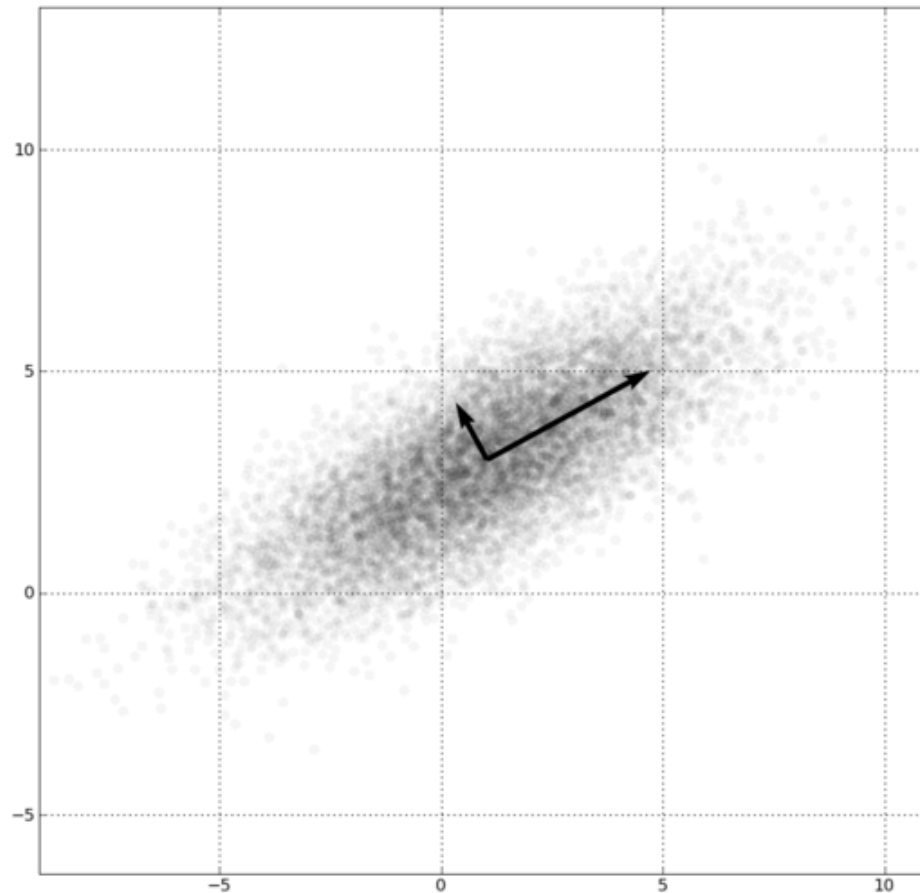


# Population Structure Analysis

# Learning objectives

- Methods to identify global estimates of population structure
  - Principal Component Analysis (PCA)
  - Admixture
- Local ancestry can identify segments of the genome corresponding to different ancestries.
- Local ancestry can be applied in a number of different ways
  - Demographic modeling
  - Selection
  - Refining PCA signals
  - Association analyses

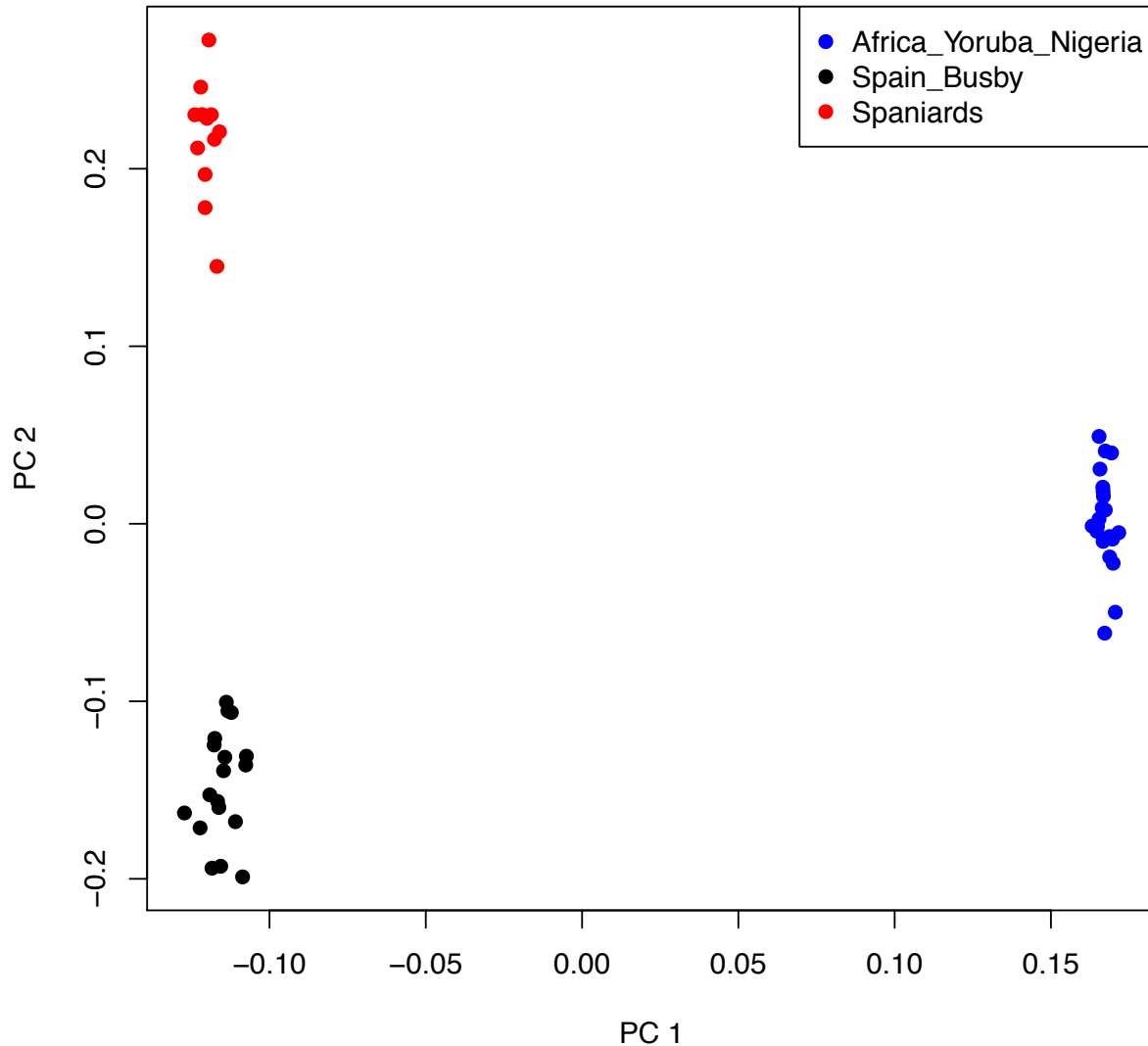
# Principal Component Analysis (PCA)



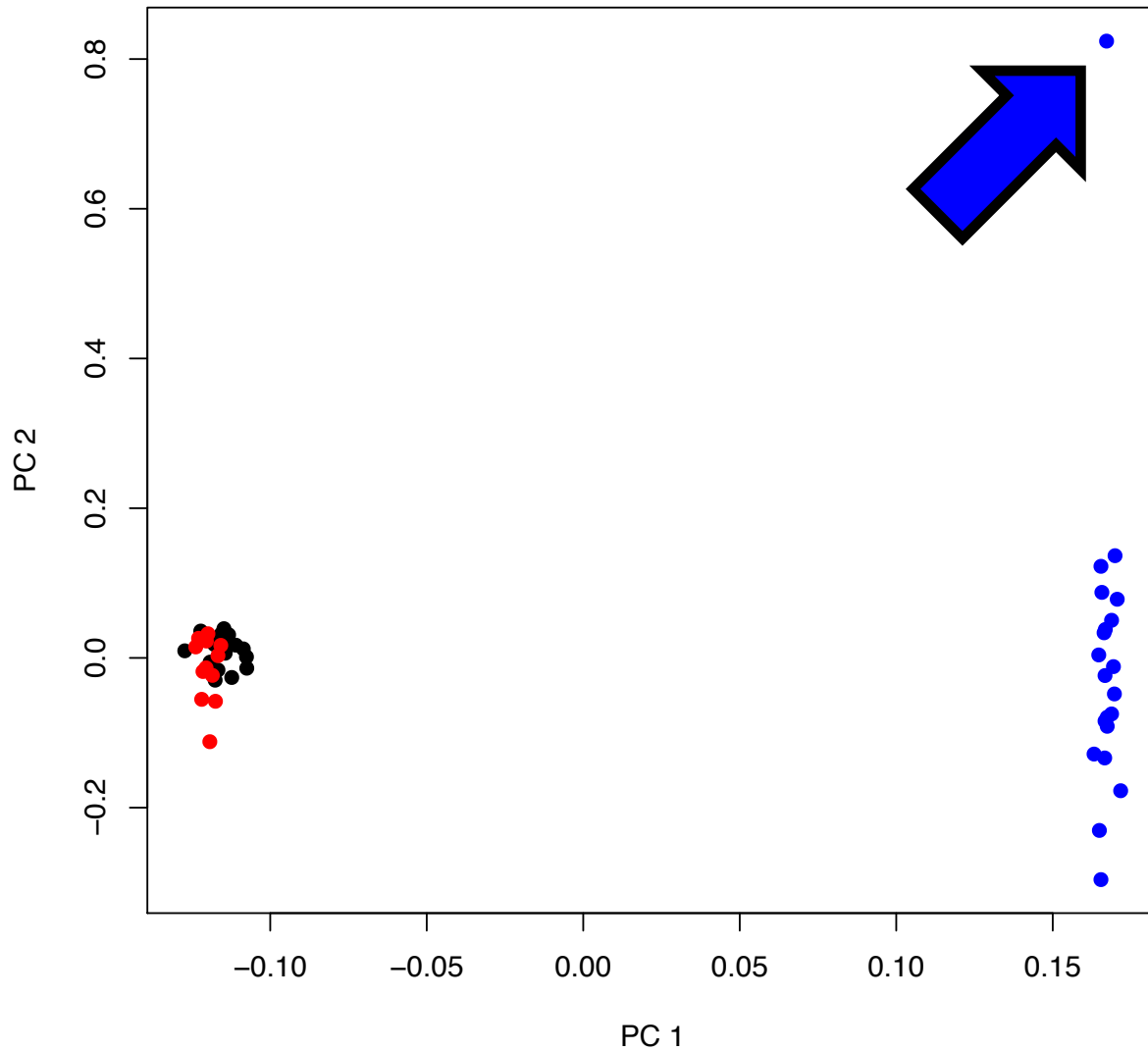
# PCA

- Uses
  - Highly sensitive summary of all the data
  - Summarize population structure
  - Identify groups within data
  - Sanity check for study design
    - E.g. Diseased individuals cluster vs controls
  - Sanity check when combining data
- Pitfalls
  - Only look at the first few PCs
  - All axes are biological (once first few are)
  - Identifying significance of an axis is non-trivial
- Assumptions
  - Linear relationship between data
  - Variants are independent (LD)

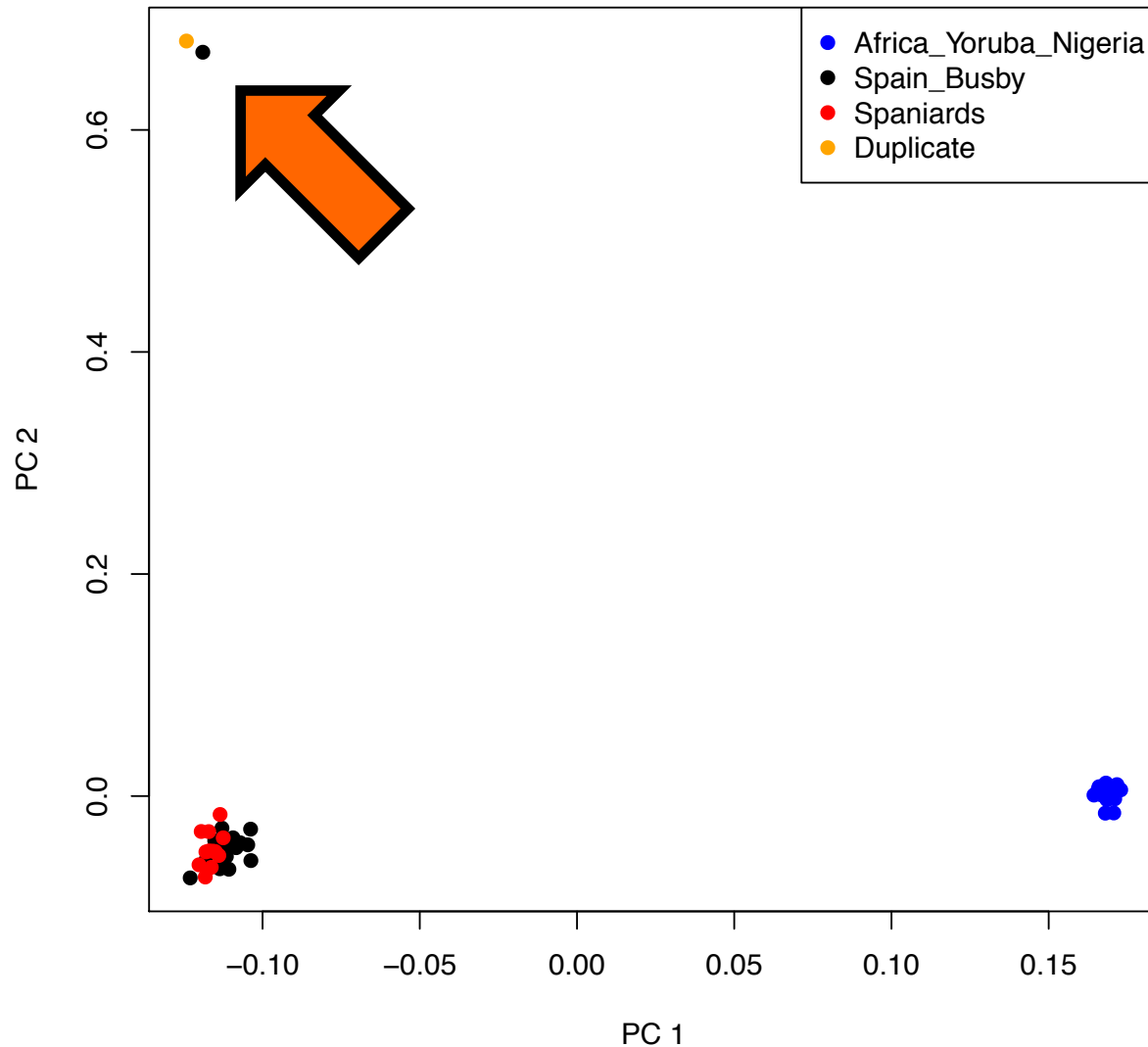
# PCA Example: Strandedness



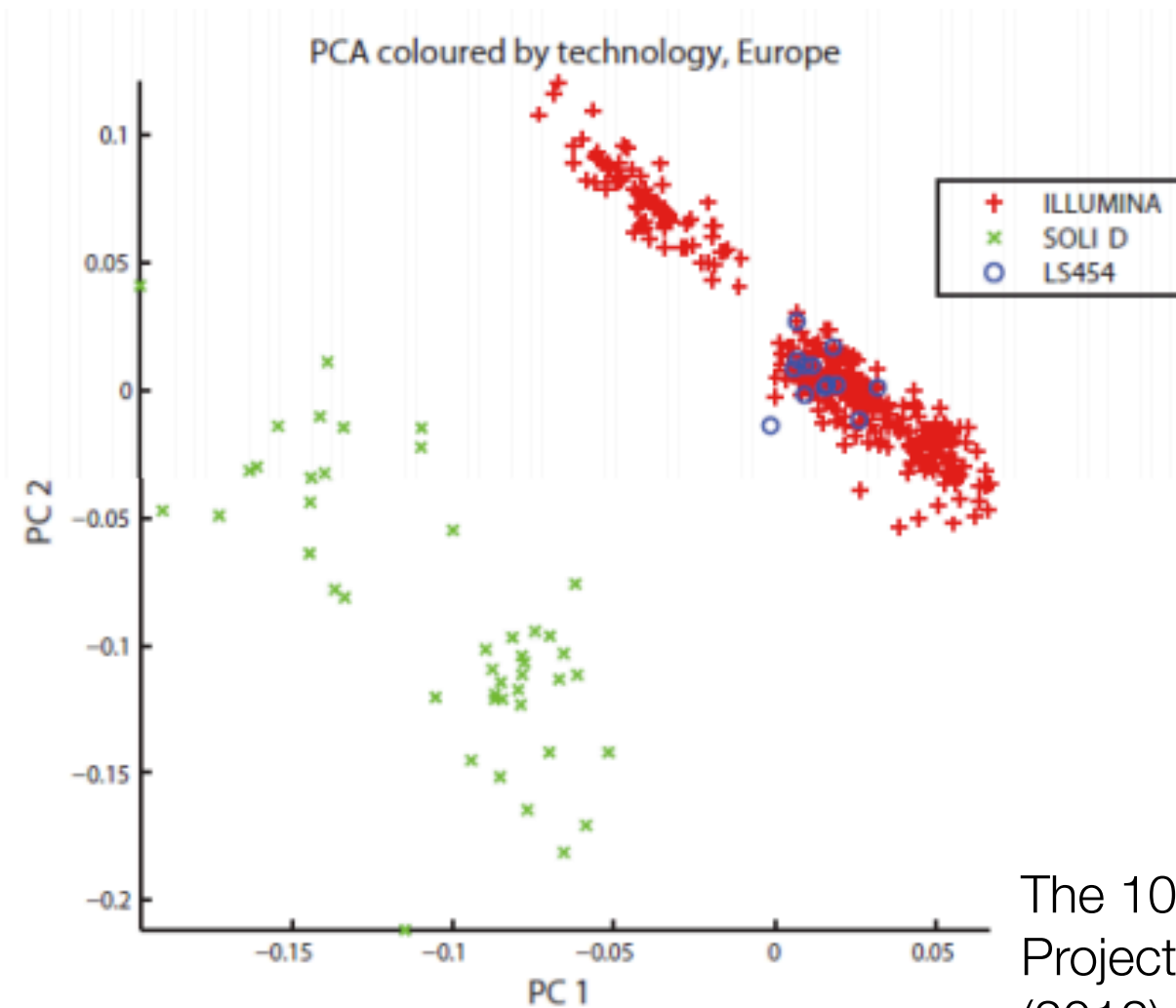
# PCA Example: Insignificance



# PCA Example: Relatedness



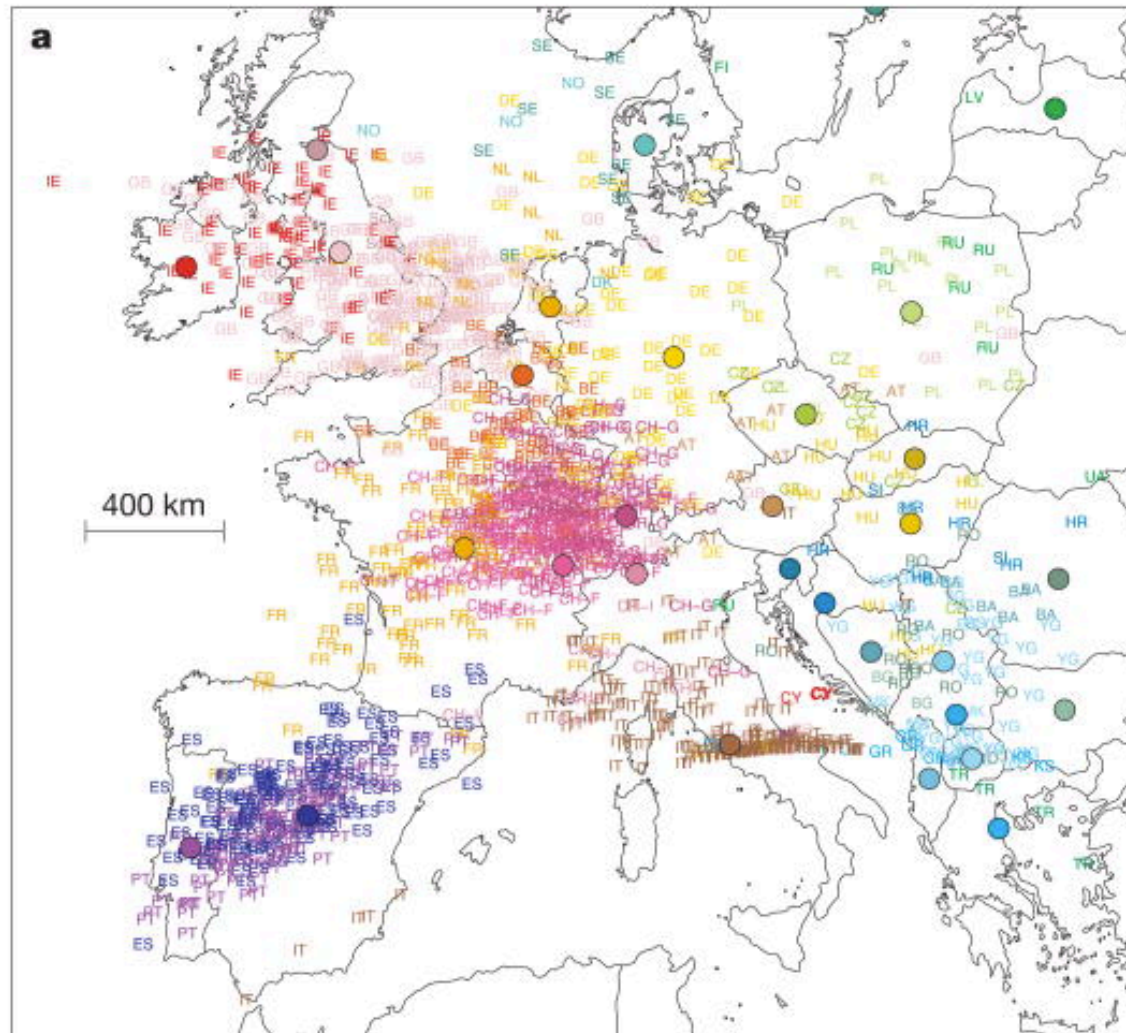
# PCA Example: Technical Issues



The 1000 Genomes  
Project Consortium  
(2012) Nature



# “Genes mirror geography within Europe”



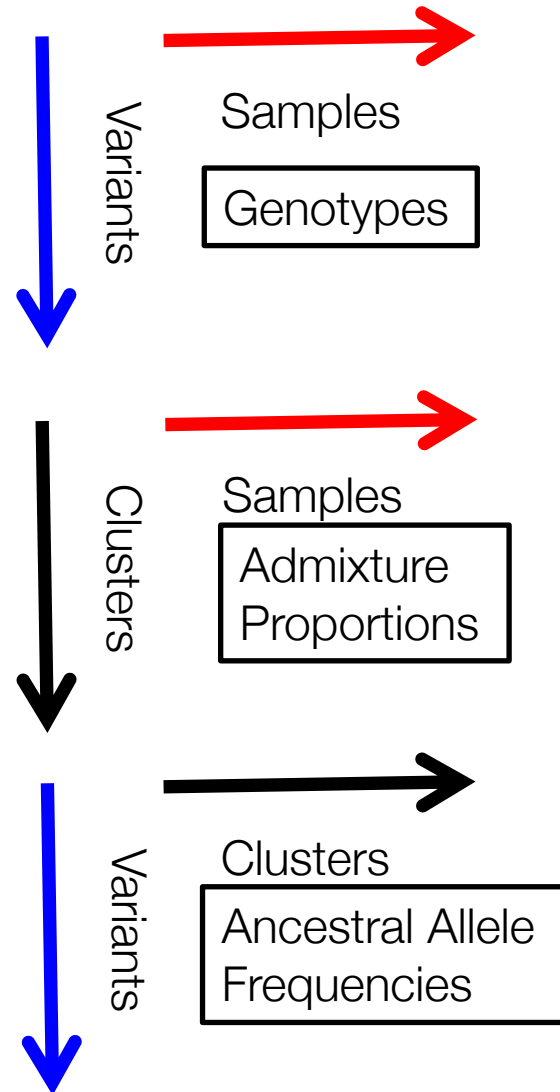
Novembre et al.  
(2008) Nature

# ADMIXTURE (Alexander et al. 2009)

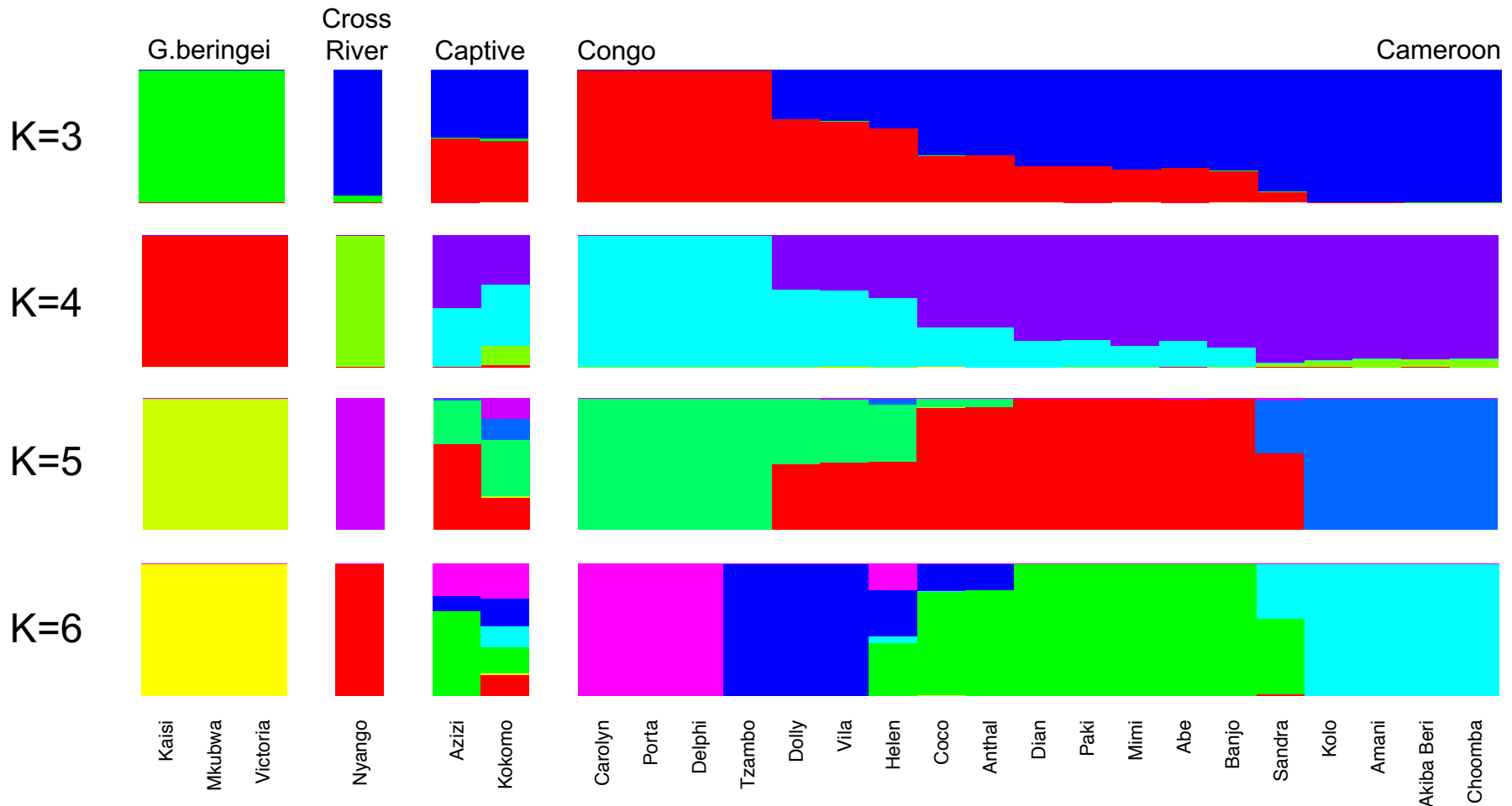
$$G = \begin{bmatrix} g_{11} & g_{12} & \cdots & g_{1N} \\ g_{21} & g_{22} & \cdots & g_{2N} \\ \vdots & \vdots & \ddots & \vdots \\ g_{M1} & g_{M2} & \cdots & g_{MN} \end{bmatrix}$$

$$Q = \begin{bmatrix} q_{11} & q_{12} & \cdots & q_{1N} \\ q_{21} & q_{22} & \cdots & q_{2N} \\ \vdots & \vdots & \ddots & \vdots \\ q_{K1} & q_{K2} & \cdots & q_{KN} \end{bmatrix}$$

$$P = \begin{bmatrix} p_{11} & p_{12} & \cdots & p_{1K} \\ p_{21} & p_{22} & \cdots & p_{2K} \\ \vdots & \vdots & \ddots & \vdots \\ p_{M1} & p_{M2} & \cdots & p_{MK} \end{bmatrix}$$



# Admixture analyses



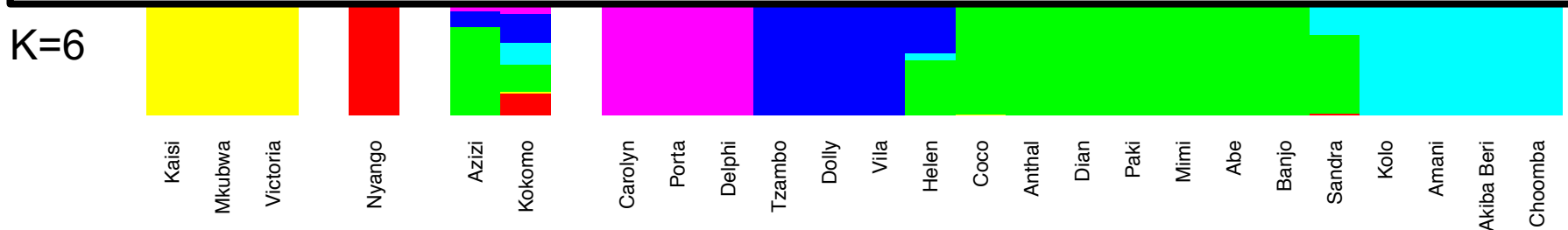
Prado-Martinez et al. (2013) Nature

# Admixture analyses: when is the K correct?

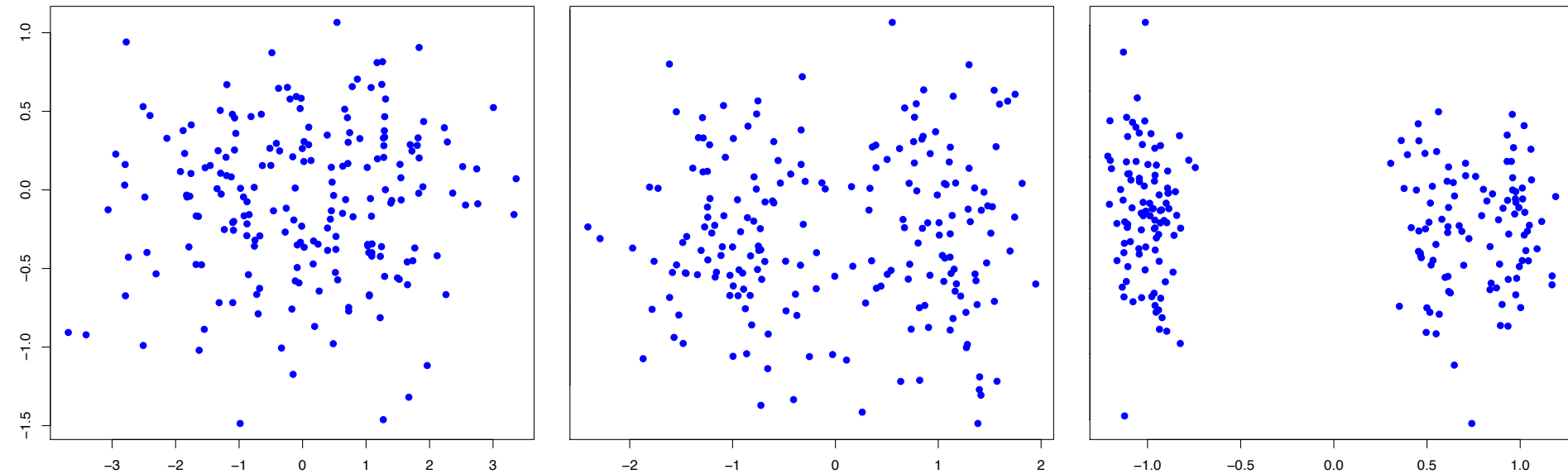


“In practice, people often try different K, and choose the K that makes most biological sense.”

-Frappe Manual



# The K Problem



How many different means are there?

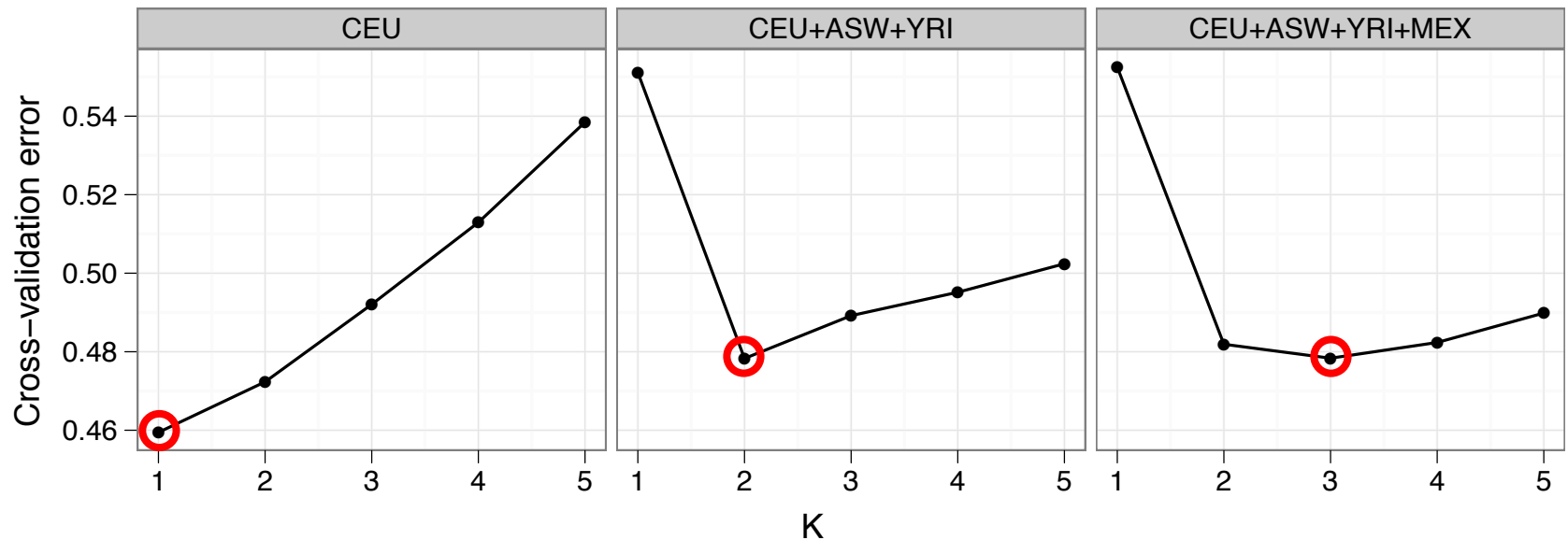
# ADMIXTURE: using cross validation to identify the best K

$$G = \begin{bmatrix} g_{11} & \cancel{g_{12}} & \cdots & g_{1N} \\ \cancel{g_{21}} & g_{22} & \cdots & g_{2N} \\ \vdots & \vdots & \ddots & \vdots \\ g_{M1} & g_{M2} & \cdots & \cancel{g_{MN}} \end{bmatrix}$$

$$\hat{g}_{li} = 2 \sum_{k=1}^K p_{lk} \times q_{ki}$$

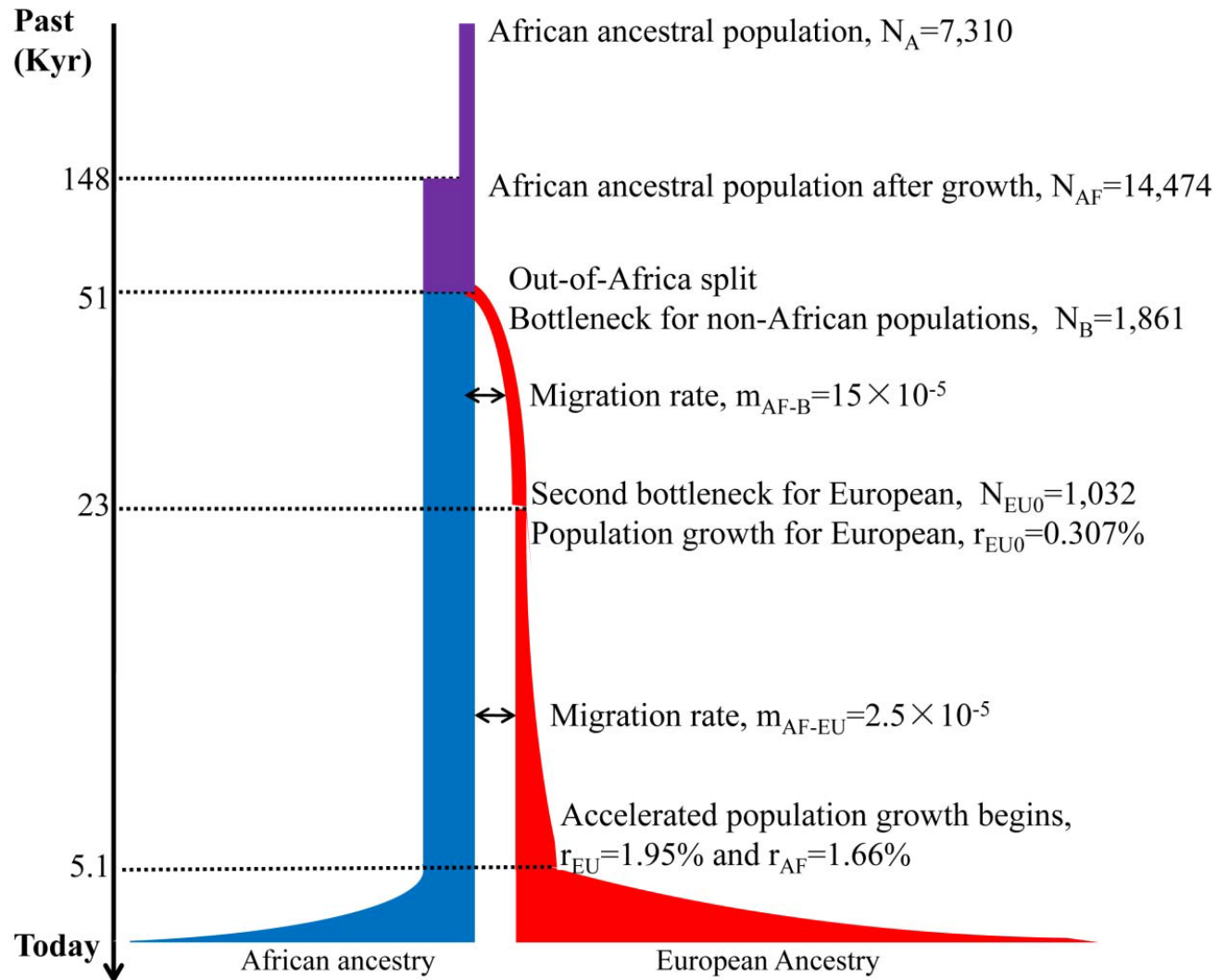
Alexander and Lange  
(2011) BMC Bioinformatics

# How well X-validation performs



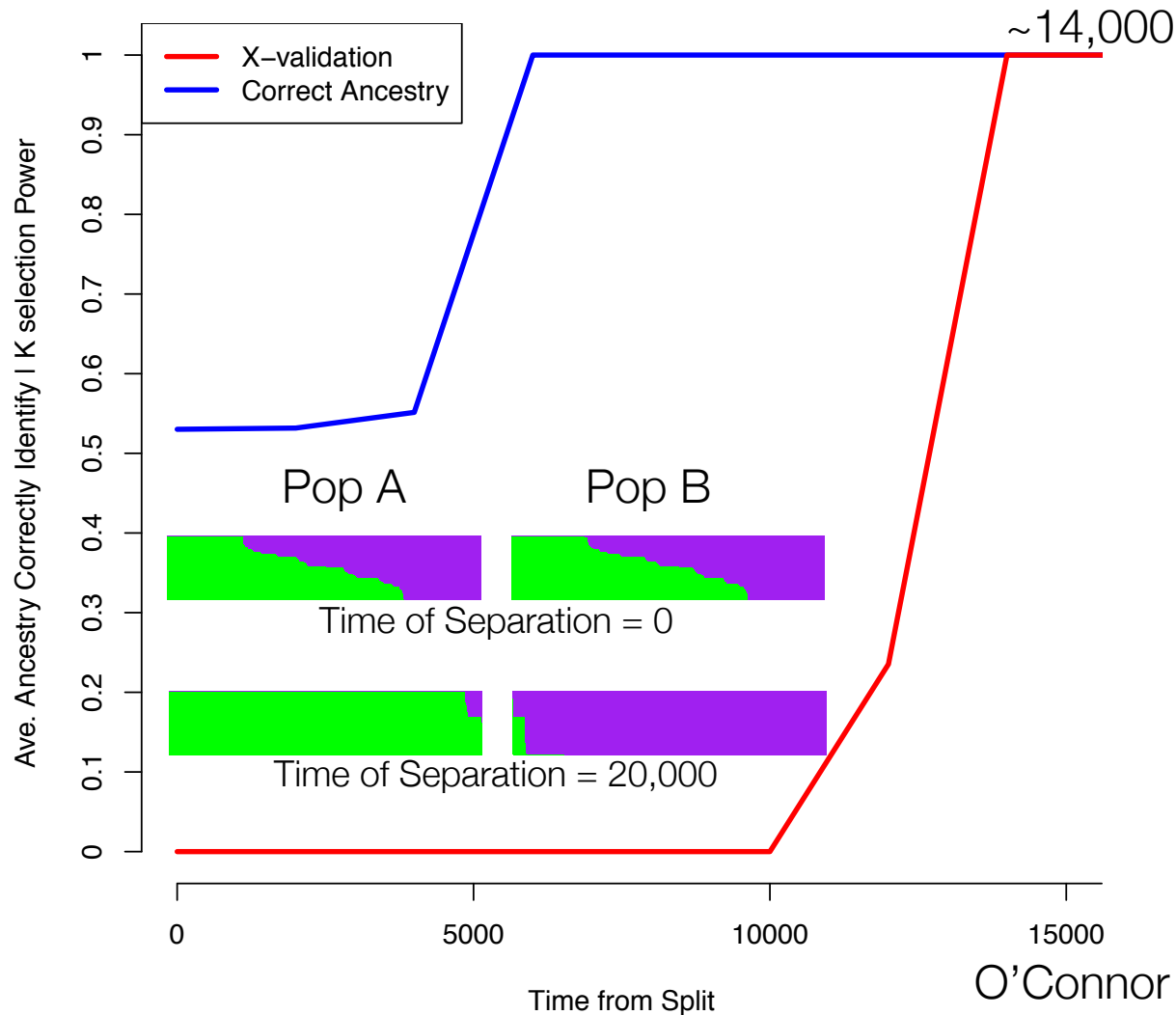
Alexander and Lange  
(2011) BMC Bioinformatics

# Test it with ESP inspired simulations





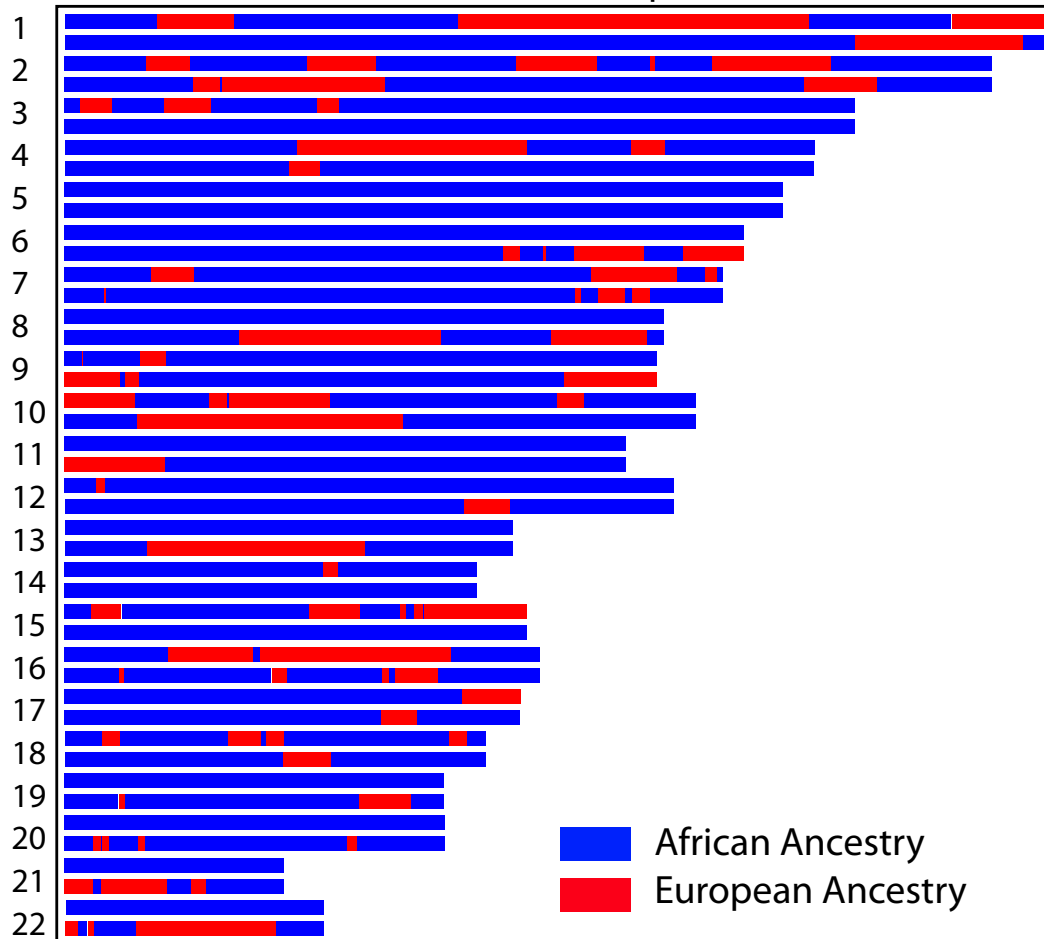
# X-validation's performance as a function of split time



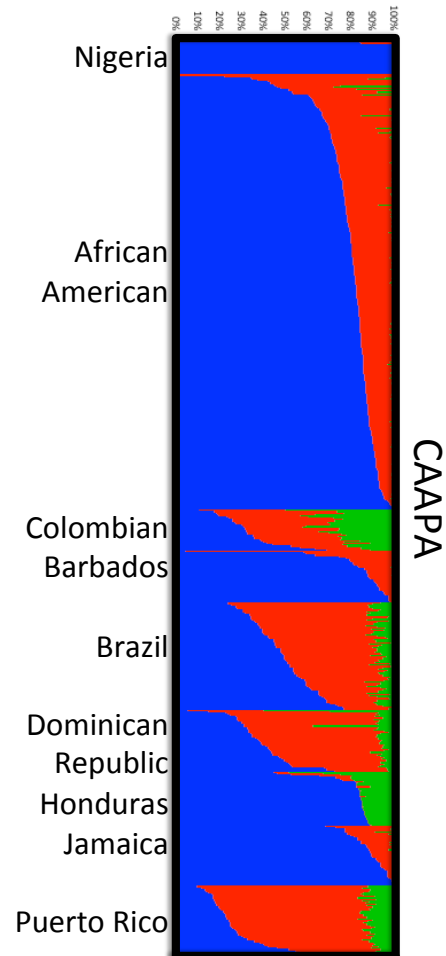
# Tricks to effectively use ADMIXTURE

- This is a Maximum Likelihood framework with many parameters
  - Run multiple times (I usually use  $>10$ ) for each  $K$  taking the best log-likelihood (an output parameter).
  - This deals with local minimum problems.
- Sometimes the lowest  $K$  that has X-validation identifies is less than what we thought. Though this is possible (see previous power figure), it doesn't mean we have objective evidence other than the  $K$  it found.
- Sometimes we get greater  $K$  than we expect or can explain. In such situations it might be better to move to a supervised learning version (also available in ADMIXTURE).

# Local vs Global Ancestry

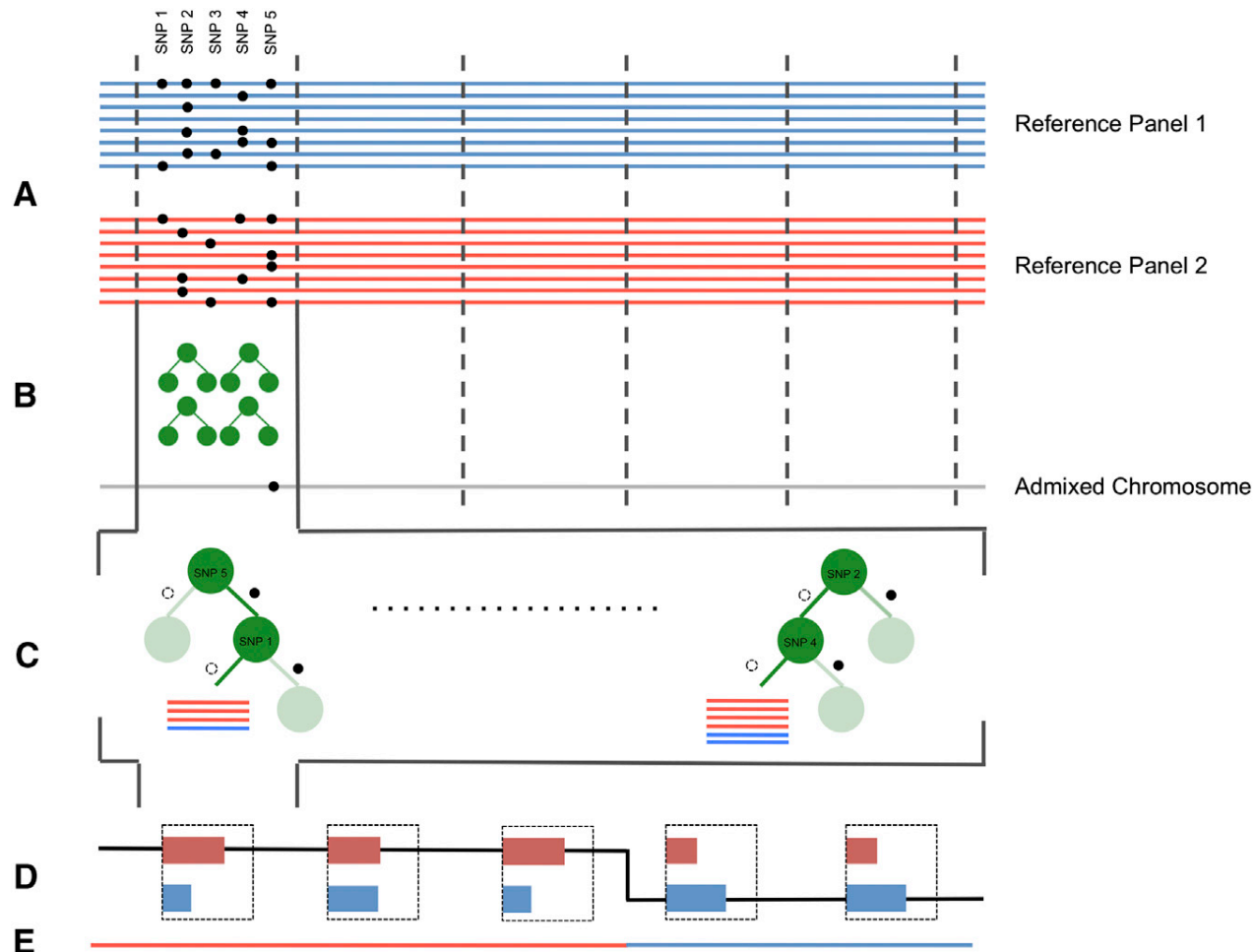


Gravel et al. (2013) Genetics

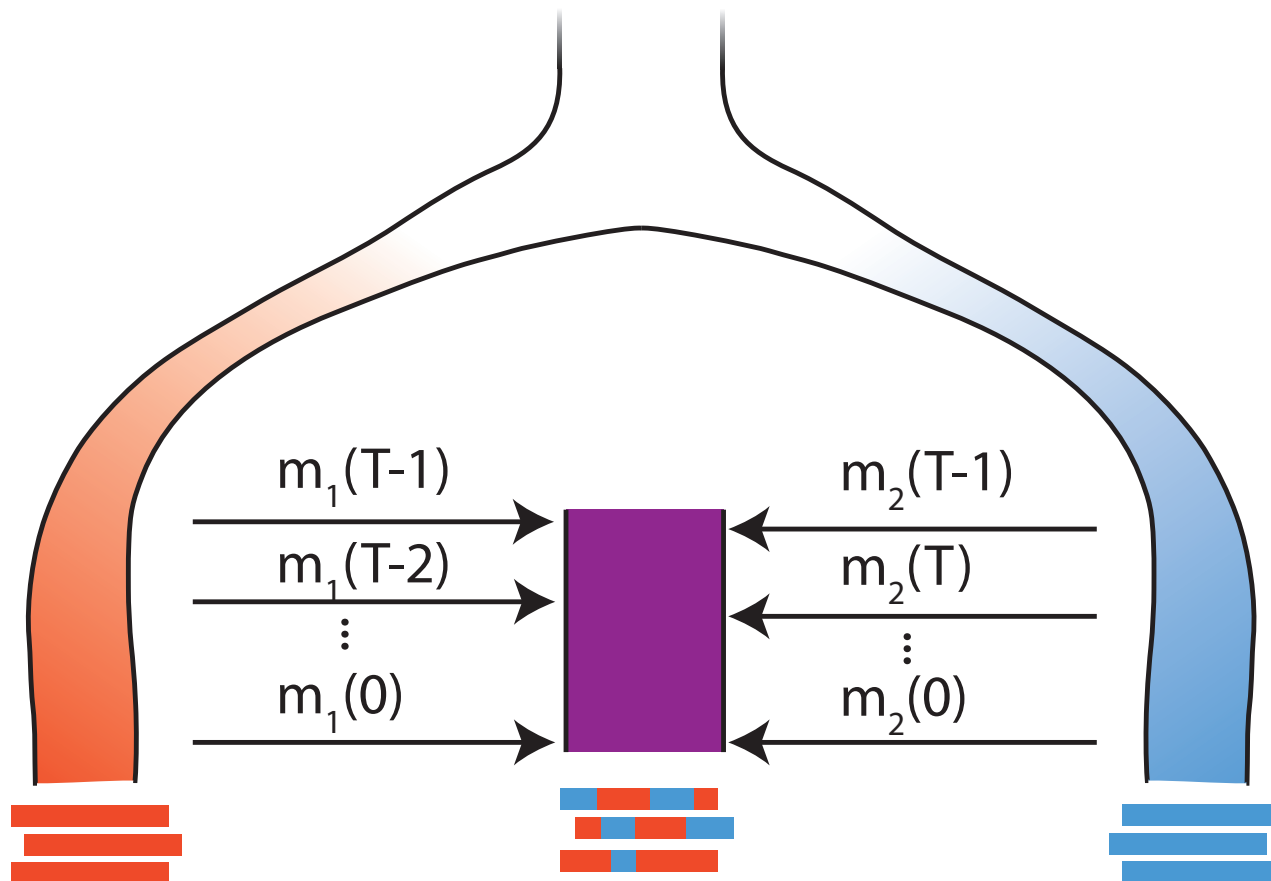


Mathias et al. (2016) Nat. Comm.

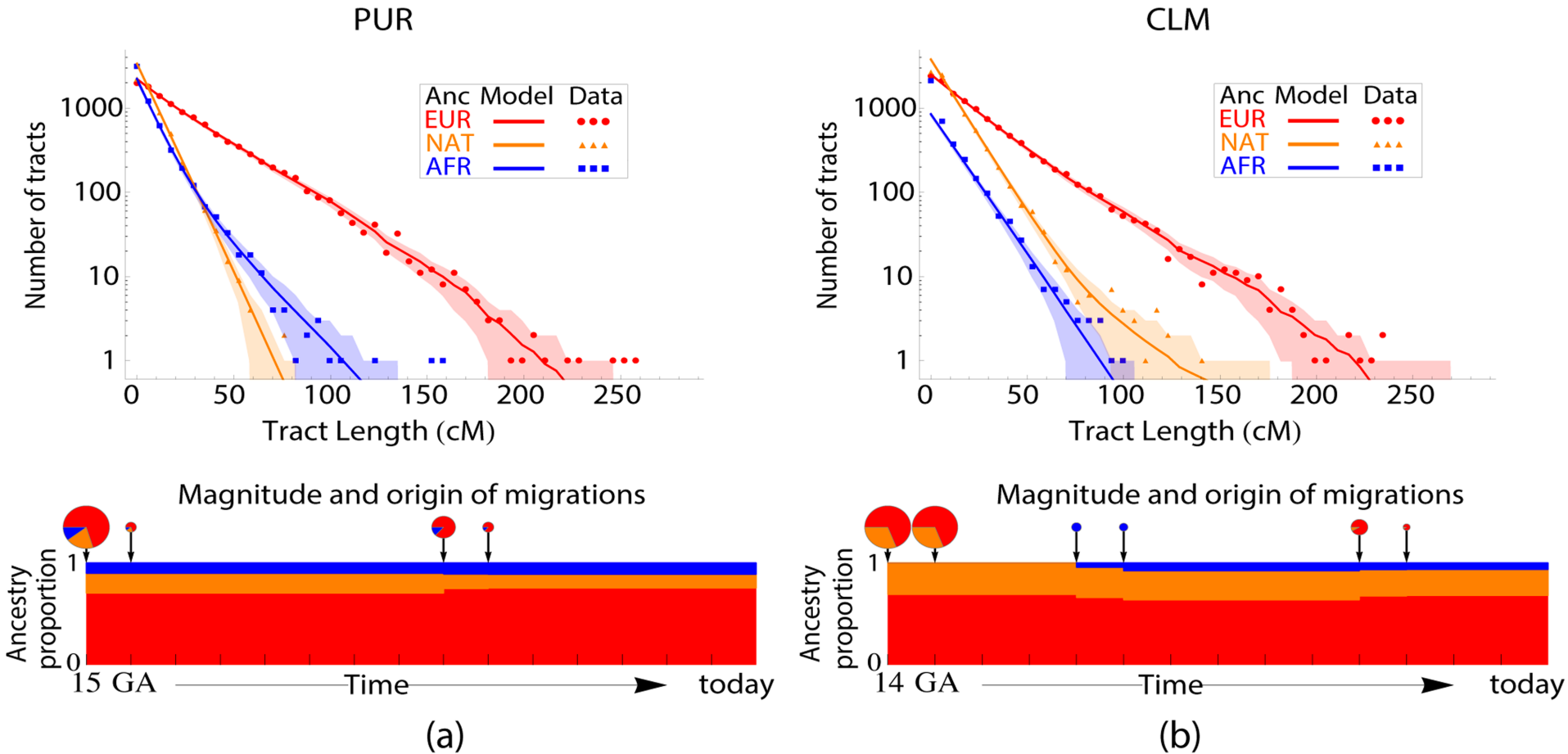
# Local ancestry calling: RFMix as an example



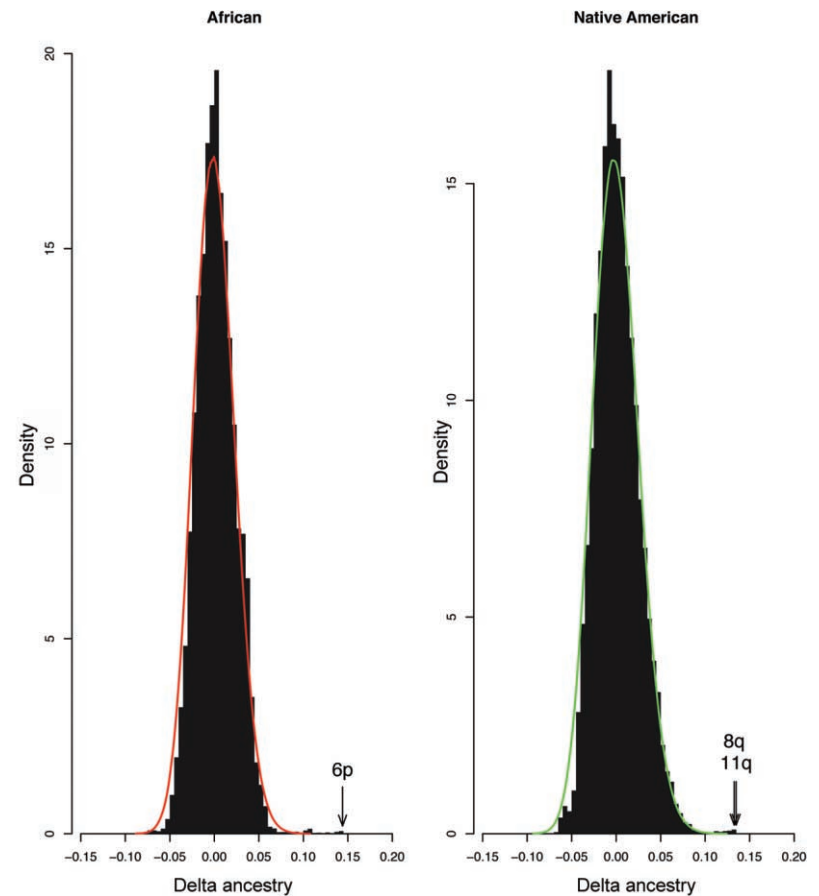
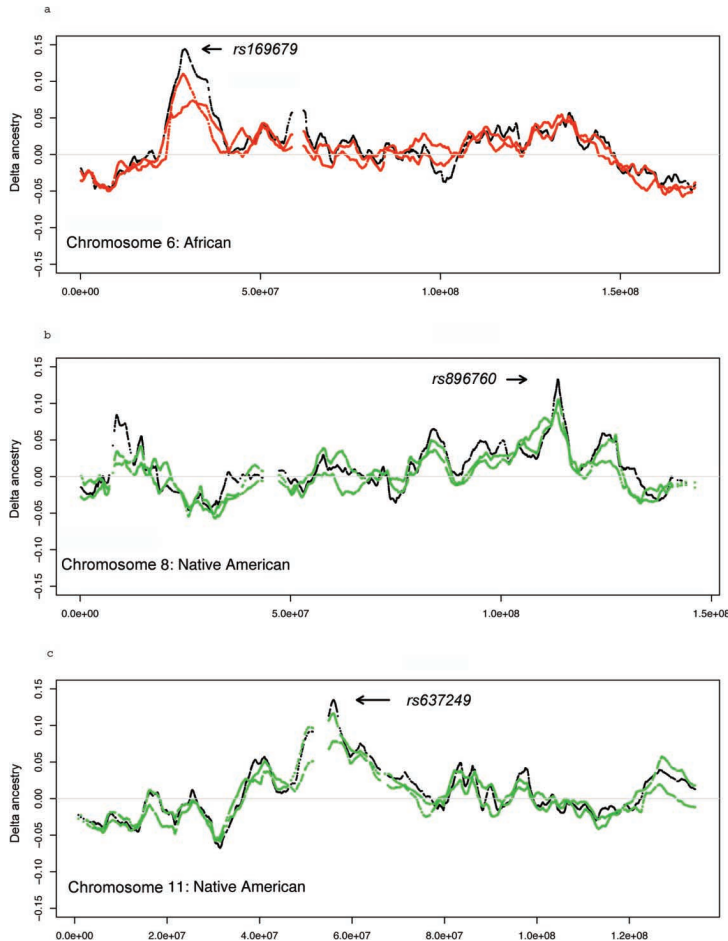
# Demographic modeling with local ancestry



# Demographic modeling with local ancestry

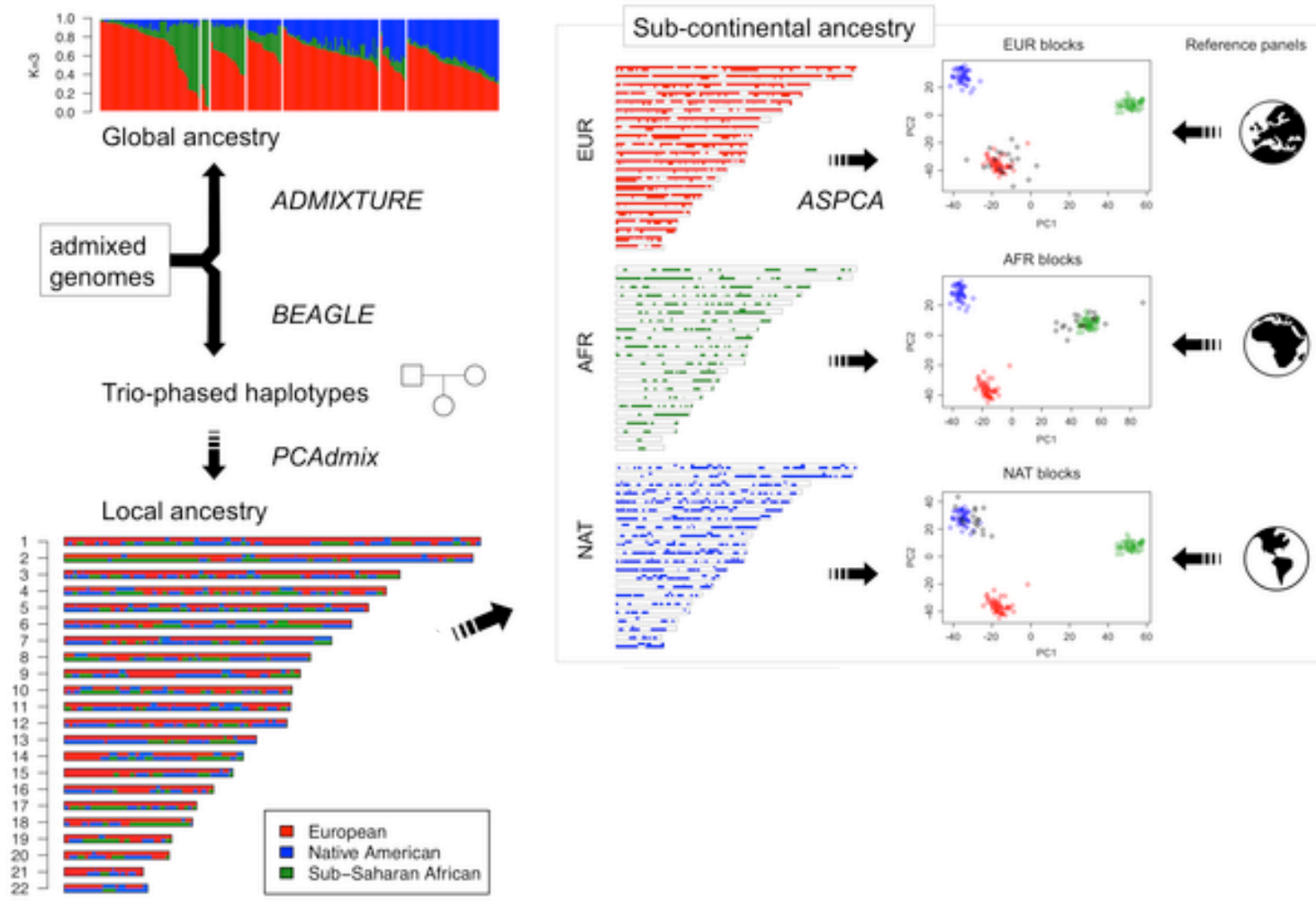


# Recent selection by looking for local ancestry biases



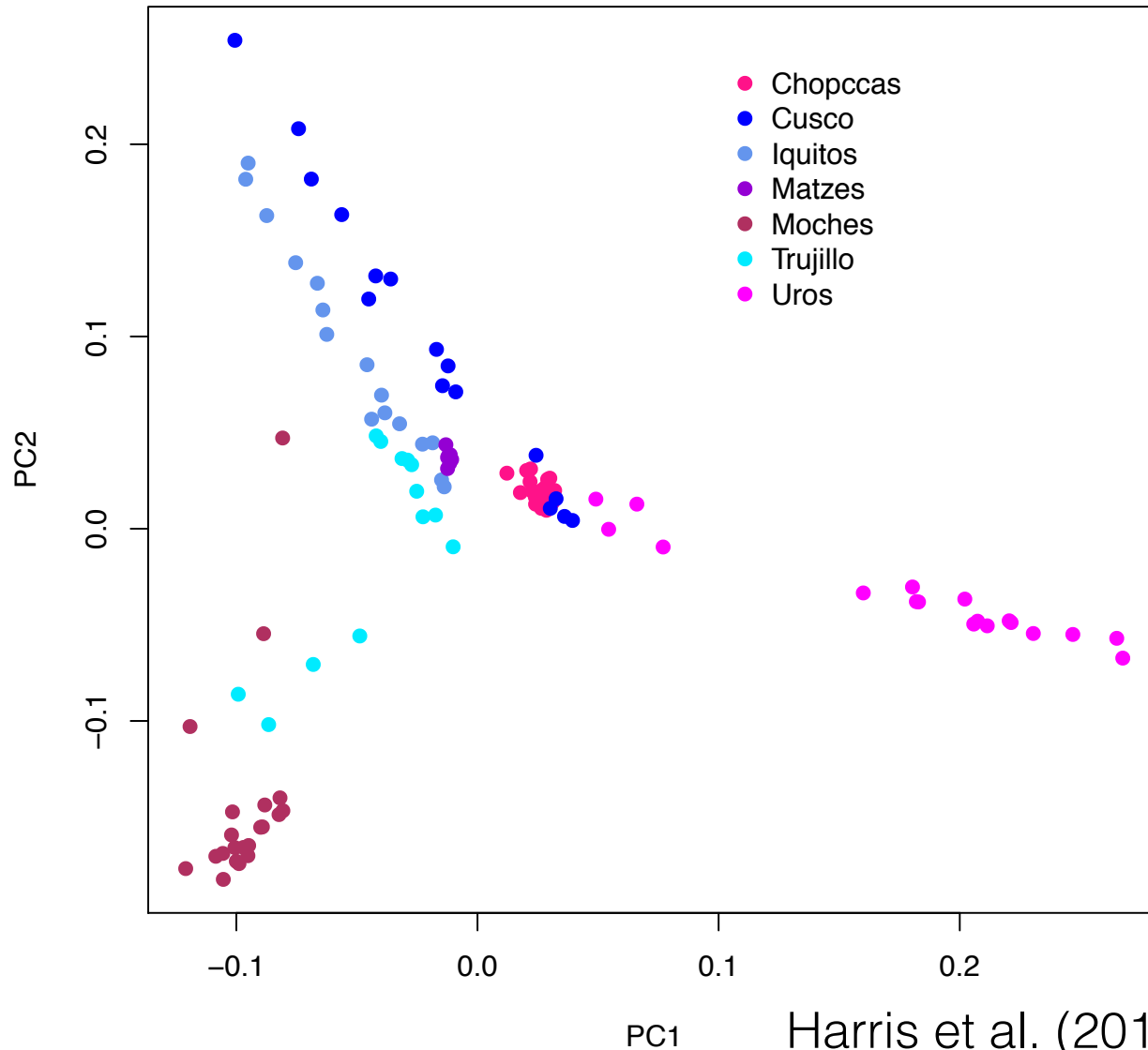
Tang et al. (2007) AJHG  
Though see Bhatia et al. (2014) AJHG

# Combining Local Ancestry and PCA to give Ancestry Specific PCA (or ASPCA)



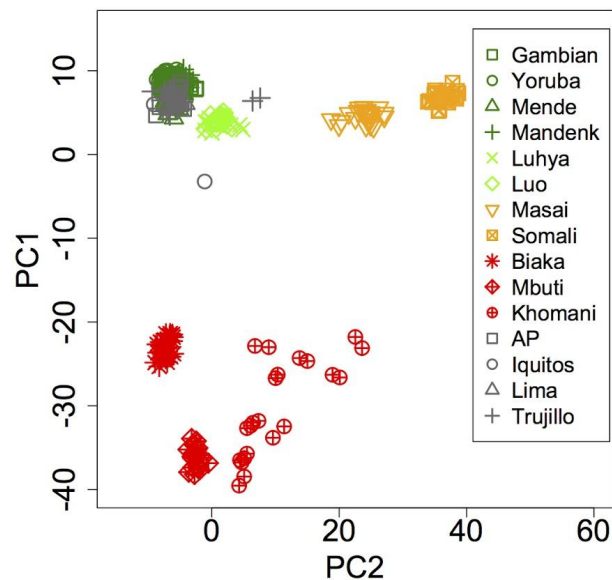
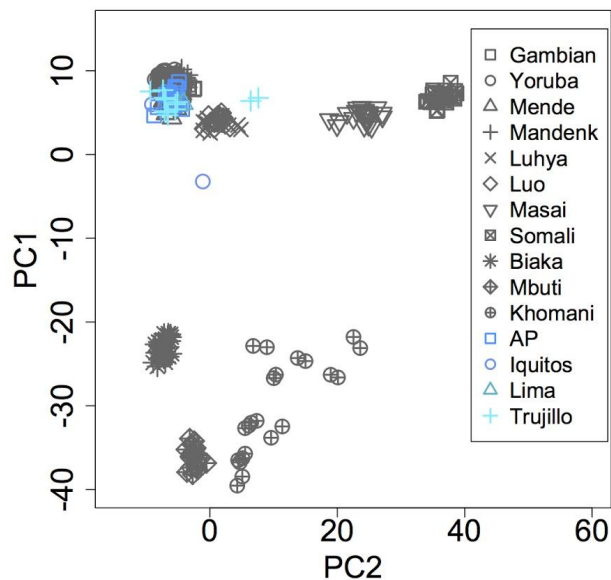
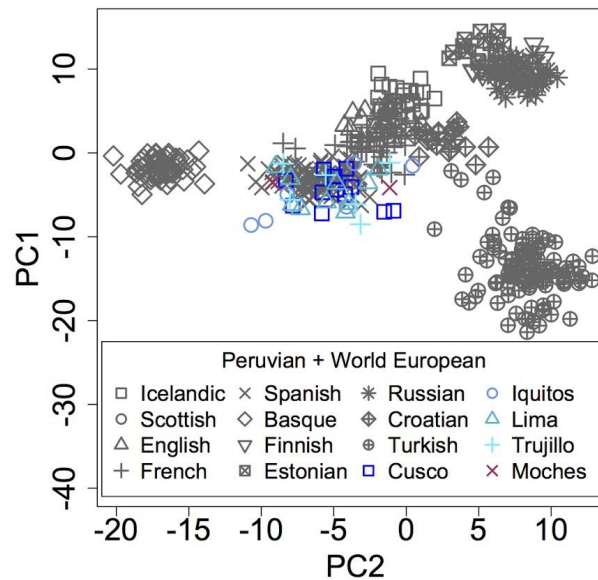
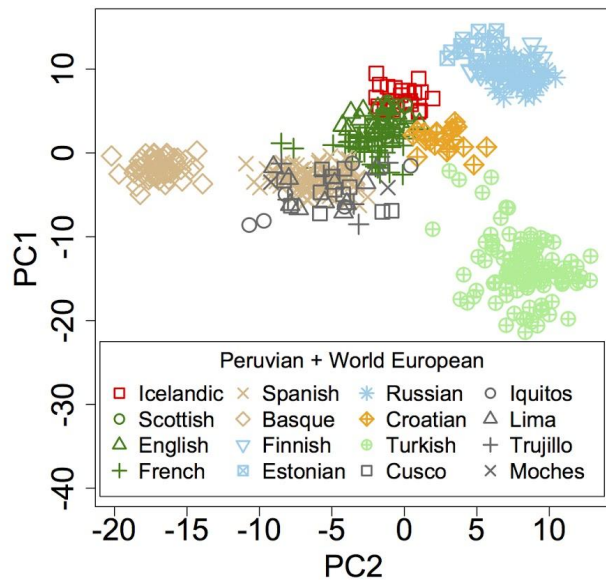


# Peruvian population structure with PCA



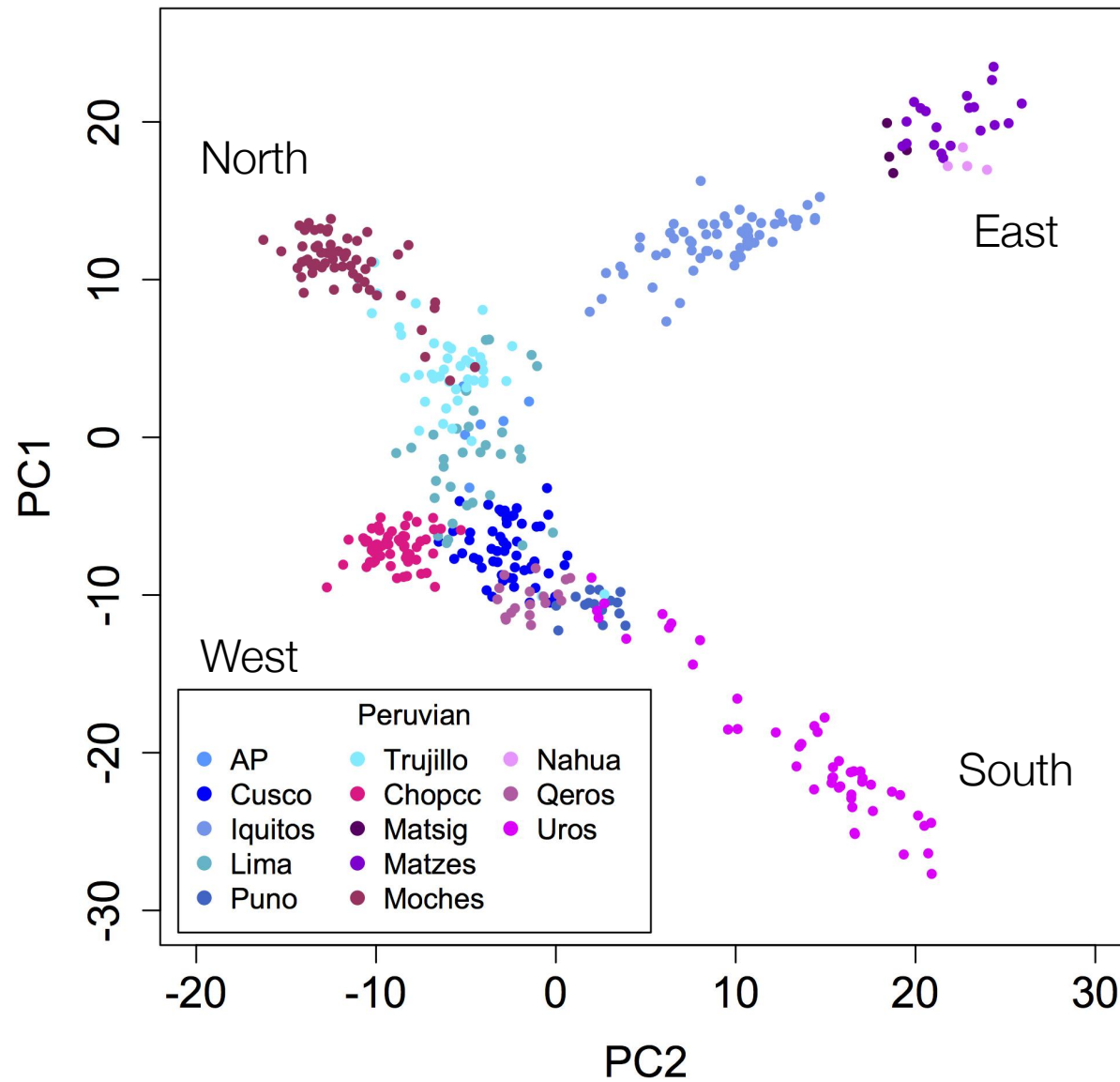
Harris et al. (2018) PNAS

# Ancestry specific PCA: Europe and Africa



Harris et al.  
(2018) PNAS

# Peruvian population structure using Ancestry Specific PCA



Harris et al.  
(2018) PNAS

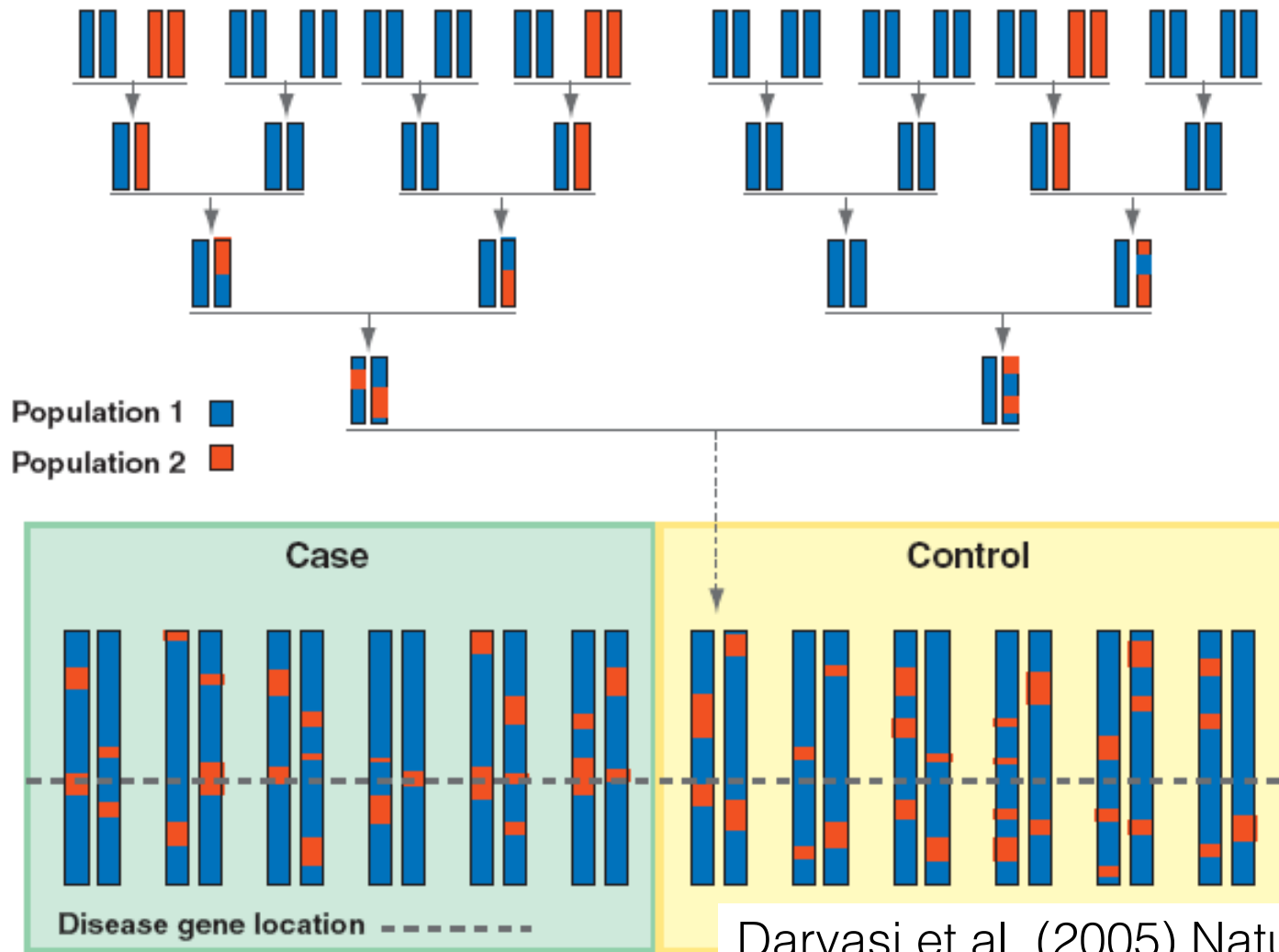
# Admixture is not just a nuisance for association

- Differences in genetic architecture are not just nuisance values that need to be 'adjusted' for in association models.
  - Extension Studies
  - Admixture Mapping

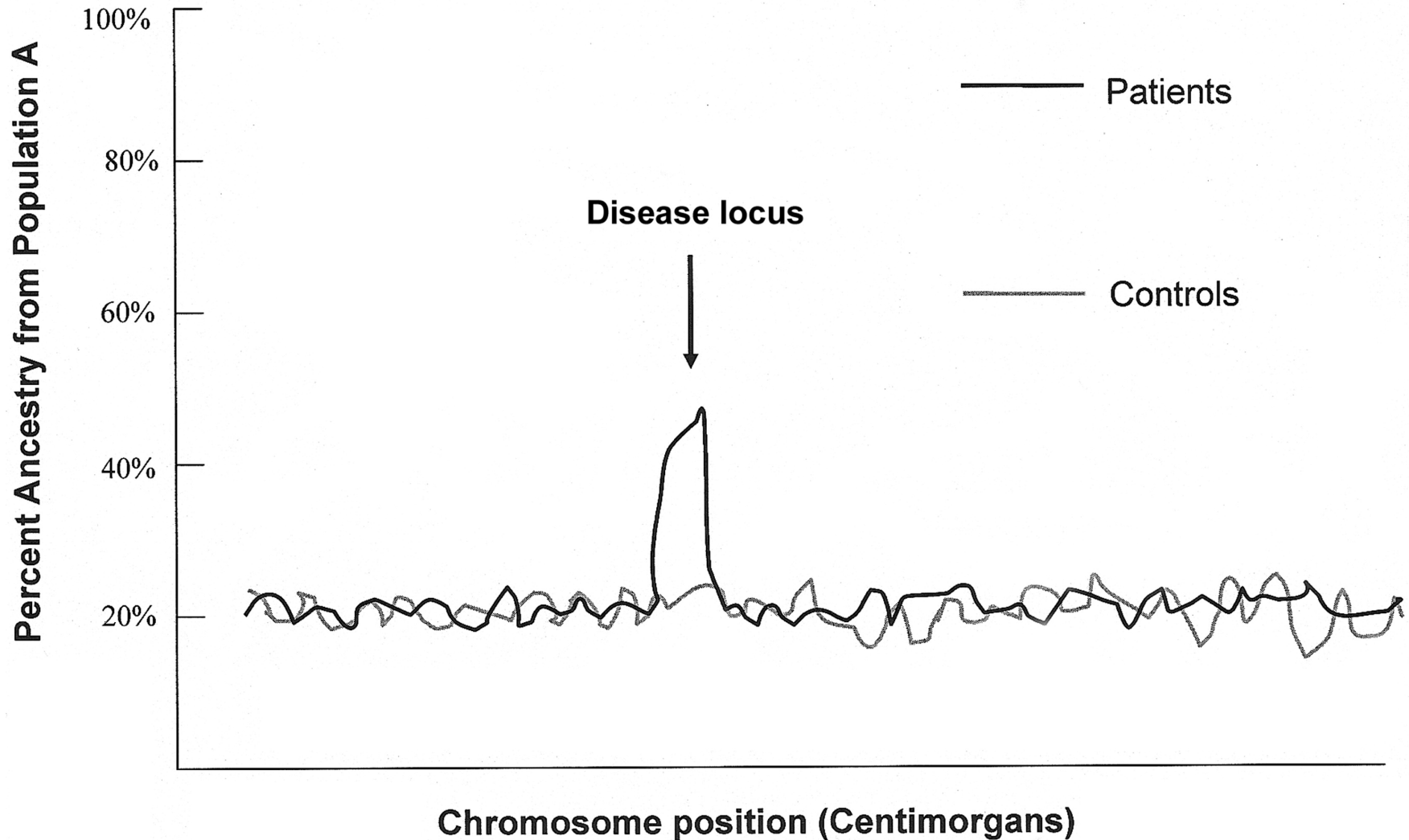
# Extension Studies

- Extension of findings to other ancestries is important to:
  - Determine association's potential public health impact
  - Provide additional evidence supporting association
  - Useful in fine-mapping an association signal
  - Finding risk variation in non-homogenous populations (like African Americans)

# Admixture mapping - Concept



# Example of an Admixture scan



# Concluding Summary

- PCA and Admixture analyses can summarize the ancestry found across the entire genome
- Local ancestry refines this inference to genomic segments with broad applications including demographic modeling and association analyses.