Lecture 2: Descriptive statistics, normalizations & testing

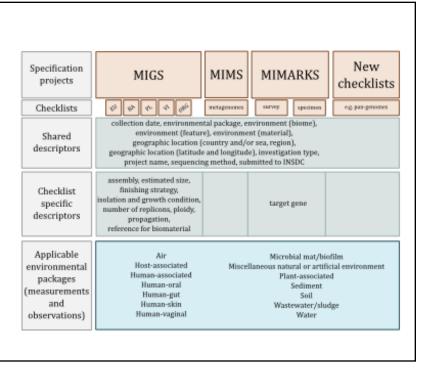
What do we need to know about a microbiome to understand it?

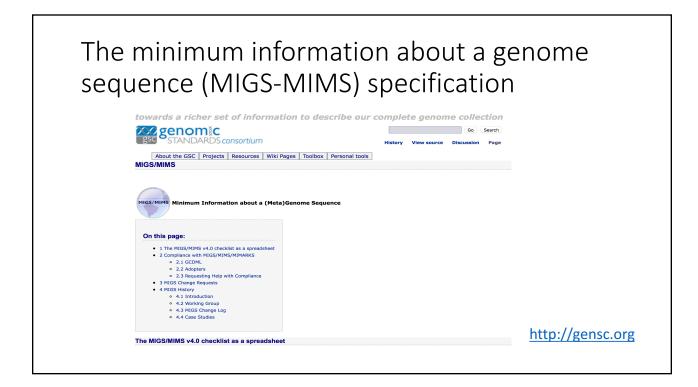
Scope-General	Scope-Specific	Description
	Reporting (Minimum information)	Documentation for publication or data deposition
Experiment description	Data exchange & modeling	Communication between organizations and tools
	Terminology	Ontologies and CV's to describe experiments or data
Experiment	Physical standards	Reference materials, spike-in controls
execution	Data analysis &	Analyze, compare, QA/QC experimental
	quality metrics	results

Acronym	Full name	Domain	Organization
	Core Information for Metabolomics		
CIMR	Reporting	Metabolomics	MSI
	Minimum Information about a		
MIAME	Microarray Experiment	Transcriptomics	MGED
	Minimum Information about a		
MIAPE	Proteomics Experiment	Proteomics	HUPO-PSI
	Minimum Information about a		
AIGS-MIMS	Genome/Metagenome Sequence	Genomics	GSC
	Minimum Information about a		
MIMIx	Molecular Interaction eXperiment	Proteomics	HUPO-PSI
	Minimal Metagenome Sequence		
MINIMESS	Analysis Standard	Metagenomics	GSC
	Minimum Information about a	Genomics, Transcriptomics	
	high-throughput Nucleotide	(UHTS)	
MINSEQE	Sequencing Experiment		MGED
	Minimum Information Specification		
	For In Situ Hybridization and		
	Immunohistochemistry		
AISFISHIE	Experiments	Transcriptomics	MGED

MIxS

- The GSC family of minimum information standards (checklists) – Minimum Information about any (x) Sequence (MIxS)
- MIGS genomes
- MIMS metagenomes
- MIMARKS marker genes
- 15 additional environmental package

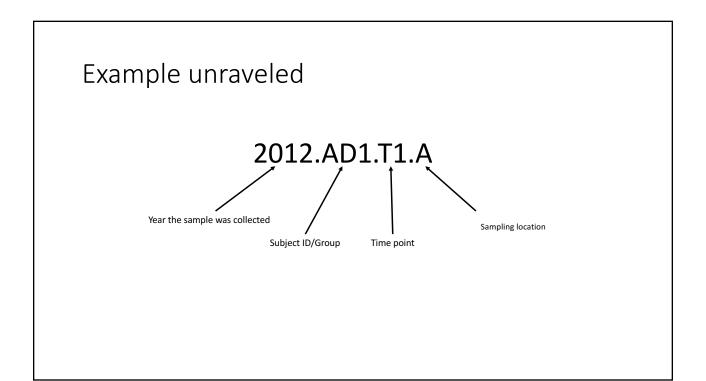




Sample Data

Example

2012.AD1.T1.A	2012.AD03.B.T1	2012.CO1.T2.A	2012.CO04.T1.B
2012.AD1.T1.B	2012.AD03.C.T1	2012.CO1.T2.B	2012.CO04.T1.C
2012.AD1.T1.C	2012.AD03.D.T1	2012.CO1.T2.C	2012.CO04.T1.D
2012.AD.T1.D	2012.AD03.A.T2	2012.CO1.T2.D	2012.CO04.T2.A
2012.AD1.T2.A	2012.AD03.B.T2	2012.CO02.T1.A	2012.CO04.T2.B
2012.AD1.T2.B	2012.AD03.C.T2	2012.CO02.T1.B	2012.CO04.T2.C
2012.AD1.T2.C	2012.AD03.D.T2	2012.CO02.T1.C	2012.CO04.T2.D
2012.AD1.T2.D	2012.AD05.T1.A	2012.CO02.T1.D	2012.CO05.T1.A
2012.AD2.T1.A	2012.AD05.T1.B	2012.CO3.T1.A	2012.CO05.T1.D
2012.AD2.T1.B	2012.AD05.T1.C	2012.CO3.T1.B	
2012.AD2.T1.C	2012.AD05.T1.D	2012.CO3.T1.C	
2012.AD2.T1.D	2012.AD04.A.T1	2012.CO3.T1.D	
2012.AD2.T2.A	2012.AD04.B.T1	2012.CO3.T2.A	
2012.AD2.T2.B	2012.CO1.T1.A	2012.CO3.T2.B	
2012.AD2.T2.C	2012.CO1.T1.B	2012.CO3.T2.C	
2012.AD2.T2.D	2012.CO1.T1.C	2012.CO3.T2.D	
2012.AD03.A.T1	2012.CO1.T1.D	2012.CO04.T1.A	



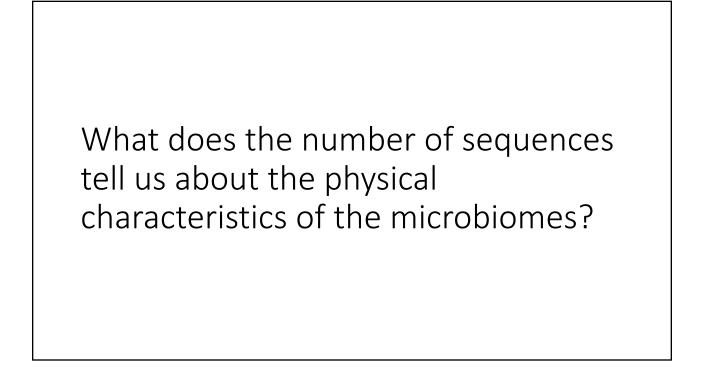
			1									1
	BarcodeSequ LinkerPrimer Group	sample_well			BC_name	Time.point Gender				Worst.affect		
2012.AD1.T1.A	TACCGCTTCT CCGGACTAC AD	p01.A1	AD1	AD	806rcbc96	1 M	A: L popliteal	3.45	6	1	0	W
2012.AD1.T1.B	TGTGCGATA, CCGGACTAC AD	p01.A2	AD1	AD	806rcbc97	1 M	B: L Back	3.45	2	0	0	W
2012.AD1.T1.C	GATTATCGA CCGGACTACIAD	p01.A3	AD1	AD	806rcbc98	1 M	C: R lateral thigh	3.45	3	0	0	w
2012.AD.T1.D	GCCTAGCCC, CCGGACTAC AD	p01.A4	AD1	AD	806rcbc99	1 M	D: R forearm	3.45	0	0	1	W
2012.CO1.T1.A	GAGAGCAAC CCGGACTACI Control	p01.B5	CO1	Control	806rcbc112	1 F	A: R antecubital	30	0			
2012.CO1.T1.B	TACTCGGGA CCGGACTAC Control	p01.B6	CO1	Control	806rcbc113	1 F	B: L popliteal	30	0			
2012.CO1.T1.C	CGTGCTTAG CCGGACTAC Control	p01.B7	CO1	Control	806rcbc114	1 F	C: L abdomen	30	0			
2012.CO1.T1.D	TACCGAAGG CCGGACTACI Control	p01.B8	CO1	Control	806rcbc115	1 F	D: R cheek	30	0			
2012.CO1.T2.A	CACTCATCAT CCGGACTAC Control	p01.B8	CO1	Control	806rcbc116	2 F	A: R antecubital	30	0			
2012.CO1.T2.B	GTATTTCGG CCGGACTAC Control	p01.B10	CO1	Control	806rcbc117	2 F	B: L popliteal	30	0			
2012.CO1.T2.C	TATCTATCCT CCGGACTAC Control	p01.B11	CO1	Control	806rcbc118	2 F	C: L abdomen	30	0			
2012.CO1.T2.D	TTGCCAAGA CCGGACTAC Control	p01.B12	CO1	Control	806rcbc119	2 F	D: R cheek	30	0			
2012.CO02.T1.A	AGTAGCGGA CCGGACTAC Control	p01.C1	CO2	Control	806rcbc120	1 M	A: face	36	0			
	GCAATTAGG CCGGACTAC Control	p01.C2	CO2	A	806rcbc121	1 M	B: L forearm	36	0			1

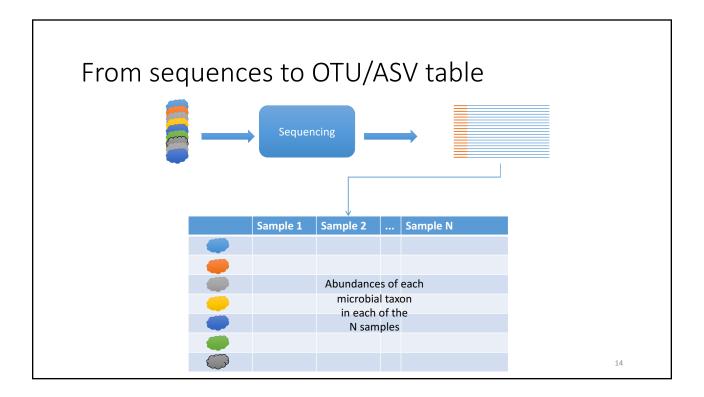
Data dictionary

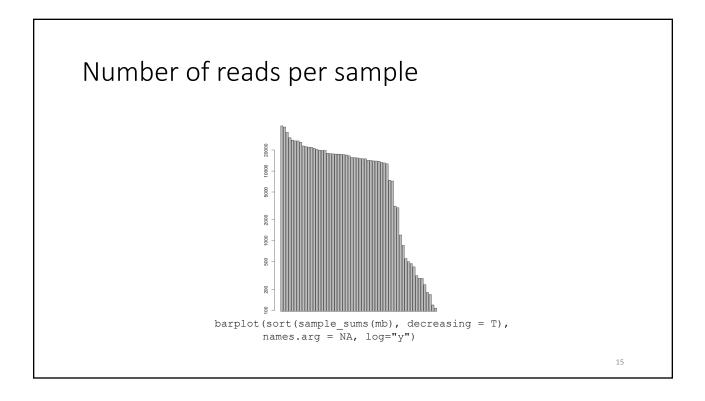
- A data dictionary is a "centralized repository of information about data such as meaning, relationships to other data, origin, usage, and format" (*IBM Dictionary of Computing*)
- Typical elements of a research data dictionary
 - Variable name
 - Measurement unit
 - Allowed values
 - Description
 - Example

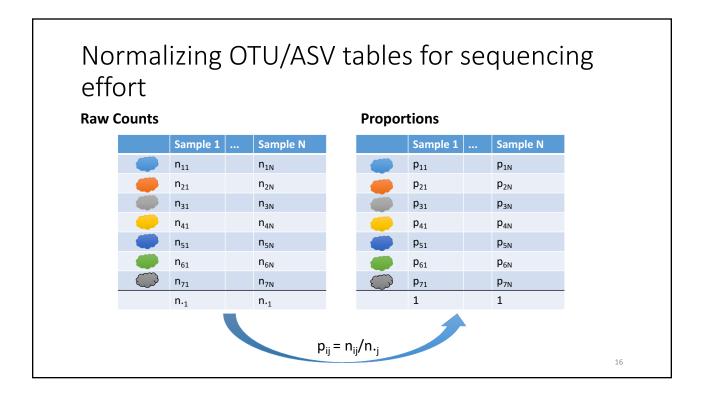
Example data dictionary

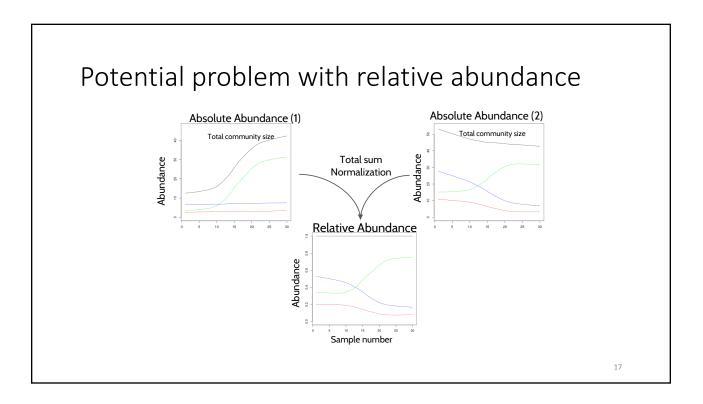
Variable	Description	Values	Example
SampleID	Unique ID number for each sample	Numeric	156
		F = female;	
gender	Gender of subject	M = male	F
age	Age of subject in years	Numeric	10
		Oral = mouth sample;	
		Fecal = fecal sample;	
bodysite	Body site of sampling	Skin = skin sample from left arm	Oral
weight	Weight of subject in kg	Numeric	35.7
height	Height of subject in cm	Numeric	116
BMI	Body mass index (BMI) of subject	Numeric	26.5

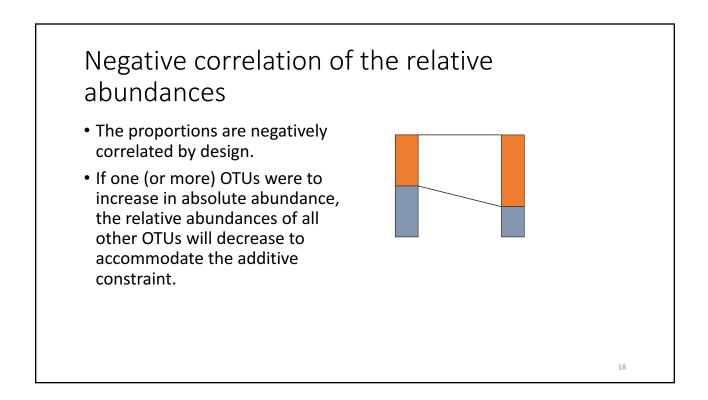


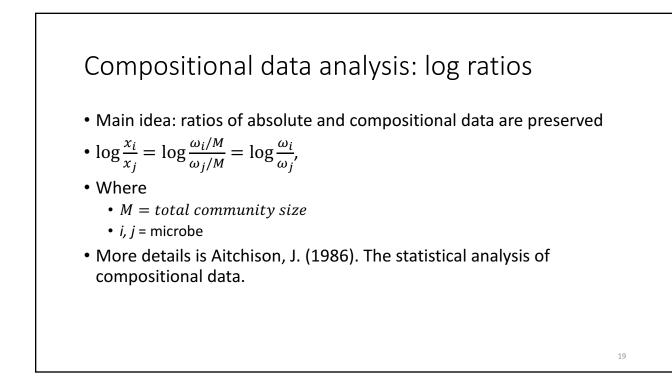


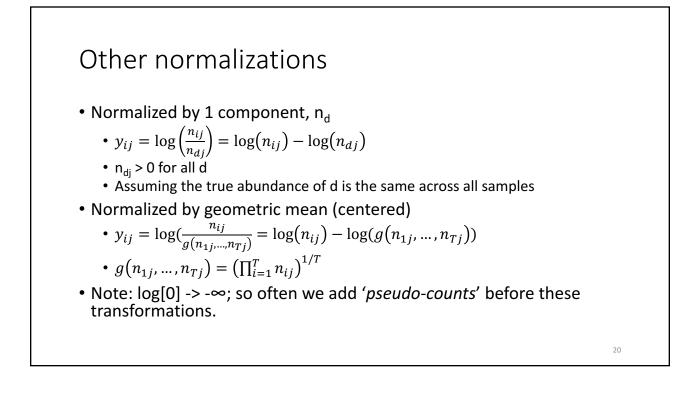


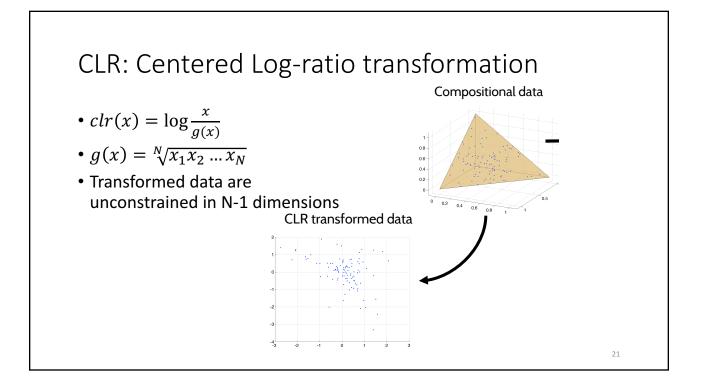


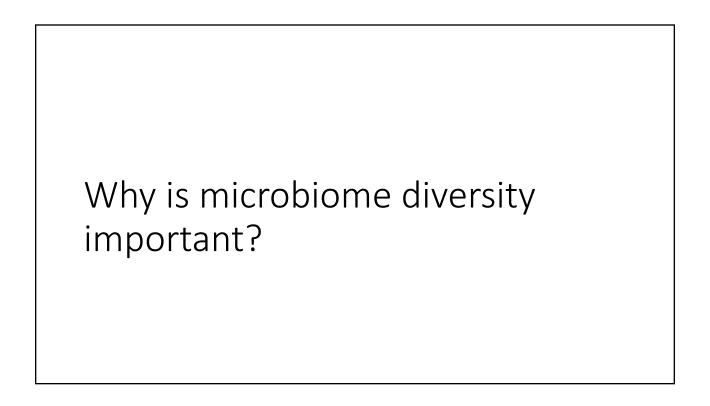


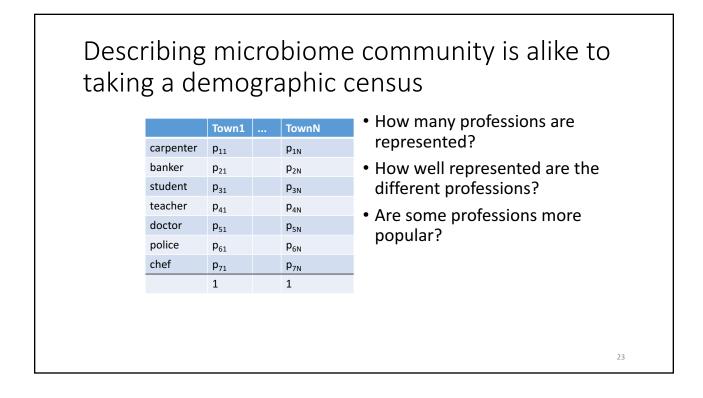


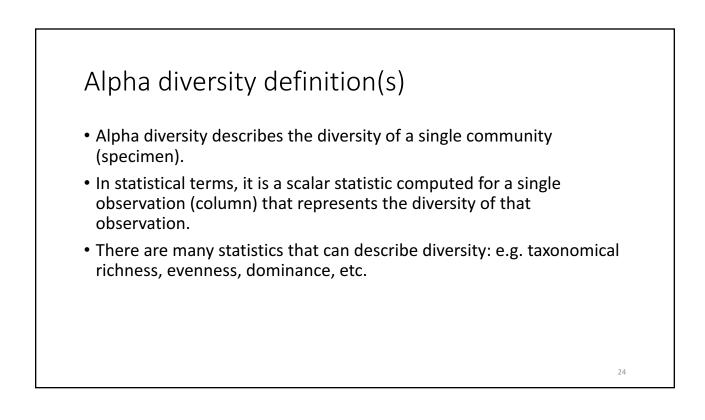


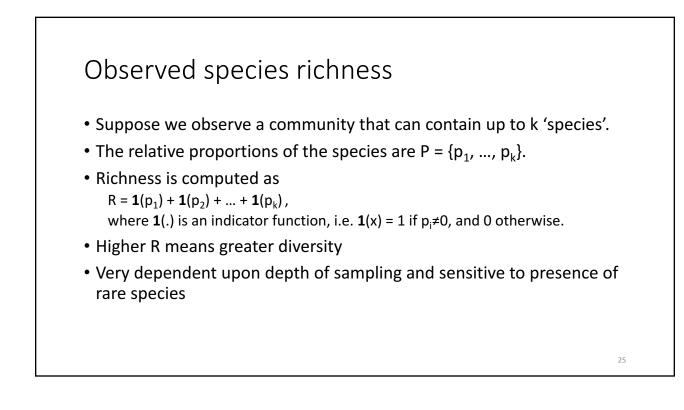






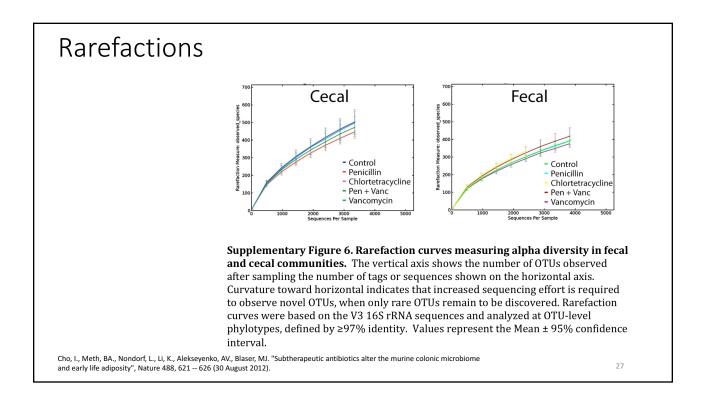


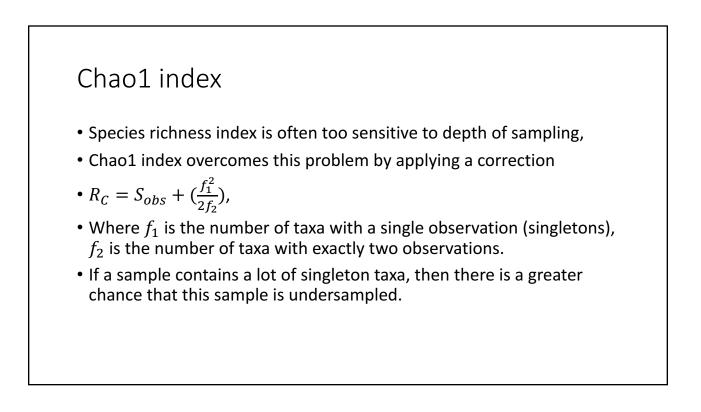




Rarefaction curves

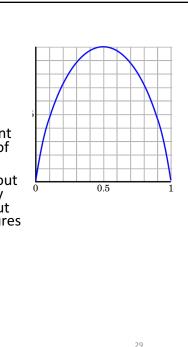
- Note: rarefication as a means for normalization is from statistical standpoint a bad idea. Don't throw away information!
- Rarefaction curves are not the same!
- Useful to assess sensitivity of sample size to observed alpha-diversity estimates.
- Idea:
 - Let N_1 , ..., N_K be a set of numbers $N_i < N_{i+1}$;
 - Let $n^\prime_{\ ij}{}^{(k)}$ be abundance of taxon i in sample j subsampled to N_k total counts per sample;
 - Estimate average alpha diversity for each N_k over a several repeated subsamplings;
 - Plot the average alpha diversity as a function of sample size.

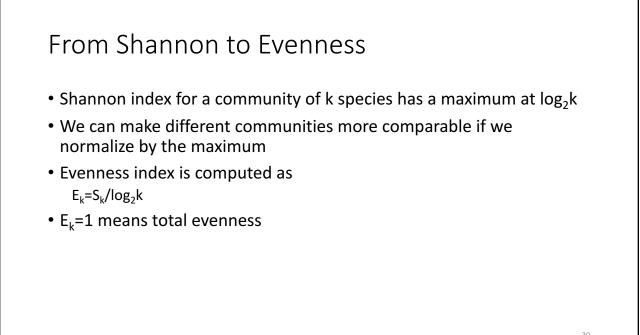




Shannon index

- Suppose we observe a community that can contain up to k 'species'.
- The relative proportions of the species are P = {p₁, ..., p_k}.
- Shannon index is related to the notion of information content from information theory. It roughly represents the amount of information that is available for the distribution of P.
- When $p_i = p_j$, for all i and j, then we have no information about which species a random draw will result in. As the inequality becomes more pronounced, we gain more information about the possible outcome of the draw. The Shannon index captures this property of the distribution.
- Shannon index is computed as
 S_k= - p₁log₂p₁ - p₂log₂p₂ - ... - p_klog₂p_k
 Note as p_i → 0, log₂p_i → -∞, we therefore define p_ilog₂p_i = 0.
- Higher S_k means higher diversity

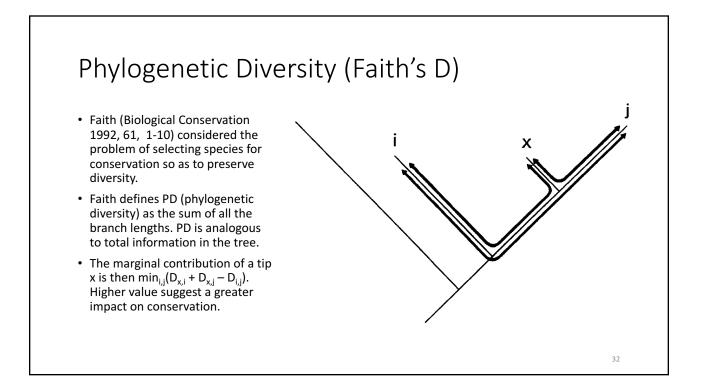


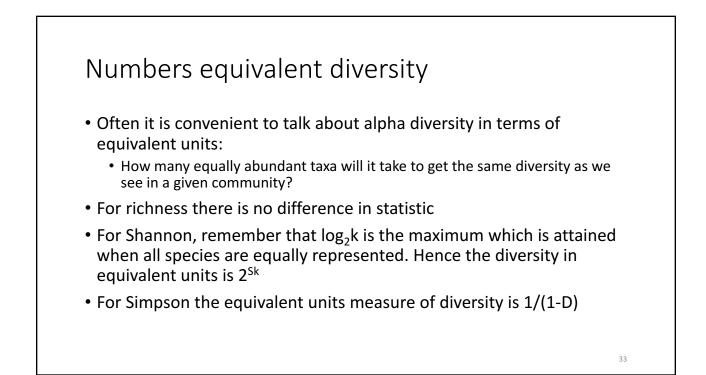


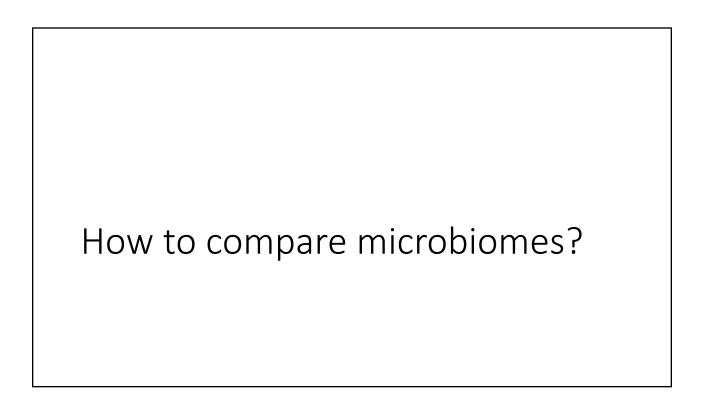
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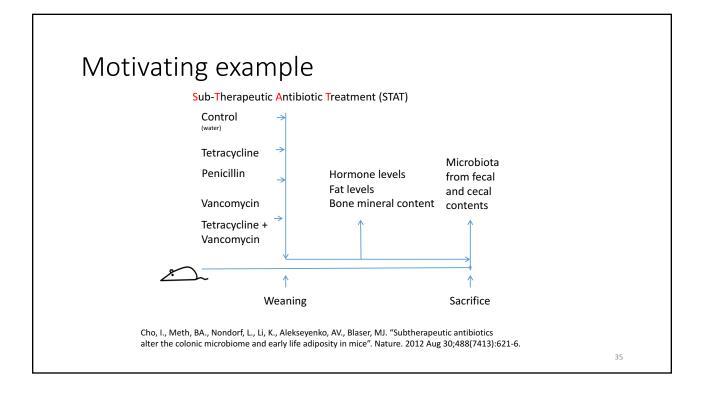
Simpson index

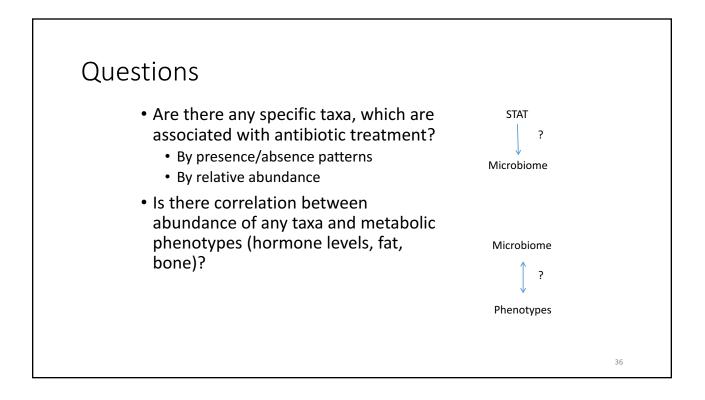
- Suppose we observe a community that can contain up to k 'species'.
- The relative proportions of the species are P = {p₁, ..., p_k}.
- Simpson index is the probability of resampling the same specie on two consecutive draws with replacement.
- Suppose on the first draw we picked specie i, this event has probability p_i, hence the probability of drawing that species twice is p_i*p_i.
- Simpson index is thus computed as $D=1-(p_1^2+p_2^2+...+p_k^2)$
- D = 0 means no diversity (1 species is completely dominant)
- D = 1 means complete diversity







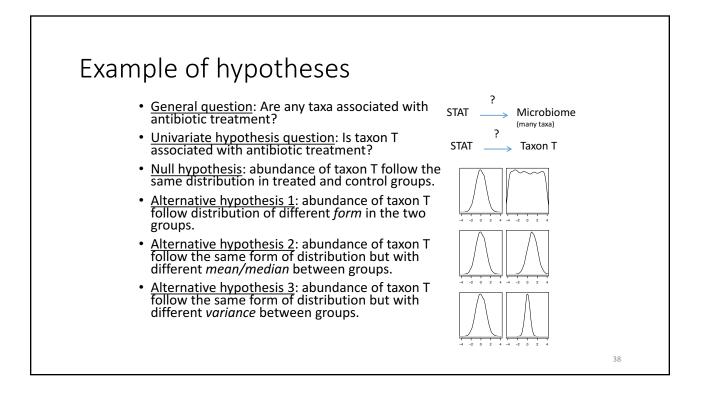




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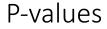
Hypotheses

- Are **precise** statements that are amenable to being proven false using data.
- *Null hypothesis*: a proposition that corresponds to default position. ("Nothing special is happening")
- Alternative hypothesis: a proposition that describes a non default outcome ("Something interesting is going on")
- The inference is obtained by rejecting the Null hypothesis. Null hypothesis can never be confirmed by the data, nor does it have to be!

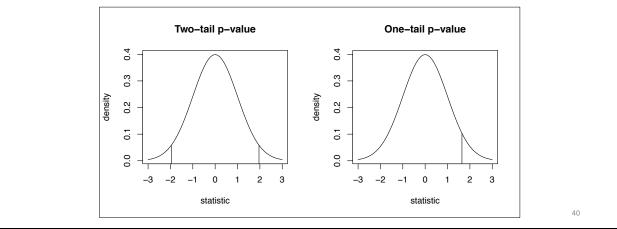


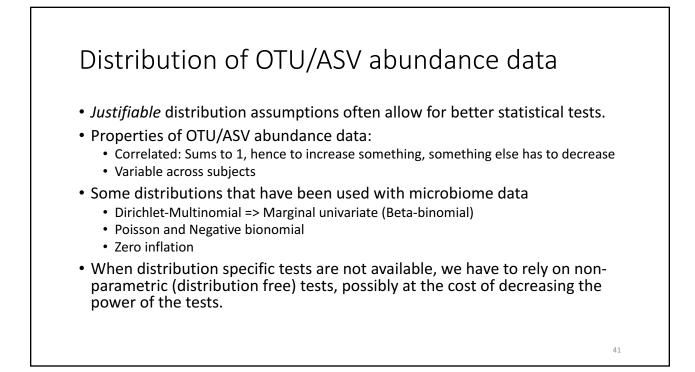
Flow of statistical inference under hypothesis testing

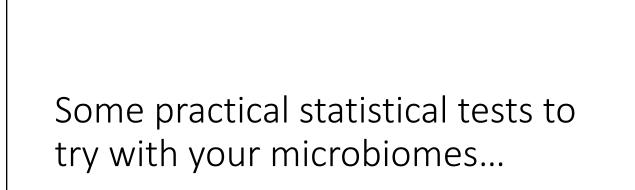
- Define a test statistic that evaluates evidence against the Null Hypothesis;
 - What is a good statistic to compare the averages of two samples: x1, ..., xN and y1, ..., yM? What is the null hypothesis here?
- Determine the distribution of the test statistic under the Null Hypothesis;
 - Options here:
 - Asymptotic properties of the statistic;
 - Monte Carlo simulations: bootstrap, permutation, ...
 - How would the distribution of statistic above look like under the Null?
- Calculate the test statistic value in the observed data;
- Compare the observed test statistic to the distribution of the statistic, when the null hypothesis is true.
 - If the probability of observing a statistic as extreme or more is small enough (P<0.05?), reject the null hypothesis.

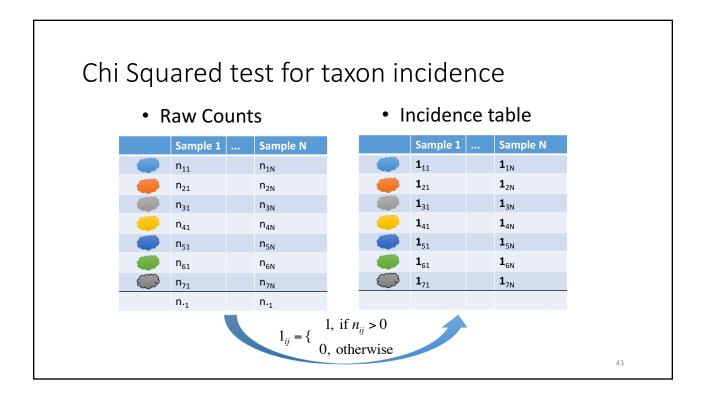


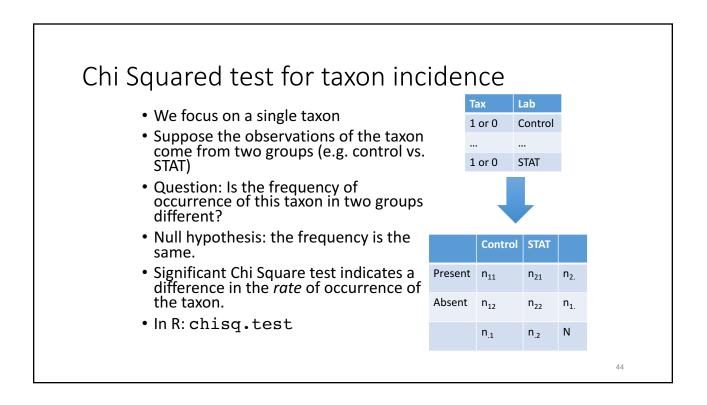
- If the Null Hypothesis was in fact true a *statistic,* used to perform the test, would follow a certain distribution: the *null distribution*.
- P-value is the tail probability under the null distribution.

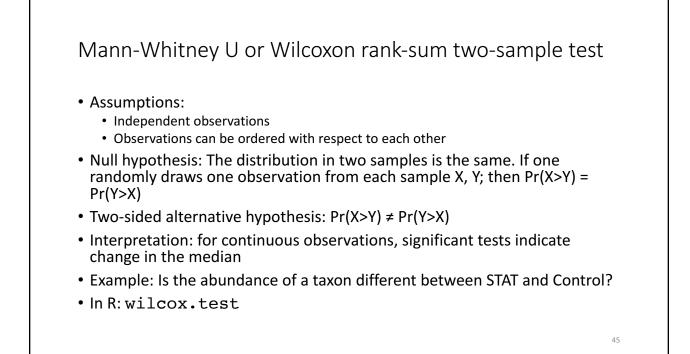












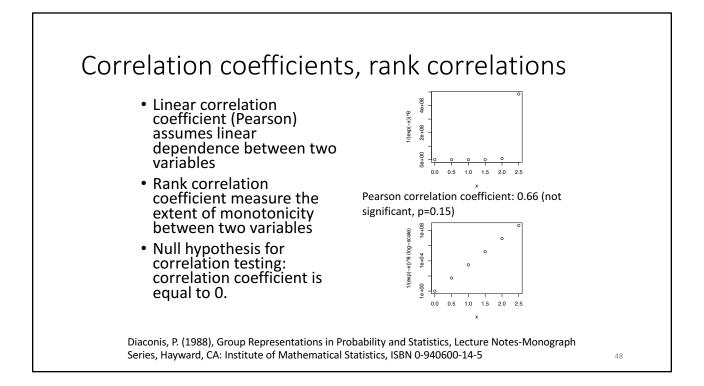
	tivity			
• Mann Whitney II statistic coloulation.	Sample 1 Sa	mple 2 F	anks 1 Ra	inks 2
 Mann-Whitney U-statistic calculation: Convert the observations to ranks 	0.135	2.680	8	1
	-0.907	1.078	18	2
 Compute the sum of ranks in each sample, R₁ and R₂ 	-0.801	0.080	16	9
• $U_1 = R_1 - n_1(n_1 + 1)/2$	0.452	0.493	6	5
• $U_2 = R_2 - n_2(n_2 + 1)/2$	-0.523	0.010	15	11
• $U = min(U_1, U_2)$	0.075	-0.322	10	13
• One can show that U statistic is	1.038	-0.370	3	14
equivalent to AUC. AUC = $U/(n_1 n_2)$	-1.140	0.633	19	4
 AUC, area under receiver operator 	-2.308	-0.020	20	12
characteristic (ROC) curve, measures how	-0.808	0.368	17	7
well we can distinguish one sample from	Rank Sums		132	78
another. AUC = 0.5 means predictivity no	U		77	23
better than random, AUC = 1.0 perfect	Us	statistic	23	
predictivity.	AL	IC	0.77	0.23

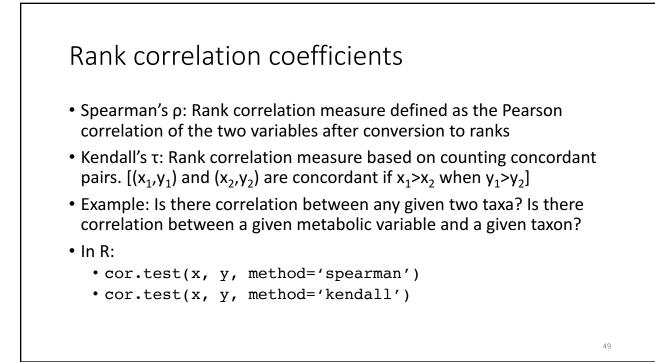
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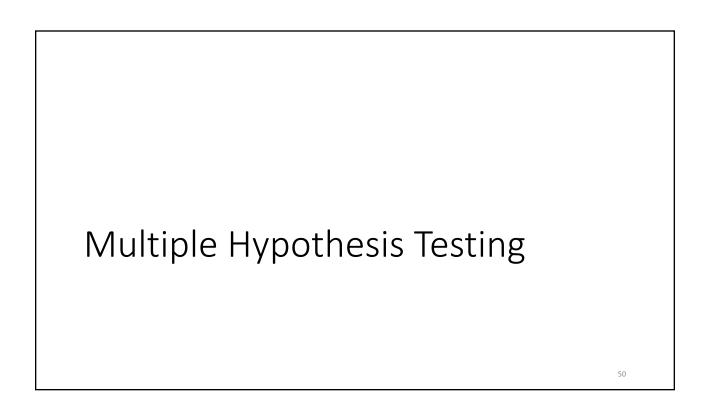
Kruskal-Wallis one-way analysis of variance (more than two samples/groups)

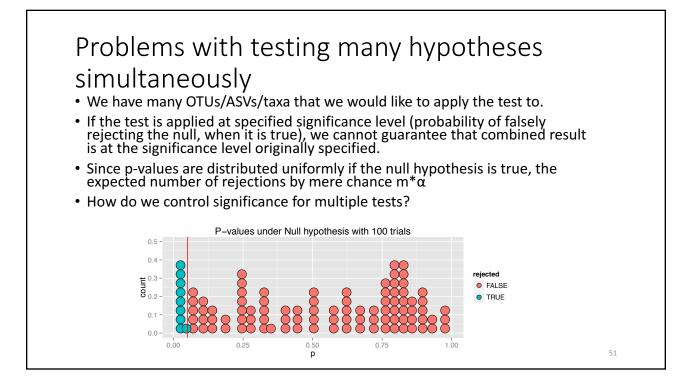
• Assumptions:

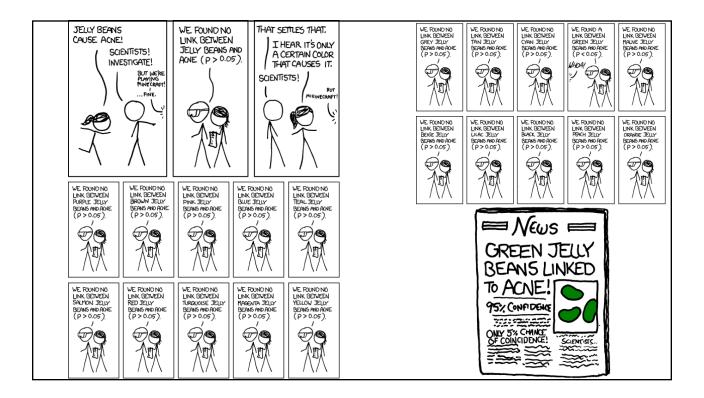
- Independent observations that follow distribution with the same shape and scale
- Observations can be ordered with respect to each other
- Null hypothesis: The location (median) of all the groups is the same.
- Alternative hypothesis: Location for at least one group is different from location of at least one other group
- Example: Is the abundance of a taxon different in STAT/control over 3 sampled time points?
- In R: kruskal.test











FWER: Family-wise error rate Total # not-• Suppose we perform m tests (e.g. rejected rejected m taxa are tested for association # true null U V m_0 with antibiotic treatment) hypotheses • The number of true null # non-true Т S null $m-m_0$ hypotheses is unknown m₀ hypotheses • V is false positive rate (Type I error) Total m-R R m • T is false negative rate (Type II error) FWER control methods adjust the • We observe R, but S, T, U, V are significance of each individual test to ensure overall significance at unobserved given α. • FWER = $Pr(V \ge 1)$ FWER result in more stringent tests. 53

