/
Early "curable" disease	~					~	~	/
Registration endpoint	~					~	~	/
Seamless phases						~		
Longitudinal modeling	~	~				~	~	
Bayesian	~	~	~			•	~	•

From Don Berry

Efficiencies of platform clinical trials: A vision of the future

Benjamin R Saville^{1,2} and Scott M Berry^{1,3}

Abstract

Background: A "platform trial" is a clinical trial with a single master protocol in which multiple treatments are evaluated simultaneously. Adaptive platform designs offer flexible features such as dropping treatments for futility, declaring one or more treatments superior, or adding new treatments to be tested during the course of a trial.

Methods: A simulation study explores the efficiencies of various platform trial designs relative to a traditional two-arm strategy.

Results: Platform trials can find beneficial treatments with fewer patients, fewer patient failures, less time, and with greater probability of success than a traditional two-arm strategy.

Conclusion: In an era of personalized medicine, platform trials provide the innovation needed to efficiently evaluate modern treatments.

Keywords

Platform trial, master protocol, multi-arm, adaptive, Bayesian, clinical trial design

CLINICAL TRIALS

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A response adaptive randomization platform trial for efficient evaluation of Ebola virus treatments: A model for pandemic response

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Abstract

The outbreak of Ebola virus disease in West Africa is the largest ever recorded. Numerous treatment alternatives for Ebola have been considered, including widely available repurposed drugs, but initiation of enrollment into clinical trials has been limited. The proposed trial is an adaptive platform design. Multiple agents and combinations will be investigated simultaneously. Additionally, new agents may enter the trial as they become available, and failing agents may be removed. In order to accommodate the many possible agents and combinations, a critical feature of this design is the use of response adaptive randomization to assign treatment regimens. As the trial progresses, the randomization ratio evolves to favor the arms that are performing better, making the design also suitable for all-cause pandemic preparedness planning. The study was approved by US and Sierra Leone ethics committees, and reviewed by the US Food and Drug Administration. Additionally, data management, drug supply lines, and local sites were prepared. However, in response to the declining epidemic seen in February 2015, the trial was not initiated. Sierra Leone remains ready to rapidly activate the protocol as an emergency response trial in the event of a resurgence of Ebola. (ClinicalTrials.gov Identifier: NCT02380625.) In summary, we have designed a single controlled trial capable of efficiently identifying highly effective or failing regimens among a rapidly evolving list of proposed therapeutic alternatives for Ebola virus disease and to treat the patients within the trial effectively based on accruing data. Provision of these regimens, if found safe and effective, would have a major impact on future epidemics by providing effective treatment options.

EBOLA

Thanks to: Scott Berry, Elizabeth Petzold, Chris Woods, David Hoover







The Problem: Ebola Treatment Trial

- Acknowledge universe of possible treatments
 - Will evolve over time
 - Recognition that combinations may play an important role
- Uncertainty over role of standard of care
- Our Goal: To determine best treatment for treating ebola
 - Not a trial to determine if a single drug X works

EV-003 Adaptive Platform Design

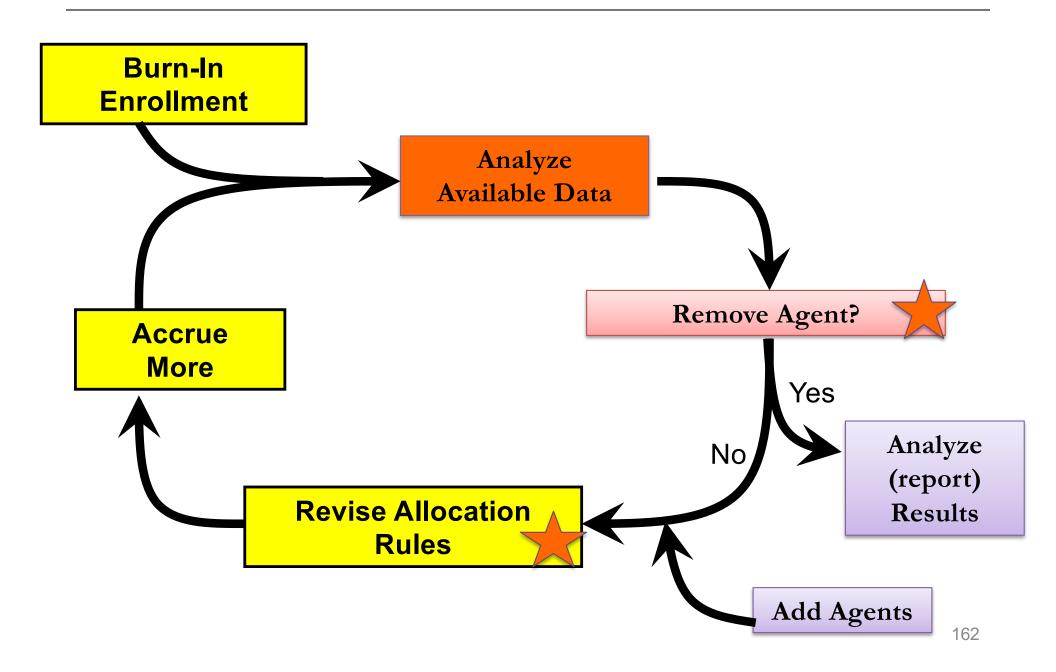
- Reviewed and approved by:
 - Duke University IRB
 - University of Sierra Leone ethics committee
- Master Protocol dictates trial behavior, each treatment included as an appendix
- Multiple Agents
 - Primary & Secondary agents
 - Combination + Single agents
- Response Adaptive Randomization (RAR)
 - Run by a single algorithm
 - Assigns treatment regimens that are performing better using collection of primary endpoint data
- Protocol is built so trial arms evolve (part of the protocol!), trial is **perpetual**
- Endpoint is 14-day mortality

Primary/Secondary Agents

- All arms receive optimized standard of care (SOC)
- Primary and Secondary agents
 - Primary: Expected capability to work as single agent (e.g. anti-viral efficacy)
 - Secondary: Expected to work with other agents (not given alone)

Regimens		Treatments							
		P1	P2	P3	P4	S1	S2		
Treatments	P1								
	P2								
	P3								
	P4								

Adaptive Platform Design



Design Details



- Endpoint: Death (Dichotomous, events are bad)
- Start with burn-in period to all 10 regimens
 - Equal randomization to 10 arms
 - 30 subjects / 3 per arm
- After burn-in
 - Response adaptive randomization
 - Proportional to probability regimen is optimal
 - Adjusted for information
 - Continue perpetually (committee can change vote)

Decision Criteria (In/Out)

Analyze (report) Results

- If there is a less than 0.01 probability an agent is part of the optimal regimen

 Candidate for futility
- If the probability an agent is in the optimal regimen is greater than 0.95
 - Report to the steering committee for public dissemination
- If a regimen has at least a 0.95 probability of being superior to SOC Alone then SOC Alone is reported for removal

Allocation Rules

- If a SOC it gets minimum of 20%...
- Randomize to regimens with probability proportional to:

$$r_{ij} \sim \frac{\Pr(\pi_{ij} = \max(\pi))}{n_{ij} + 1}$$

Statistical Model Analyze
Available Data
$$\log\left(\frac{p}{1-p}\right) = \alpha + \sum_{X=1}^{M} [X] + \sum_{X=1}^{M} \sum_{Y=X+1}^{M} [X,Y] + \lambda_{TIME}$$

• Priors:

$$[X] \sim N(0, 1^2) \qquad [X, Y] \sim N(0, 0.2^2)$$

Statistical ModelAnalyze
Available Data
$$log\left(\frac{p}{1-p}\right) = \alpha + \sum_{X=1}^{M} [X] + \sum_{X=1}^{M} \sum_{Y=X+1}^{M} [X,Y] + \lambda_{TIME}$$
Priors:

• Priors:

$$[X] \sim N(0, 1^2)$$
 $[X, Y] \sim N(0, 0.2^2)$

N(0,1) has 95% CI from about 1/7 to 7.

Statistical Model Analyze
Available Data
$$\log\left(\frac{p}{1-p}\right) = \alpha + \sum_{X=1}^{M} [X] + \sum_{X=1}^{M} \sum_{Y=X+1}^{M} [X,Y] + \lambda_{TIME}$$

• Priors:

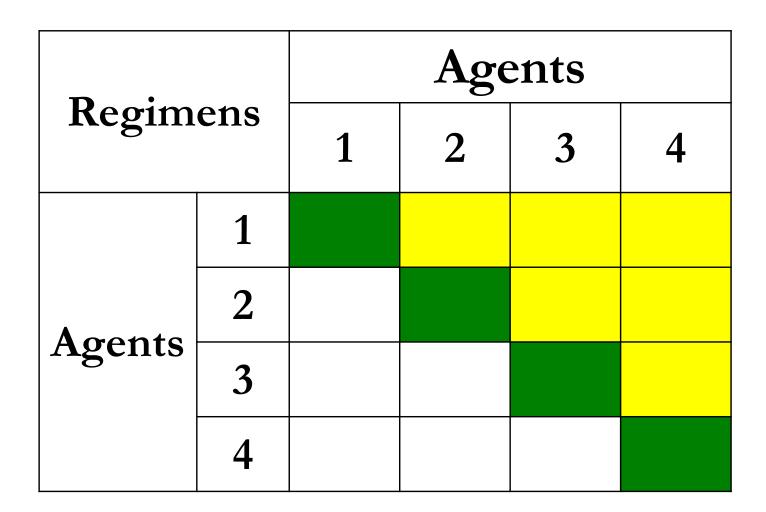
$$[X] \sim N(0, 1^2)$$

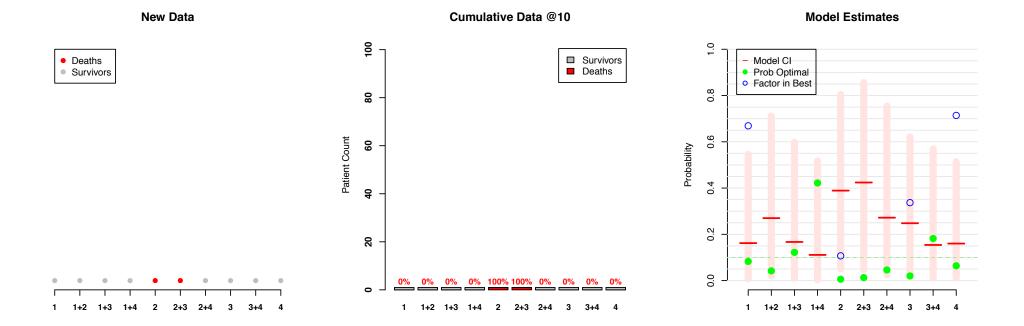
$$[X,Y] \sim N(0,0.2^2)$$

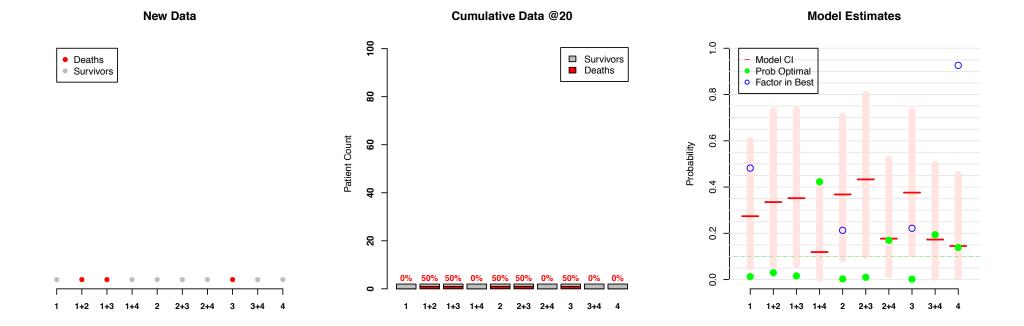
N(0,0.2²) has 95% CI from about 2/3 to 3/2.

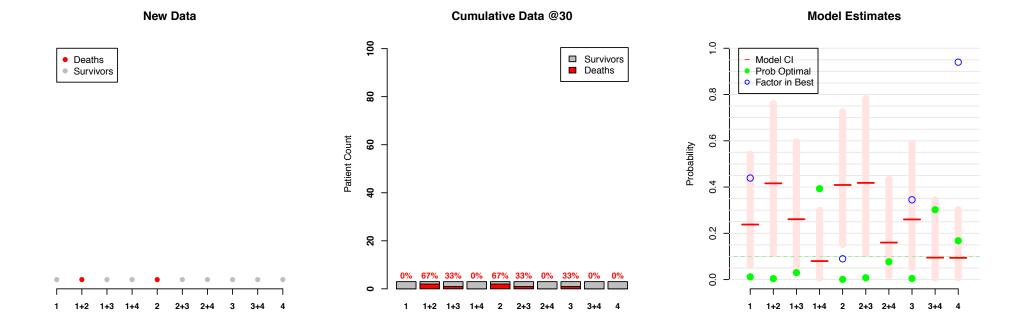
Statistical ModelAnalyze
Available Data
$$log\left(\frac{p}{1-p}\right) = \alpha + \sum_{X=1}^{M} [X] + \sum_{X=1}^{M} \sum_{Y=X+1}^{M} [X,Y] + \lambda_{TIME}$$
Priors:
 $[X] \sim N(0,1^2)$ $[X,Y] \sim N(0,0.2^2)$ Time:
 \cdot
 $lncorporate time "buckets" to model time trend or $drift'$
 $[\lambda] \sim NDLM(0,\tau^2)$$

Example Trial





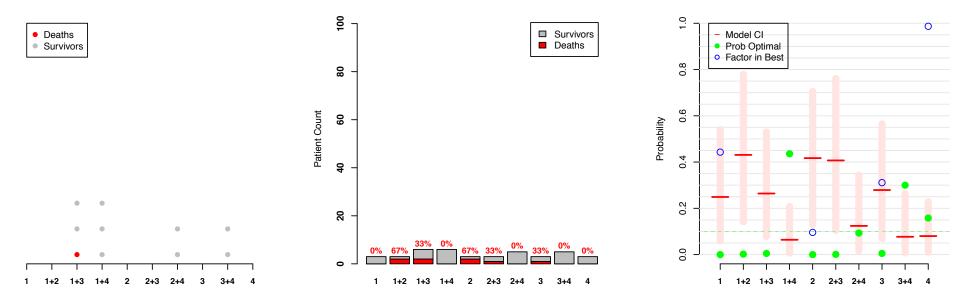






Cumulative Data @40

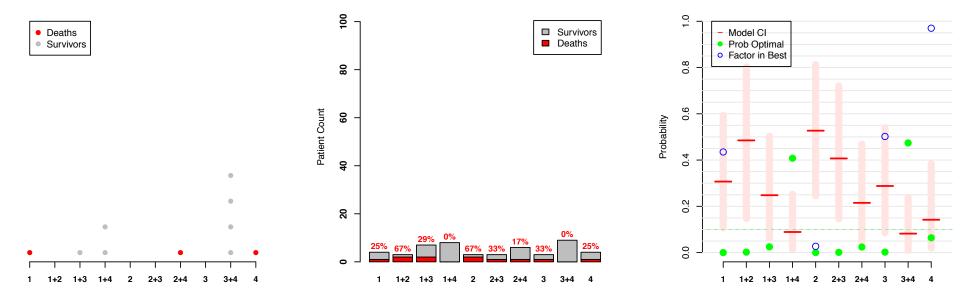
Model Estimates





Cumulative Data @50

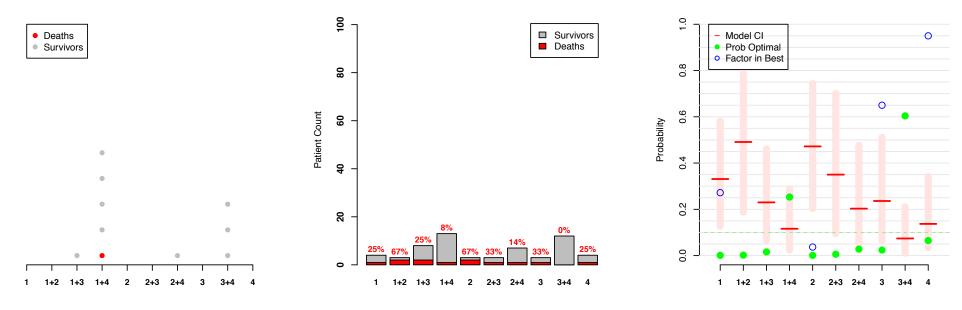
Model Estimates



New Data

Cumulative Data @60

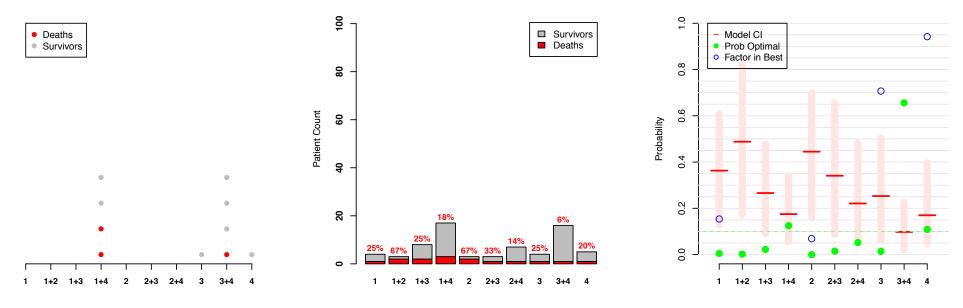
Model Estimates



New Data

Cumulative Data @70

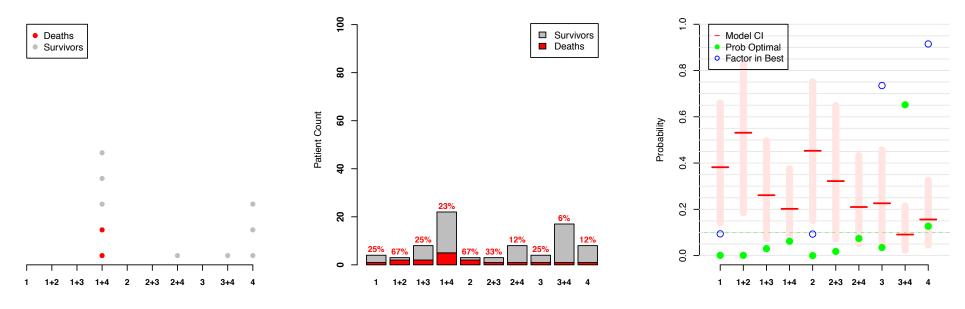
Model Estimates



New Data

Cumulative Data @80

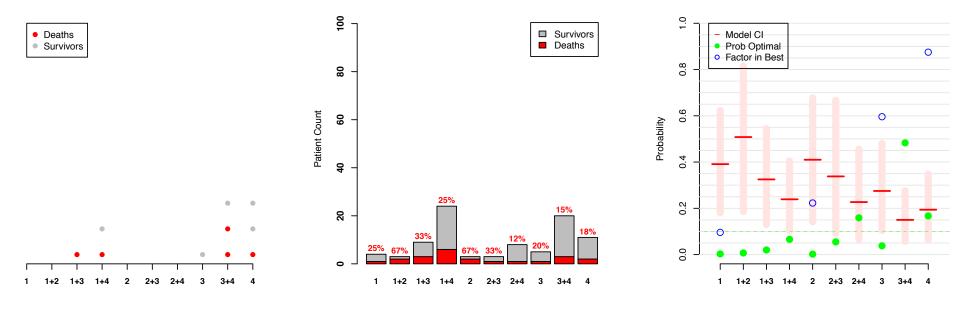
Model Estimates



New Data

Cumulative Data @90

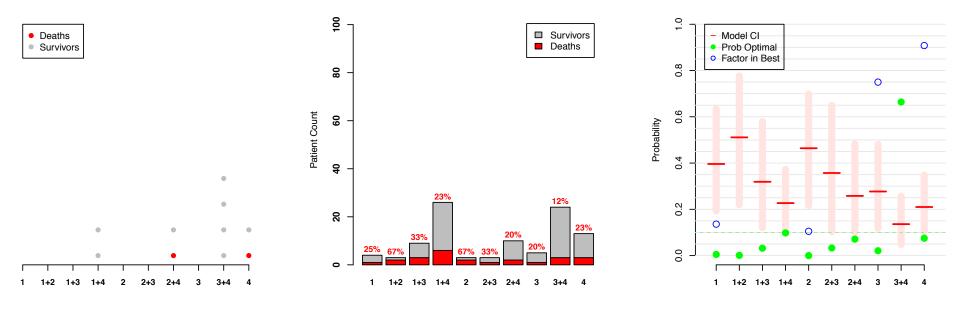
Model Estimates



New Data

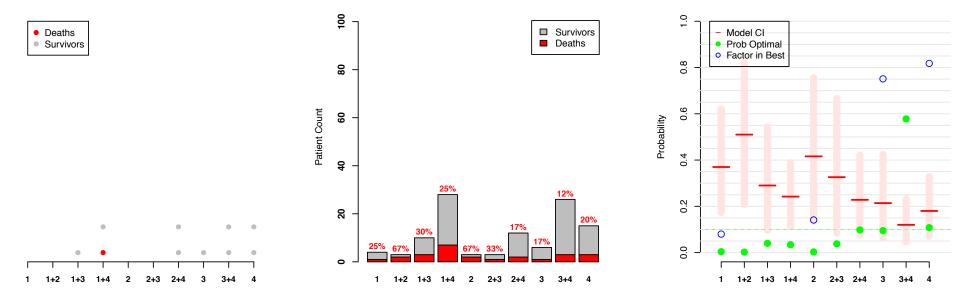
Cumulative Data @100

Model Estimates

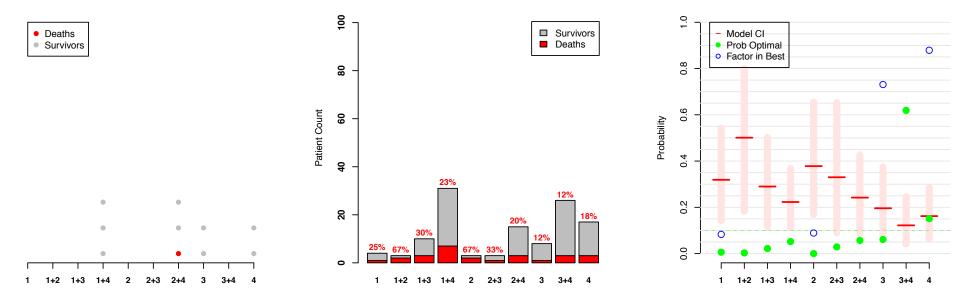


Cumulative Data @110

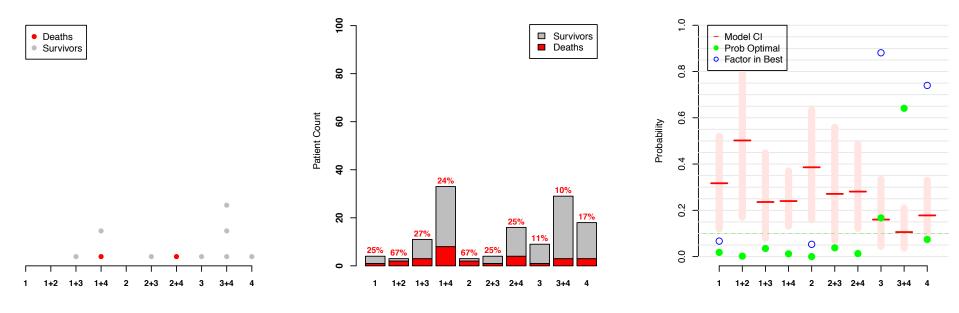
Model Estimates



Cumulative Data @120



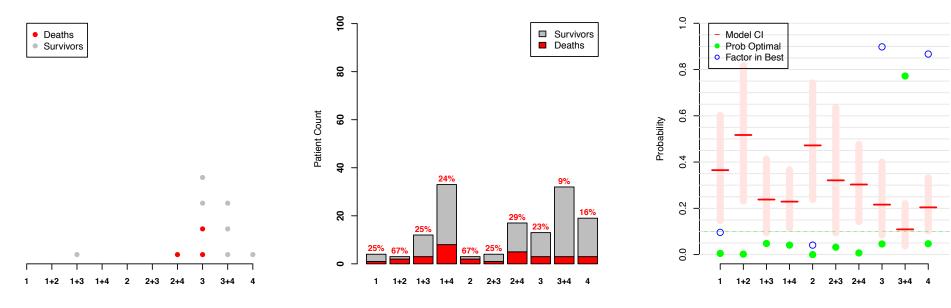
Cumulative Data @130



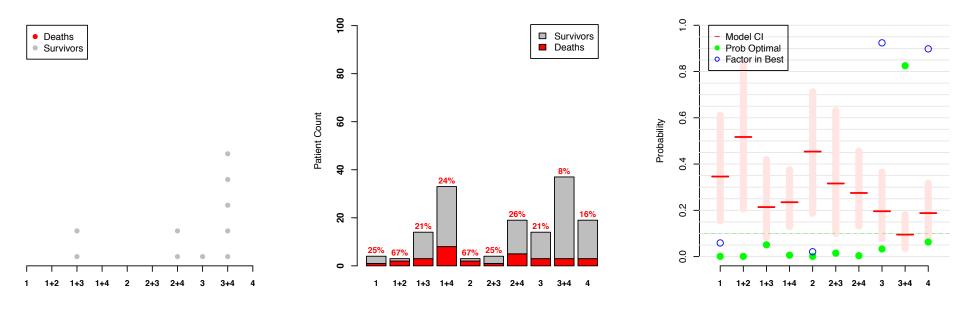
New Data

Cumulative Data @140

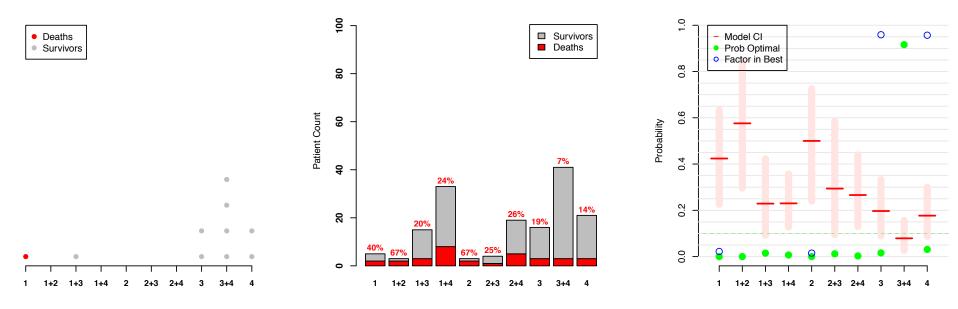
Model Estimates



Cumulative Data @150



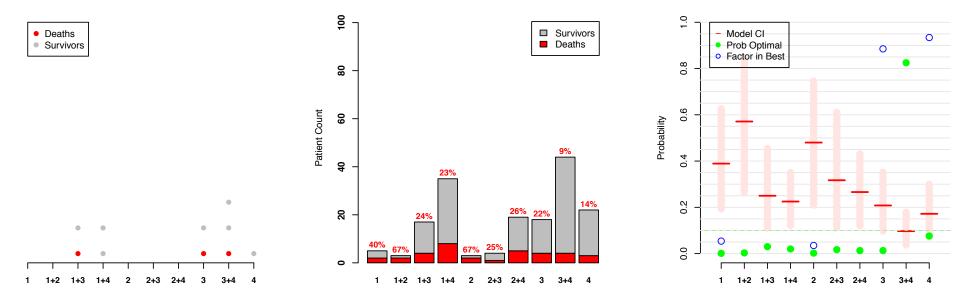
Cumulative Data @160



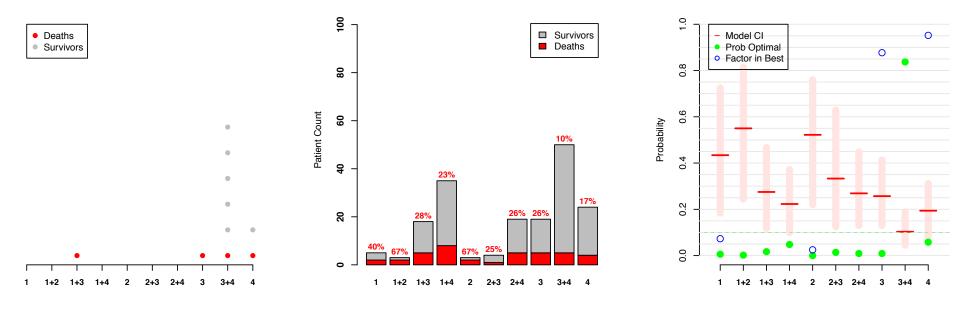
New Data

Cumulative Data @170

Model Estimates



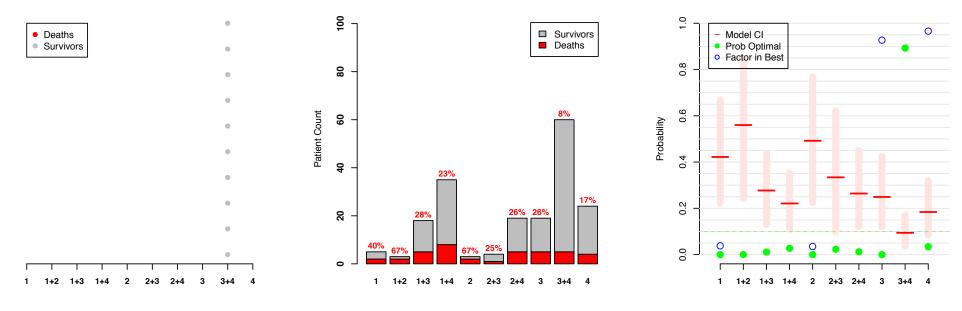
Cumulative Data @180



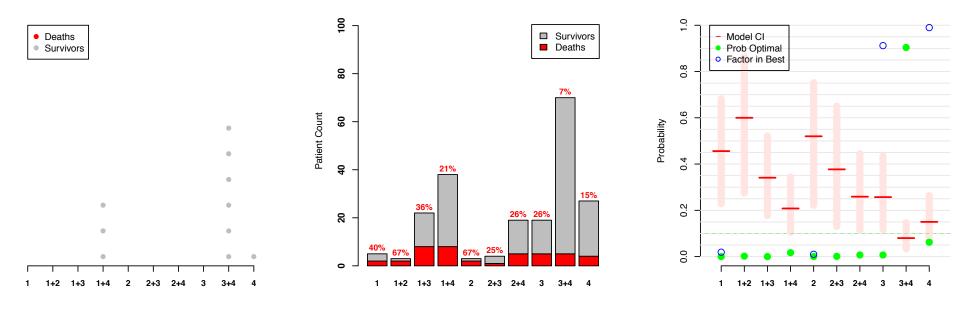
New Data

Cumulative Data @190

Model Estimates

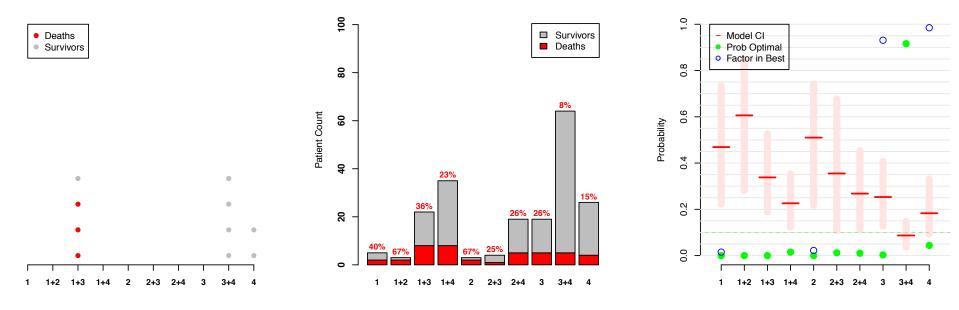


Cumulative Data @210

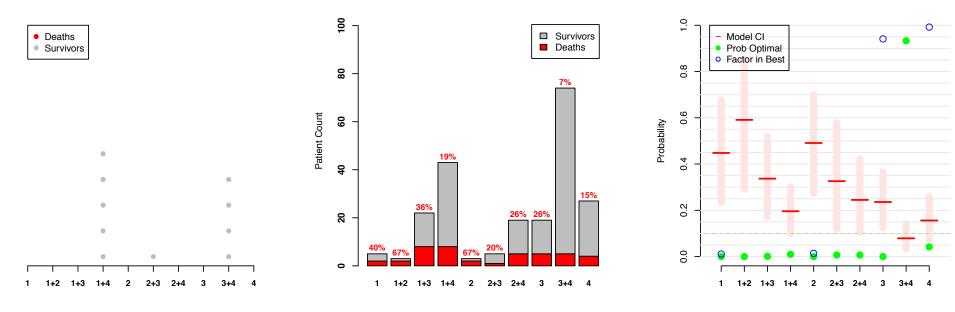


Cumulative Data @200

Model Estimates



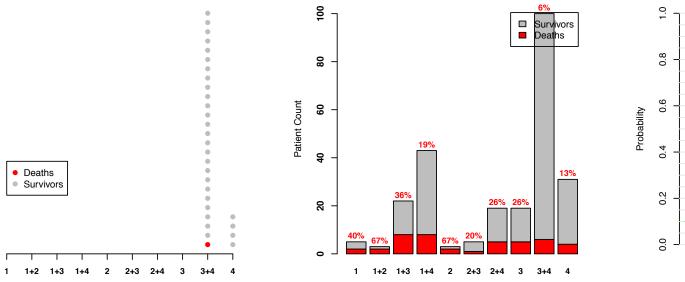
Cumulative Data @220

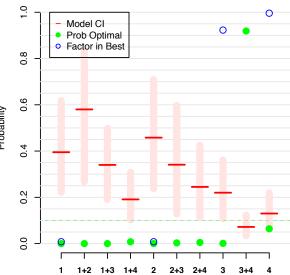


New Data

Cumulative Data @250

Model Estimates

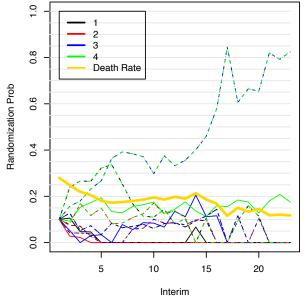


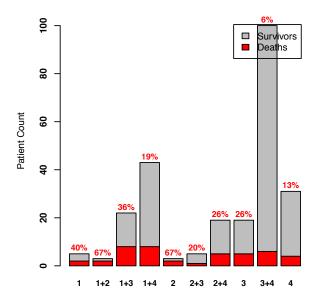


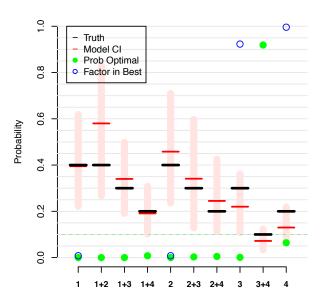
Randomization Time Course

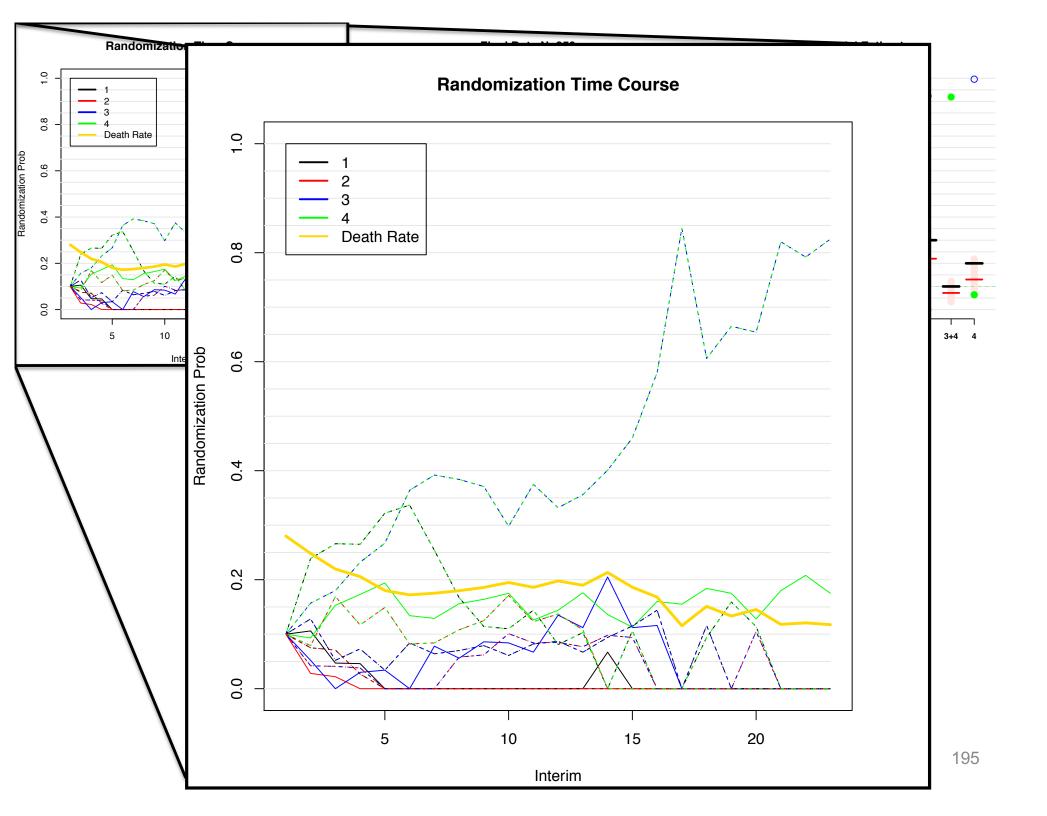
Final Data N=250

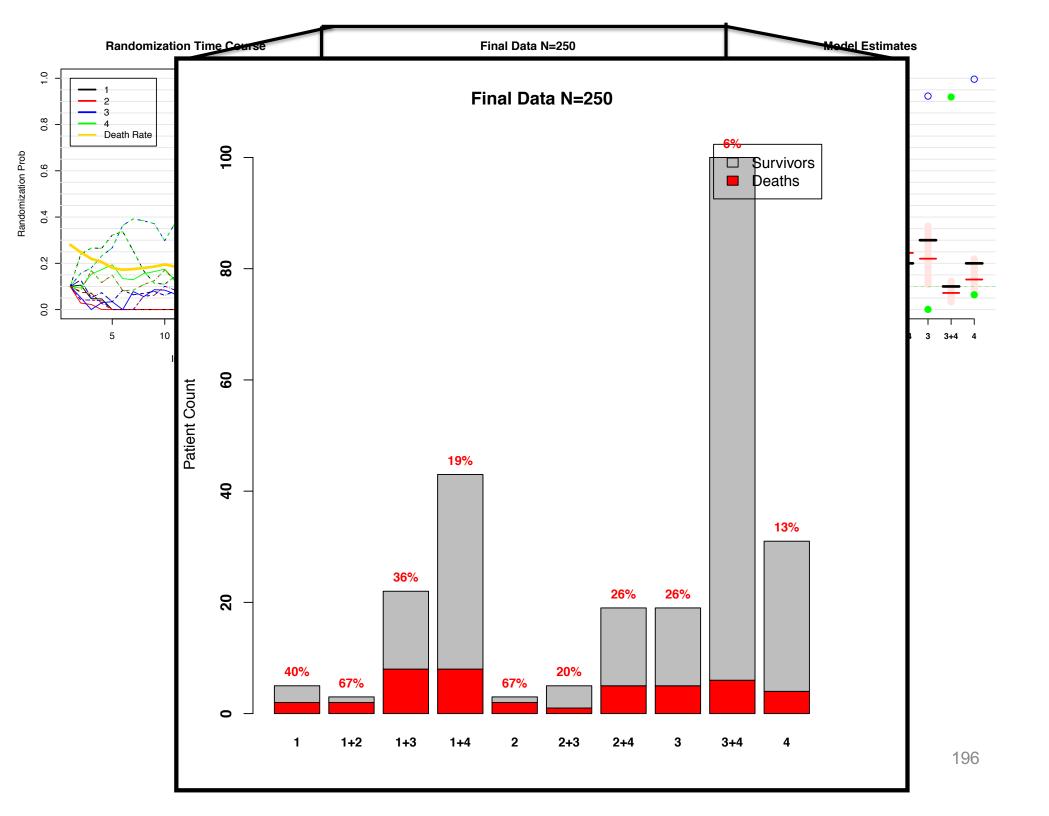
Model Estimates

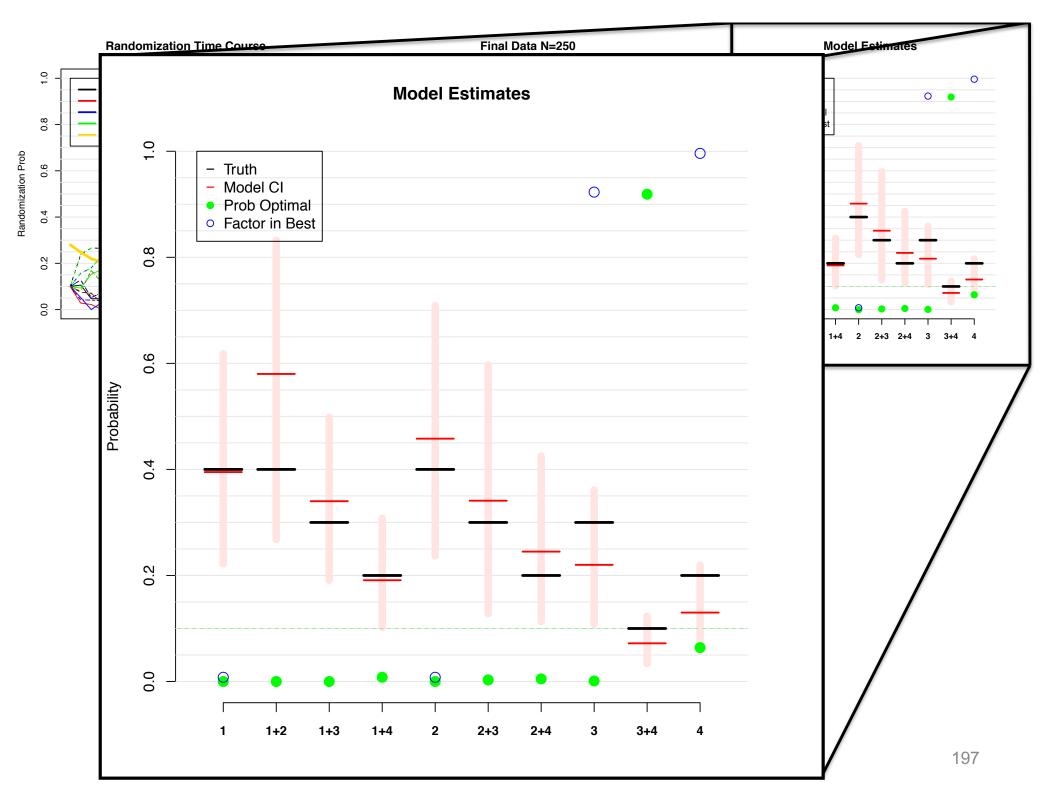


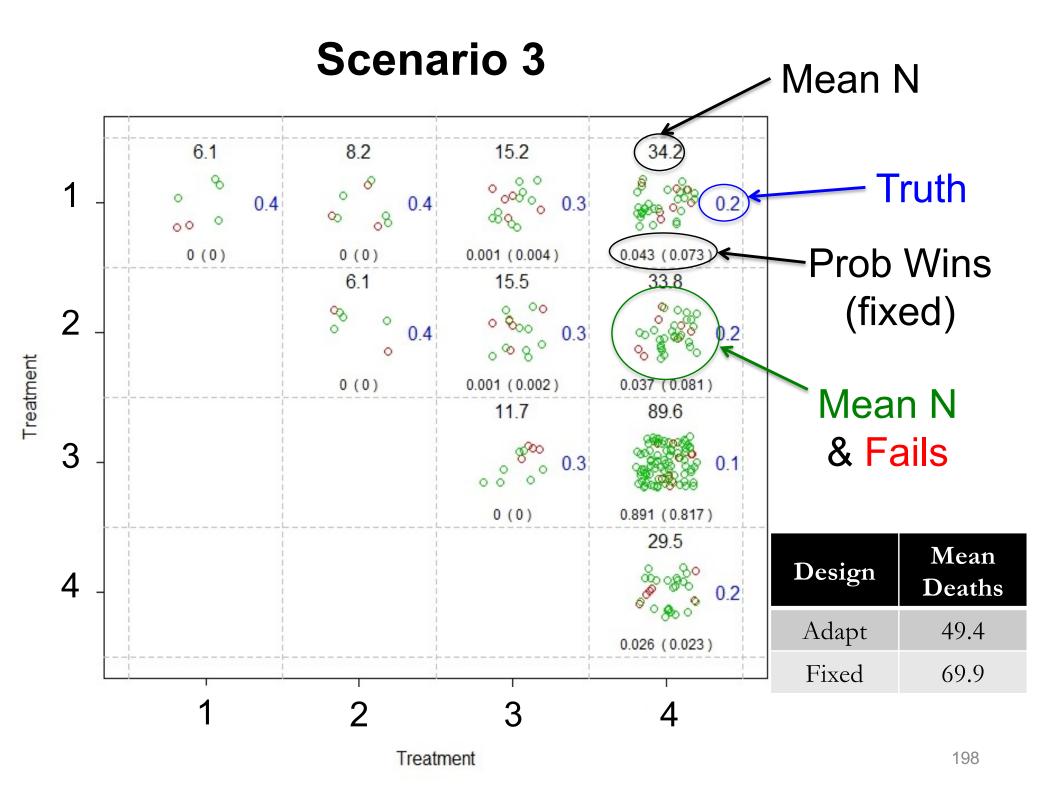


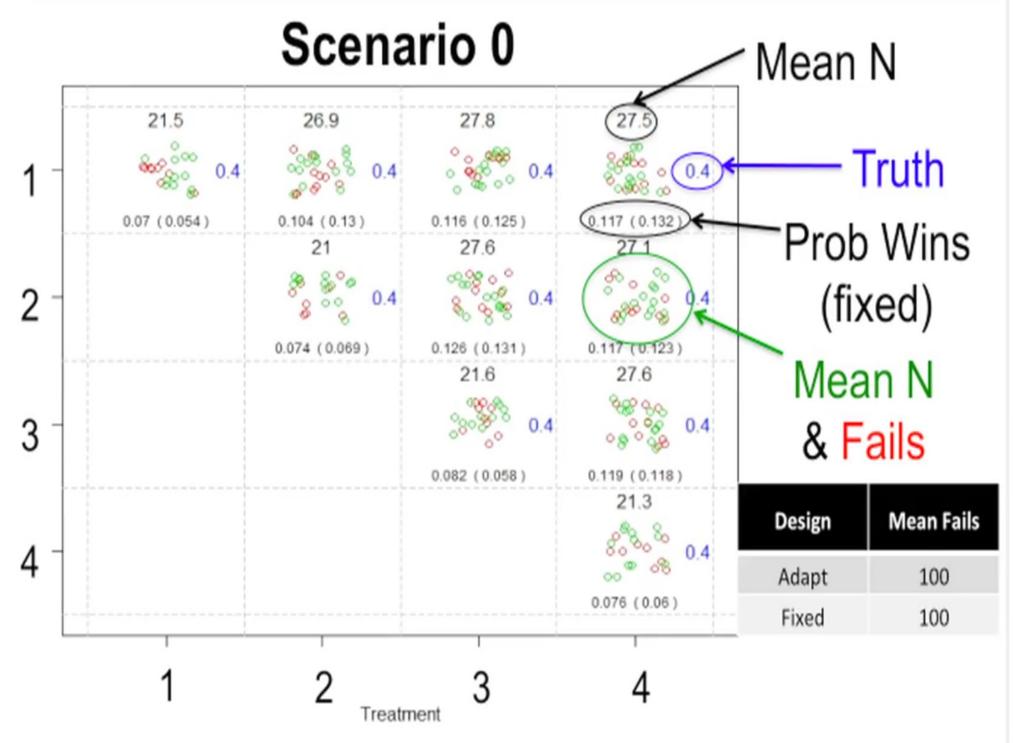




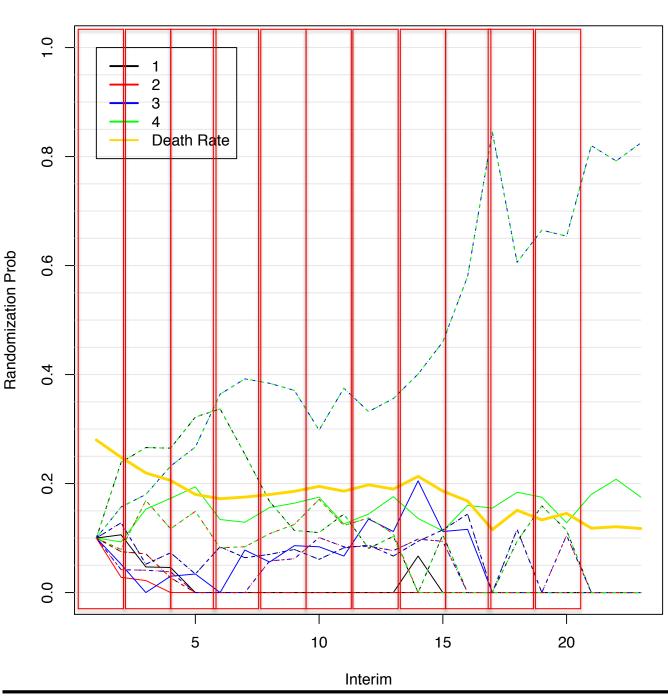








reatment



The model adjusts for time trends by modeling the patient drift within "buckets" or months.



Randomization Time Course

Summary

- Incredibly powerful design for finding effective therapies and combinations in the universe of treatments
 - Type III Error (the question never asked!)
- Allows the arms to evolve internally and externally to changing science
- Improved Embedded Care: Efficiently and quickly identifies best agents, *while treating patients more effectively*
- Have design ready—on the shelf for next pandemic
 - A number of parameters can be optimized quickly
 - Protocol ready (add appendices)
 - Models + simulations ready
- Need independent committee to decide which drugs to plug in

Platform Example 2

The Role of Biomarkers in Treatments & Trials

Testing a New Treatment

• Standard of Care works in 40%



10% of Patients Benefit

- Standard of Care works in 40%
- New therapy works in 50%



50% still untreatable



- Standard of Care works in 40%
- New therapy works in 50%
- Nothing works in 50%

50% still untreatable



- Standard of Care works in 40%
- New therapy works in 50%
- Nothing works in 50%

 How many patients do we need to have 90% chance to see a 'statistically significant' difference?

Need 1036 patients for 90% Power



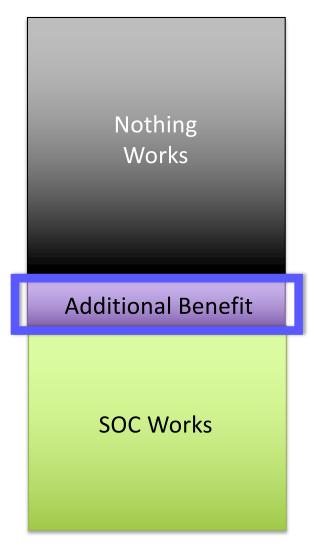
- Standard of Care works in 40%
- New therapy works in 50%
- Nothing works in 50%

Need 1036 patients for 90% Power



- Standard of Care works in 40%
- New therapy works in 50%
- Nothing works in 50%
- 90% of patients you enroll tell you nothing

Need 1036 patients for 90% Power



- Standard of Care works in 40%
- New therapy works in 50%
- Nothing works in 50%
- 90% of patients you enroll tell you nothing
- What if you knew which 10% of patients benefited?

What if you KNEW which 10% Benefit

	Nothing Works	
A	Additional Benefit	
	SOC Works	

• If you just enrolled the purple patients how many patients do you need for 90% power?

What if you KNEW which 10% Benefit

Nothing Works	
Additional Benefit	
SOC Works	Ī

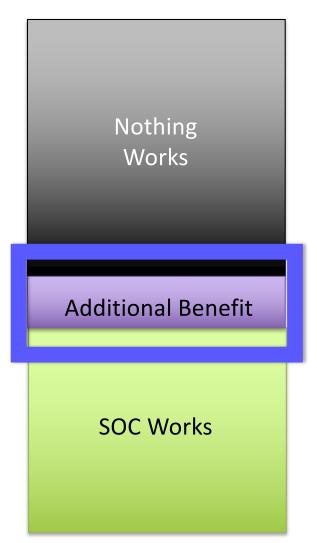
- If you just enrolled the purple patients you need 8 patients for 100% power
- If you could perfectly predict
 0/4 on standard of care
 - -4/4 on new treatment
 - Fisher's exact test p-value = 0.029

What if goda ^KNEW which 10% Benefit



- Enroll 20% to capture the 10%
- 25% cured by SOC
- 25% still not cured
- 50% of enrolled patients benefit

What is the KNEW which 10% Benefit



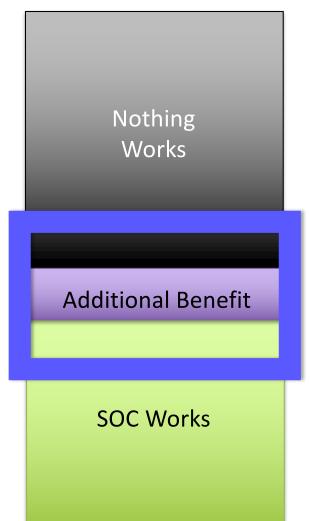
- Enroll 20% to capture the 10%
- 25% cured by SOC
- 25% still not cured
- 50% of enrolled patients benefit
- Need 36 patients for 90% power

Whakindgoarta KNEW which 10% Benefit



- Enroll 30% to capture the 10%
- 33% cured by SOC
- 33% not cured
- 33% of enrolled patients benefit

Whakindgoarta KNEW which 10% Benefit



- Enroll 30% to capture the 10%
- 33% cured by SOC
- 33% not cured
- 33% of enrolled patients benefit
- Need 90 patients for 90% power

Platform Example 2

GBM AGILE Adaptive Global Innovative Learning Environment Trial Design V1

EXAMPLE TRIAL ONLY TRIAL HAS CHANGED DRAMATICALLY SINCE THIS

Thanks to Todd Graves & Don Berry

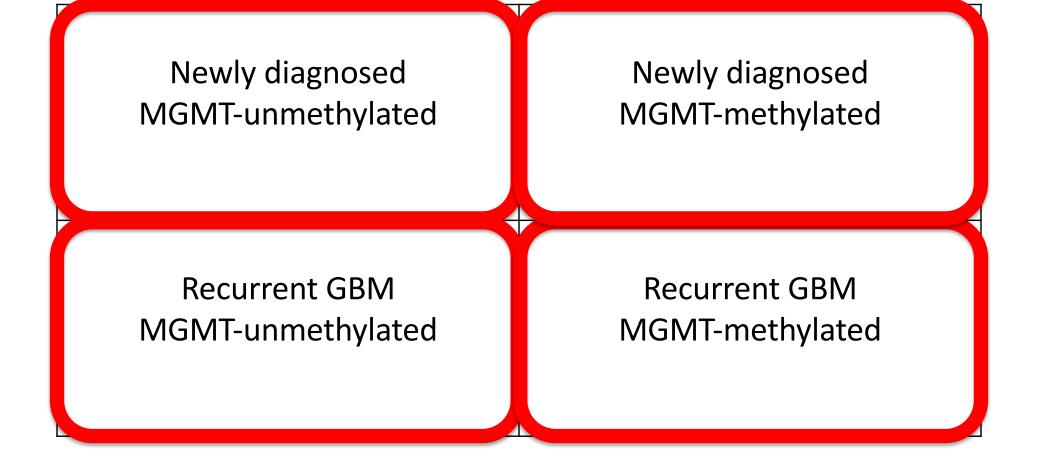
Statistical Model

- Primary outcome: Overall Survival
- Time-to-event model including
 - Age
 - Tumor Size
 - Performance Status
 - Site (to be defined)
 - Drug
 - Drug × Biomarker
 - Drug × Biomarker × Biomarker
- Flexible to add drugs & biomarkers on the fly

Biomarkers \rightarrow Signatures

Newly diagnosed	Newly diagnosed
MGMT-unmethylated	MGMT-methylated
Recurrent GBM	Recurrent GBM
MGMT-unmethylated	MGMT-methylated

2 × 2 Biomarkers \rightarrow 4 Signatures



2 × 2 Biomarkers \rightarrow 3 Signatures

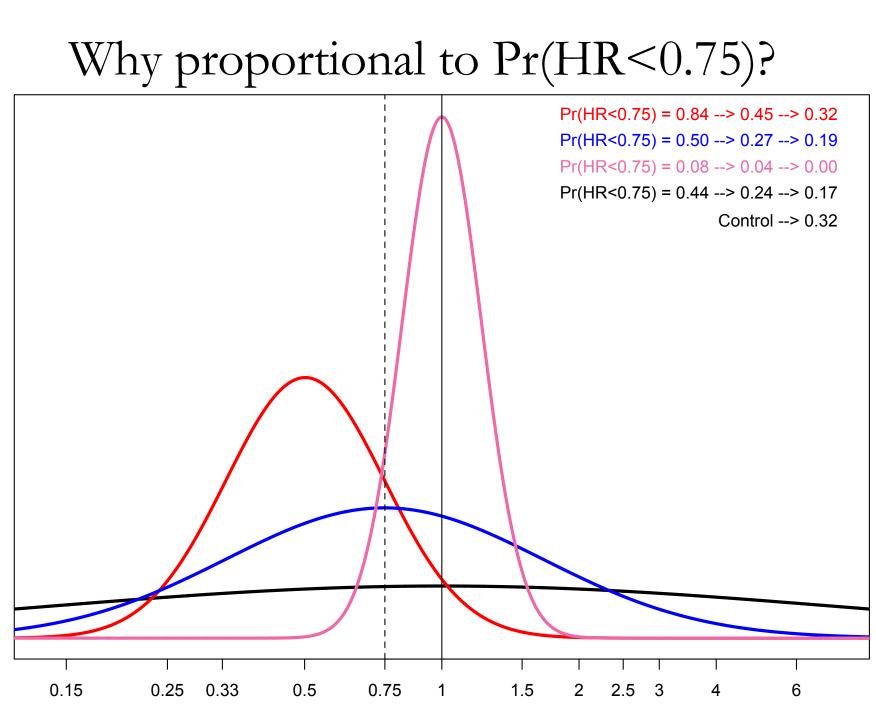
Newly diagnosed	Newly diagnosed
MGMT-unmethylated	MGMT-methylated
Recurrent GBM	Recurrent GBM
MGMT-unmethylated	MGMT-methylated

2 × 2 Biomarkers \rightarrow 1 Signature

Newly diagnosed	Newly diagnosed
MGMT-unmethylated	MGMT-methylated
Recurrent GBM	Recurrent GBM
MGMT-unmethylated	MGMT-methylated

Response-adaptive randomization

- Randomize separately within signature
- Randomization probability proportional to Pr(HR < 0.75)
- If randomization probability < 5%, round to 0
- If N < 50, min rand prob = 1/ # of drugs
- Probability randomize to control =
 Probability randomize to best drug
- Update monthly



Graduation

- A drug graduates if, *within any signature*,
- • $\Pr(HR < 1) > 99\%$
- •Min 75 patients on that drug overall
- •Min 300 pt-months exposure on that signature

When a drug graduates

- •Drug out of trial
- •Data for all subtypes delivered to sponsor

Futility

A drug is removed from the trial for futility if

- Pr(HR < 0.75) < 5% for all signatures
- At least 50 patients

Or

• Been enrolling for 3 years

Stop at Max N=150 over all signatures

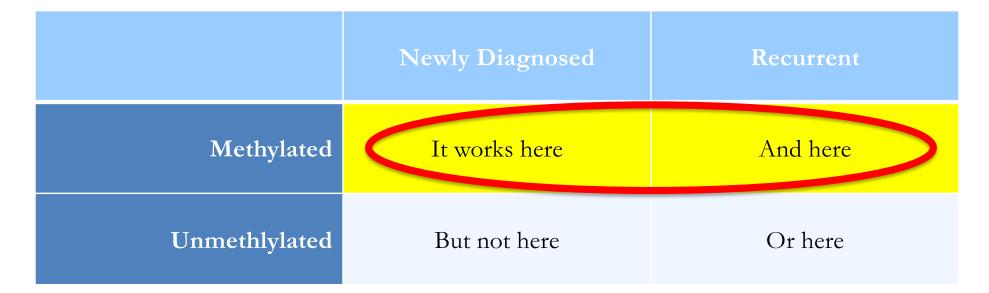
	Newly Diagnosed	Recurrent
Methylated	It works here	
Unmethlylated		



Identify it works in red lasso: We made the right choice



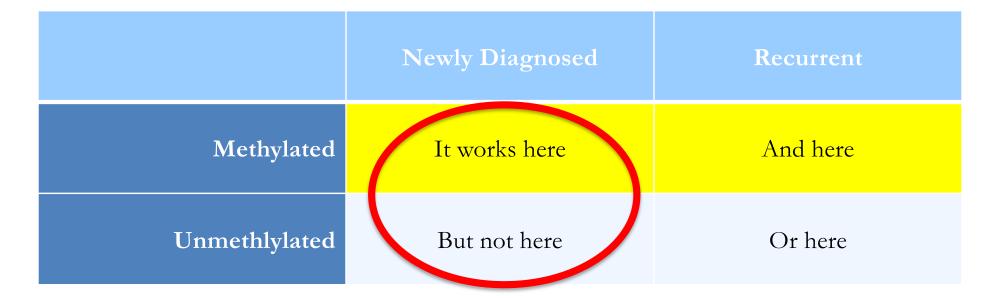
Identify it works in red Iasso: Have we made the right choice? Is this a Type 1 error? Call this a SUPERSET error



Identify it works in red lasso: We made the right choice



Identify it works in red lasso: Did we made the right choice? We made a "Type 2 error" Call this a SUBSET error



Identify it works in red Iasso: Did we made the right choice? We got one right but made a "Type 1 Error" & "Type 2 error"! Call this a "MIXED TYPE ERROR"

Factors We Can Tune

- Max N per drug
- Signatures (Biomarker-drug interactions)
- Randomization algorithm
- Futility rule
 - Pr(HR < 0.75)
 - Min N
 - Max time allowed to accrue
- Graduation rule
 - $Pr(HR \le 1)$
 - Min N, Min Exposure

Learn & Confirm Using Biomarkers

- Make confirmatory trials dramatically smaller
 - Or learn & confirm within a trial
- Lead us toward personalized medicine
 What works best in whom?
- May require larger platforms trials, data sharing & adaptive randomization to efficiently identify
- Different drugs work in different types of patients
 - Not one trial, one patient type
 - Learn, confirm, perpetually

Challenges in Platform Trials

- Complexity in trial implementation and planning
- Collaborations across sponsors who initiates the planning?
- Timely communication between participating sites and data coordinating units
- Sponsors sacrifice autonomy in running the trial
- Determining shared costs
- Identifying what to report when
 - iSpy2 has rules for 'graduating'
 - When to report subgroup results broadly?

Platform Trial Efficiencies

- Useful for evaluating combinations of treatments and for direct comparisons between competing treatments
 - Decide a prior whether each vs. control or vs. each other
- Do not require a new trial infrastructure for every treatment under investigation
- Easier for regulators given evidence comes in common form
- Always new drugs on horizon
 - Even if lull, get SOC in the process
- Can build in Phase 2/3 design
 - Learn & confirm
- Need to prospectively define control group
 - Concurrent controls
 - "Time machine"
 - What if control group changes

Conclusions

- Adaptive trial designs can be used to create a seamless process in which new evidence about effectiveness is immediately used to improve patient care
- A platform trial can extend this process beyond a single treatment or few treatments
- Current work is focused on embedding this approach into the health care infrastructure
- Patients will benefit if we merge clinical trials and decision support into a single, continuous process

Thank you!

- Thank you for a great class.
- Please complete evaluations To access evaluations, log in to https://si.biostat.washington.edu/user/login, click "My Account" in the upper right, the evaluations will appear on your dashboard. After you have completed your evaluations, a link to download the certificate of completion will appear within 24 hours.

Example: Goldilocks Trial with 2 Endpoints & Informative Prior on Longitudinal Model

Background

- Medical device to treat atrial fibrillation (AF)
- Used during open cardiac surgery

 Only used when surgery being done for other reason
 e.g., CABG, Valve replacement
- Label was to 'ablate cardiac tissue' not 'treat AF'
- Trial needed to produce evidence of safety and efficacy for treatment of AF
- Controlled trial not possible due to extensive use

Background

- Early safety study with matched controls failed to enroll
 - Matched control having same cardiac surgery without AF treatment component
 - Stopped @ 32 months when 39 cases & just 5 controls enrolled
- FDA suggested to company to explore Bayesian adaptive trial with safety & efficacy OPCs

Objective Performance Criteria

- Efficacy OPC (6m)
 - AF free & off AF drugs at 6 months
 - Goal: 70%, $\delta_{\rm E} = 10\%$
 - Based upon published rates of this procedure
 - 10 papers had 60.1% efficacy
- Safety OPC (1m)
 - Free of significant adverse event
 - Goal: 13.95%, $\delta_{\rm S} = 5\%$
 - Based upon published SAE rates in Cut & Sew MAZE

Statistical Endpoints

• Show $\Pr(p_E > 0.60) > 0.975$

 $-70\% - \delta_{\rm E} = 70\% - 10\% = 60\%$

- Show $\Pr(p_S < 0.1895) > 0.95$ - 13.95% + $\delta_S = 13.95\% + 5\% = 18.95\%$
- Achievable in 100 patients if
 - observed efficacy $\geq 70\%$
 - observed safety $\leq 12\%$
 - basically point estimates have to match or beat OPCs
- $p_E, p_S \sim \text{Beta}(1,1)$ priors for both endpoints

Goldilocks Design

- Enroll 50 100 patients
 - Must have 20 patients at 6 months or skip analysis
- Interim analyses every 5 patients
- Final sample size based upon predictive probabilities
- Expect to enroll 5 patients per month
 ~30 patients enrolled without complete 6m data

Stopping Decisions

- P_n = Pr(Meet Efficacy & Safety Goals with current sample size n | Current Data)
 - If $P_n \ge S_n$ then stop <u>accrual</u> for predicted success - $S_n = 0.90$ for n=50-65 - $S_n = 0.85$ for n=70-80 - $S_n = 0.80$ for n=85-95
- $P_{max} = \Pr(\text{Meet Efficacy} @ \text{Safety Goals with} 100 \text{ patients} | \text{Current Data})$
 - If $P_n \leq F_n$ then stop <u>trial</u> for futility
 - $-F_n = 0.05$ for n=50-70
 - $-F_n = 0.10$ for n=75-95

Longitudinal Model

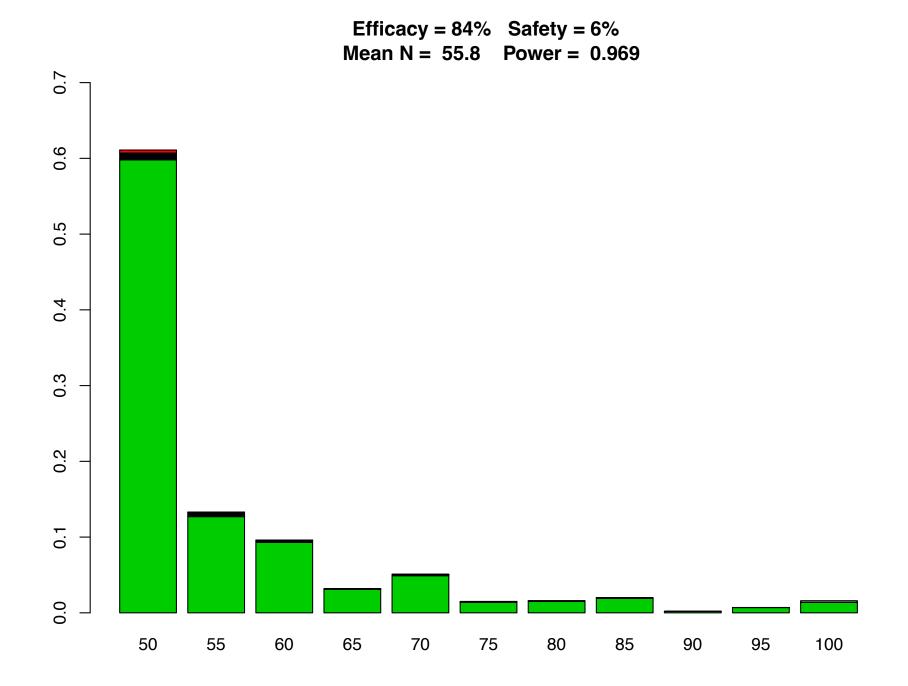
- Efficacy outcome is AF-free and off AADs at 6m
- Interim outcome at 3-months is whether patients are AF-free already
- Predict 6m outcomes using Beta-Binomial

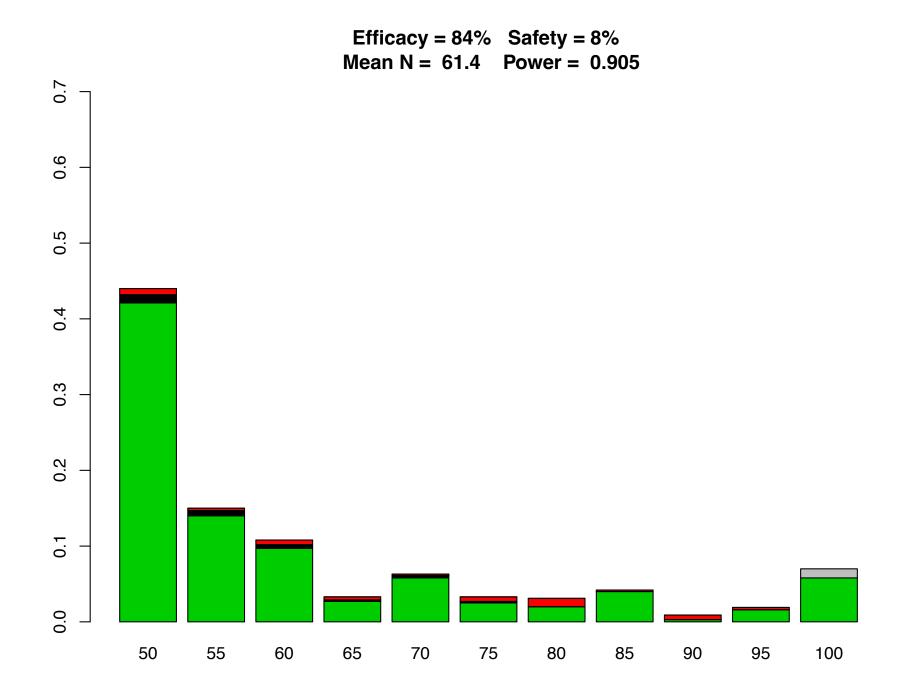
Group	α	β	Prior Mean
No 3m data	5	1	83%
In AF	4.2	1.8	70%
AF-free	5.4	0.6	90%

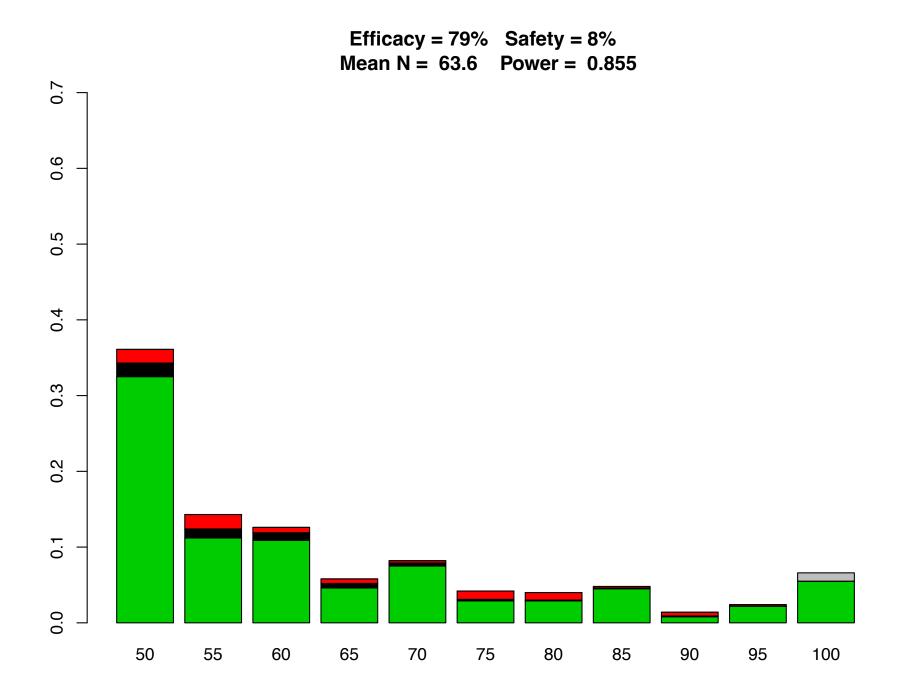
Operating Characteristics for Trial with $p_T = 0.84, p_S = 0.08$

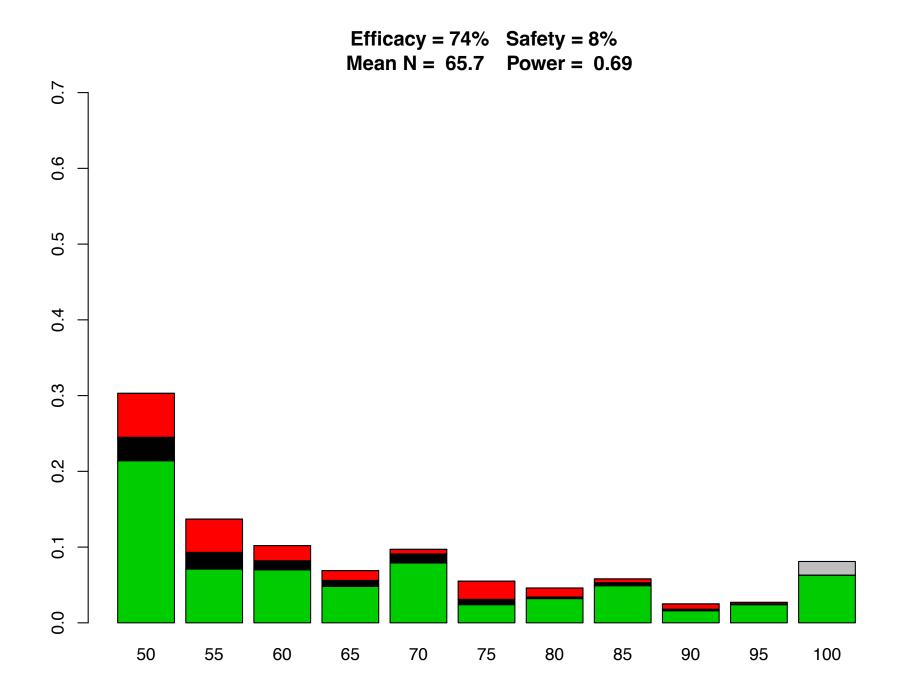
Sample Size	Proportion Of Trials	Stop for Futility	Stop Early For Success	& Lose	& Win
50	0.440	0.008	0.432	0.011	0.421
55	0.150	0.003	0.147	0.007	0.140
60	0.109	0.006	0.102	0.005	0.097
65	0.033	0.004	0.029	0.002	0.027
70	0.063	0.002	0.061	0.002	0.058
75	0.034	0.006	0.027	0.002	0.025
80	0.031	0.011	0.020	0.000	0.020
85	0.042	0.002	0.040	0.000	0.040
90	0.009	0.006	0.003	0.000	0.003
95	0.019	0.003	0.016	0.000	0.016
100	0.070		0.070	0.011	0.058
Total	1.000	0.053	0.947	0.042	0.906

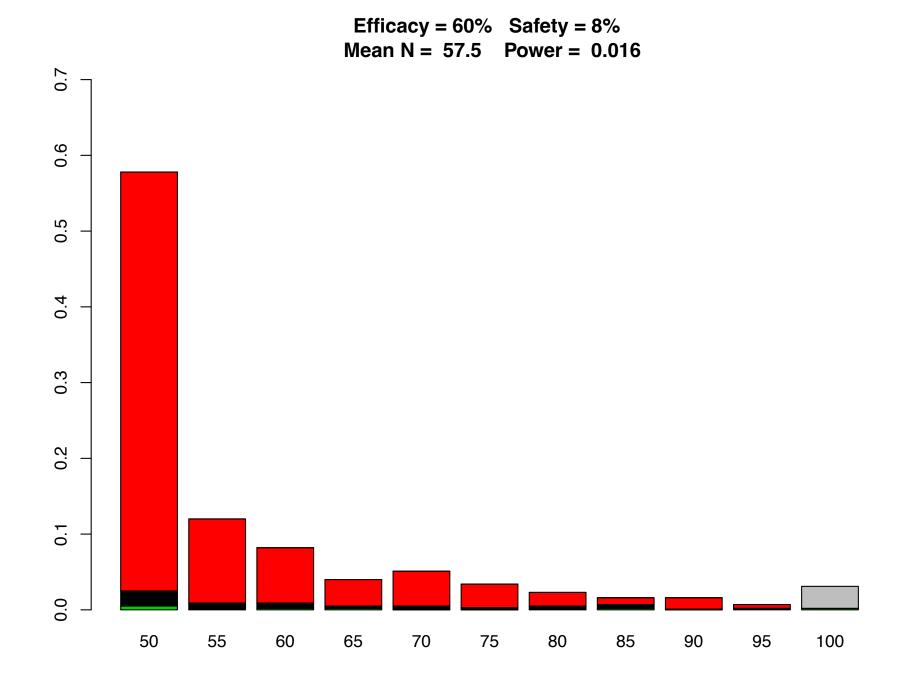
Mean Sample Size = 61.6, SD = 15.6

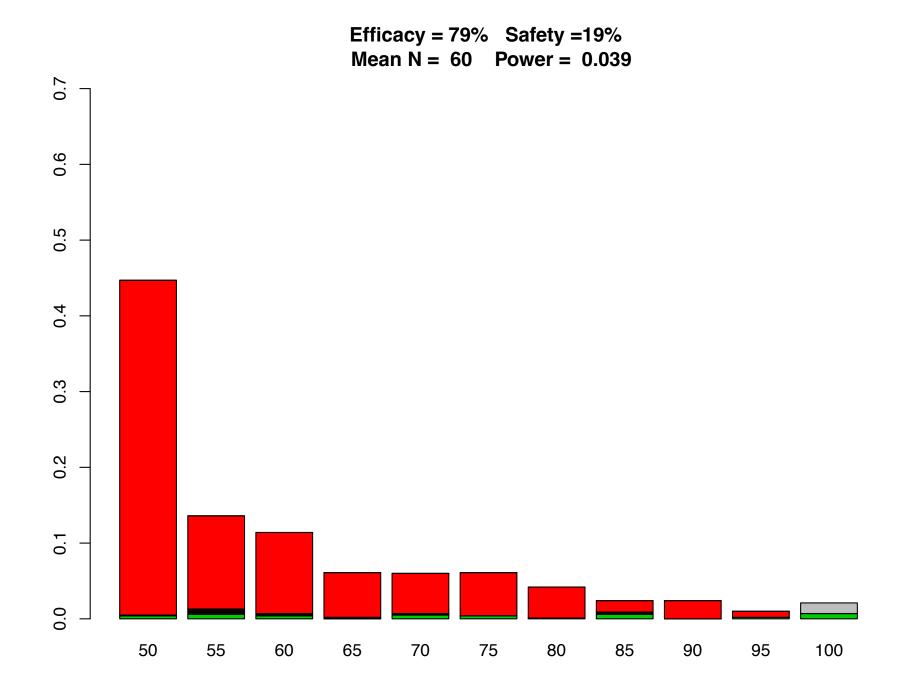












Interim Analysis

- No look at 50 patients
- At 55-patients August 24, 2009
 - All patients through 30-day safety, 5/55 had
 SAEs
 - -24/29 efficacy successes at 6-months
 - 21 subjects remain under surveillance
 - -37/50 successes would show

 $\Pr(p_t > 0.60 \mid 37 \text{ of } 50) = 0.978 > 0.975$

- Total number of efficacy successes $X = 24 + x_0 + x_+ + x_-$

Interim Analysis

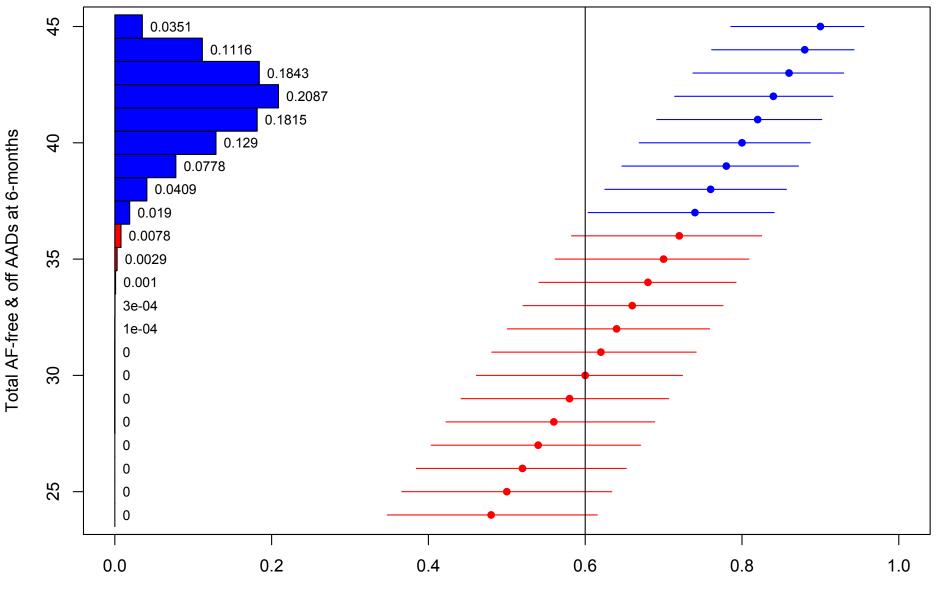
- x_o = 5 enrolled with < 3mo follow-up - x_o ~ Beta-Bin(n₀ = 5, α=5+24, β=1+5)
 x- = 3 enrolled not AF-free at 3mo - x₋ ~ Beta-Bin(n₋ = 3, α=4.2+3, β=1.8+1)
 x+ = 13 enrolled AF-free at 3mo - x+ ~ Beta-Bin(n+ = 13, =5.4+17, =0.6+3)
- $\Pr(24 + x_0 + x_1 + x_+ \ge 37) = 0.988$

Interim Analysis

•
$$x_0 = 5$$
 enrolled with < 3mo follow-up were right on
- $x_0 \sim Beta$ -Bin($n_0 = 5$, $\alpha = 5+24$, $\beta = 1+5$)
• $x_- = 3$ enrolled not AF-free at 3mo
- $x_- \sim Beta$ -Bin($n_- = 3$, $\alpha = 4.2+3$, $\beta = 1.8+1$)
• $x_+ = 13$ enrolled AF-free at 3mo
- $x_+ \sim Beta$ -Bin($n_+ = 13$, $= 5.4+17$, $= 0.6+3$)
• $x_+ = 13 = 0.6+3$

• $Pr(24 + x_0 + x_1 + x_+ \ge 37) = 0.988$

Prediction of 21 remaining pts based on 29 observed pts



Probability & 95% Cl

Sample Size Analysis at 55 pts

Current Patients Enrolled: 55 Current patients not contributing to efficacy: 5 Current Safety Events: 5 of 55 patients Current Efficacy Successe: 24 of 29 patients Current Efficacy Successes: 24 of 29 patients Current Efficacy Successes: 3 of 4 Efficacy Failures at 3 months Current Efficacy Successes: 17 of 20 Efficacy Successes at 3 months

0 enrolled patients to predict for 1mo safety outcomes
45 future patients to predict for 1mo safety outcomes
5 enrolled patients with <3mo to predict for efficacy outcomes
3 enrolled patients with AF at 3mo to predict for 6mo efficacy outcomes
13 enrolled patients without AF at 3mo to predict for 6mo efficacy outcomes
45 future patients to predict for 6mo efficacy outcomes</pre>

Decision Rule: Stop Enrolling Due to Predicted Success

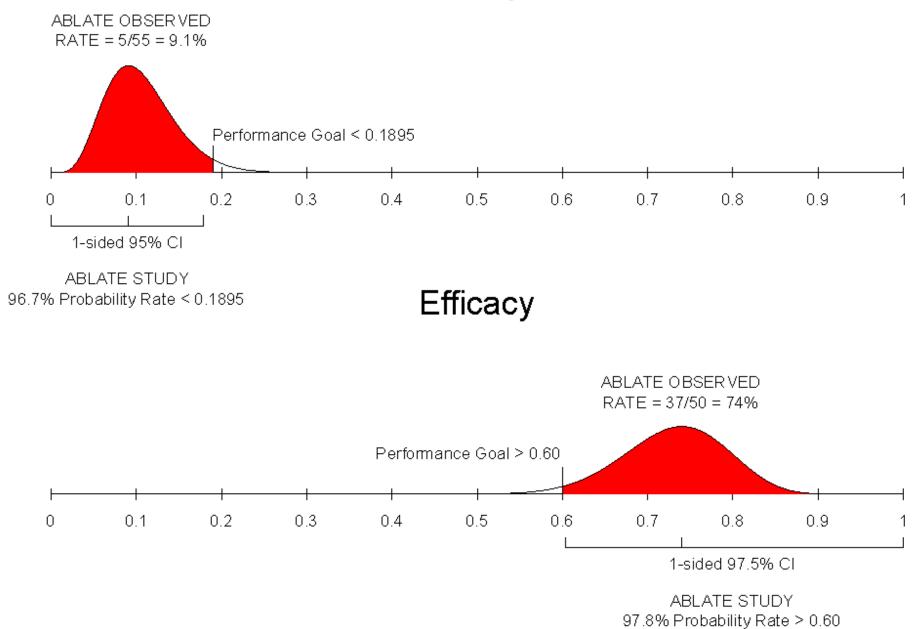
	Prob Win Efficacy	Prob Win Safety I		.988 > .90
Now Max N	0.988 0.992	1.000 0.846	0.988	Stop for
				predicted success
				259

Stopped Accrual for Predicted Success

- Accrual stopped with 55 patients in
- Continue to follow 21 enrolled patients
- Perform final analysis on complete data

- Final Data
 - 5/55 SAEs
 - 37/50 AF-free and off AADs

Safety

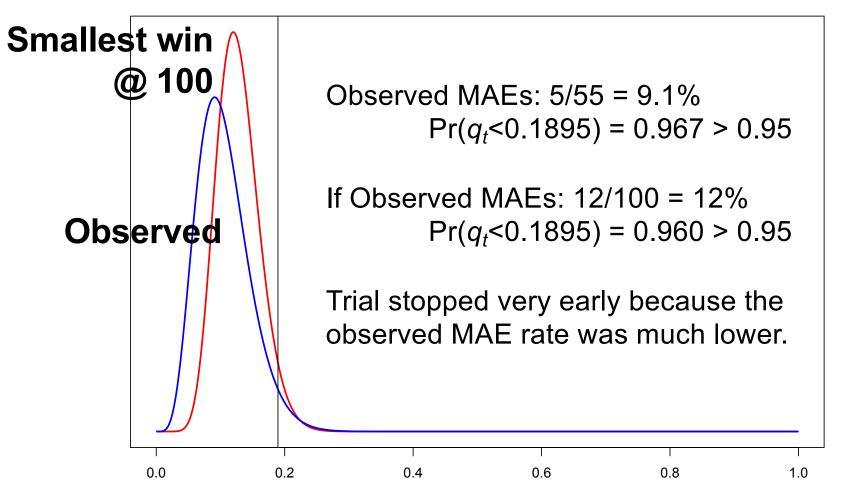


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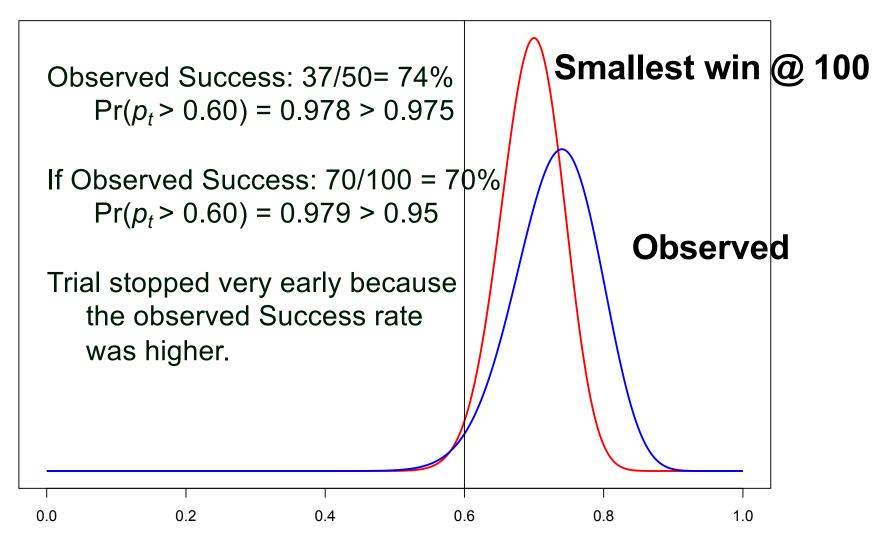
Post Trial Discussion with FDA

- Efficacy barely won
 - One less success would have failed to meet primary endpoint
 - Not a robust win, in part due to post-hoc changes related to inc/excl criteria
- Some concern with n=55
 - But this was possible based upon design
 - Safety OPC = 0.1395, observed 0.091
 - Efficacy OPC = 0.70, observed 0.74

Safety: Compare Stopping at n=55 to Maximum Trial Size n=100



Efficacy: Compare Stopping at n=50 to Maximum Trial Size n=100



FDA Advisory Panel Vote Oct 2011

- Is there reasonable assurance that the AtriCure Synergy Ablation System is effective ...?
 – 9 for, 0 against
- Is there reasonable assurance that the AtriCure Synergy Ablation System is safe...?
 - 5 for, 4 against, 1 abstain (chair broke 4-4 tie)
 - Largely due to patients needing pacemakers
- Do the benefits ... outweigh the risks ...?
 5 for, 3 against, 1 abstain



ARRHYTHMIA/EP

AtriCure AF ablation system gets cautious thumbs-up from FDA advisors



Rockville, MD (updated) - The **AtriCure Synergy Ablation System** squeaked by today in a meeting of the **Food and Drug Administration**'s Circulatory System Devices advisory panel when panelists gave a cautious nod of approval for the device.

Five panel members believed the benefits of the ablation system outweighed the risks when used in the treatment of atrial-fibrillation (AF) patients undergoing open concomitant coronary artery bypass graft (CABG) surgery and/or valve replacement or repair. Three panelists expressed doubts about the system and cautioned against device approval, voting that they did not believe the benefits outweighed the risks.

One panelist abstained from voting on the benefit/risk trade-off question.

In a vote on efficacy alone, all panelists believed the ablation system is effective in restoring sinus rhythm, but they were split for the vote on safety. Chair of the advisory panel, **Dr John Hirschfeld** (University of Pennsylvania, Philadelphia), cast the deciding vote on safety, saying he believes there is reasonable assurance the device is safe for use in patients who meet the indication criteria. Overall, the panel voted 9 to 0 on efficacy and 5 to 4 on safety (with one abstention).

Panel member **Dr David Slotwiner** (Long Island Jewish Medical Center, New Hyde Park, NY) voted in favor of the ablation system, saying that he believes the benefits outweigh the risks.

"I think it's effective at creating these ablation lesions, and I think it's effective in many people for maintaining sinus rhythm, although what that means [clinically] for many patients remains unanswered," he said. "But I hope, mostly, that if an approval is granted, it will allow us to get more information and to educate more surgeons so that the procedure becomes more widely available and we understand better who will benefit the most."

FDA Approved Dec 14, 2011

- Study Design (from device label)
- ABLATE was a multi-center, prospective, nonrandomized study based on a Bayesian adaptive design that provides high probability of demonstrating safety and effectiveness of the AtriCure Synergy Ablation System for the treatment of permanent atrial fibrillation. The safety and effectiveness of the device was compared to performance goals derived from historical information. The Bayesian adaptive clinical design incorporated interim analyses of the data to determine the point of completion of trial enrollment. Enrollment was targeted to be between 50 and 100 subjects at 20 sites. The study was designed to have an initial assessment of results at the point that 50 subjects were enrolled with a minimum of 20 subjects completing their six-month follow-up visit. Nine investigational sites enrolled 55 subjects.

Lessons

- Ensure minimum sample size will suffice
 - Not just statistical, but impactful
 - Company did a continue access protocol to get more patients during review, leading to panel
- Ensure data isn't coded optimistically
- Ensure inclusion / exclusion criteria rigorously followed
- Goldilocks gets the size 'just right' but that means you can be close to 'just wrong' if some data changes post hoc