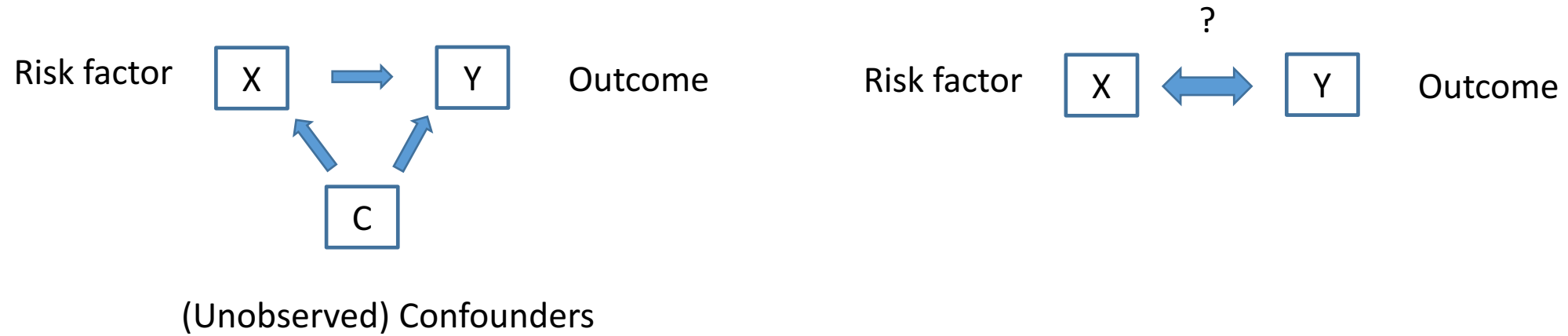
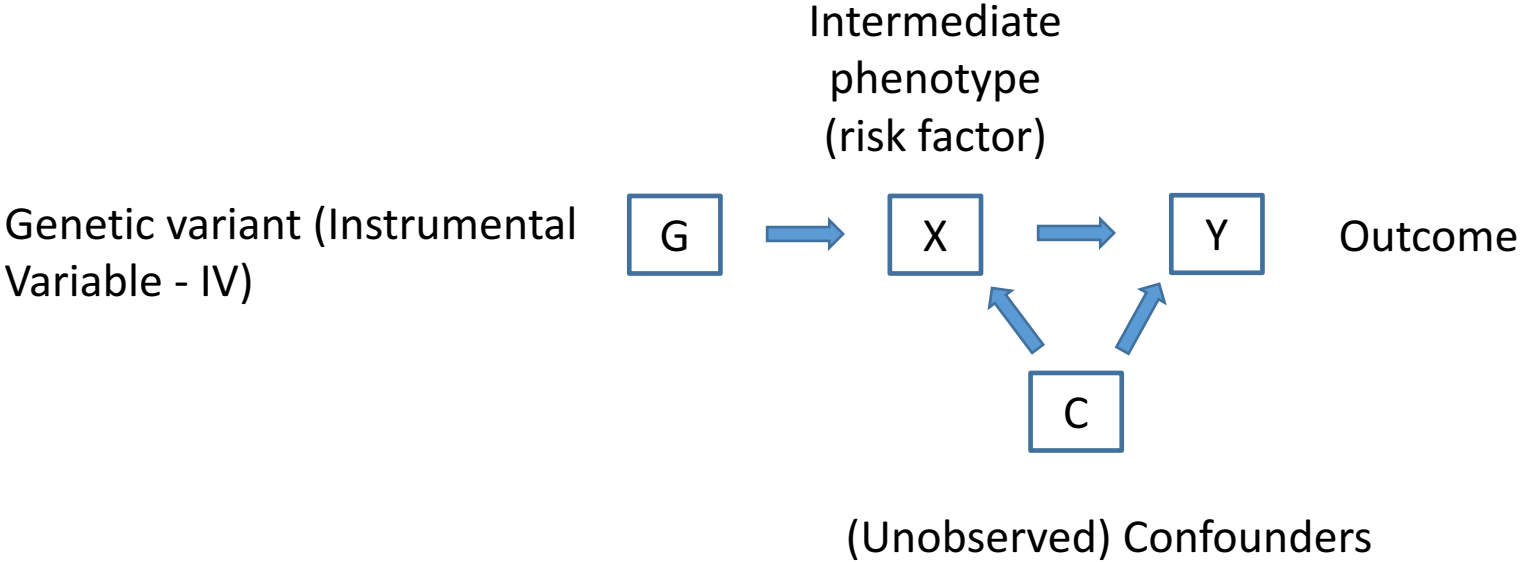


# Mendelian Randomization

# Drawback with observational studies



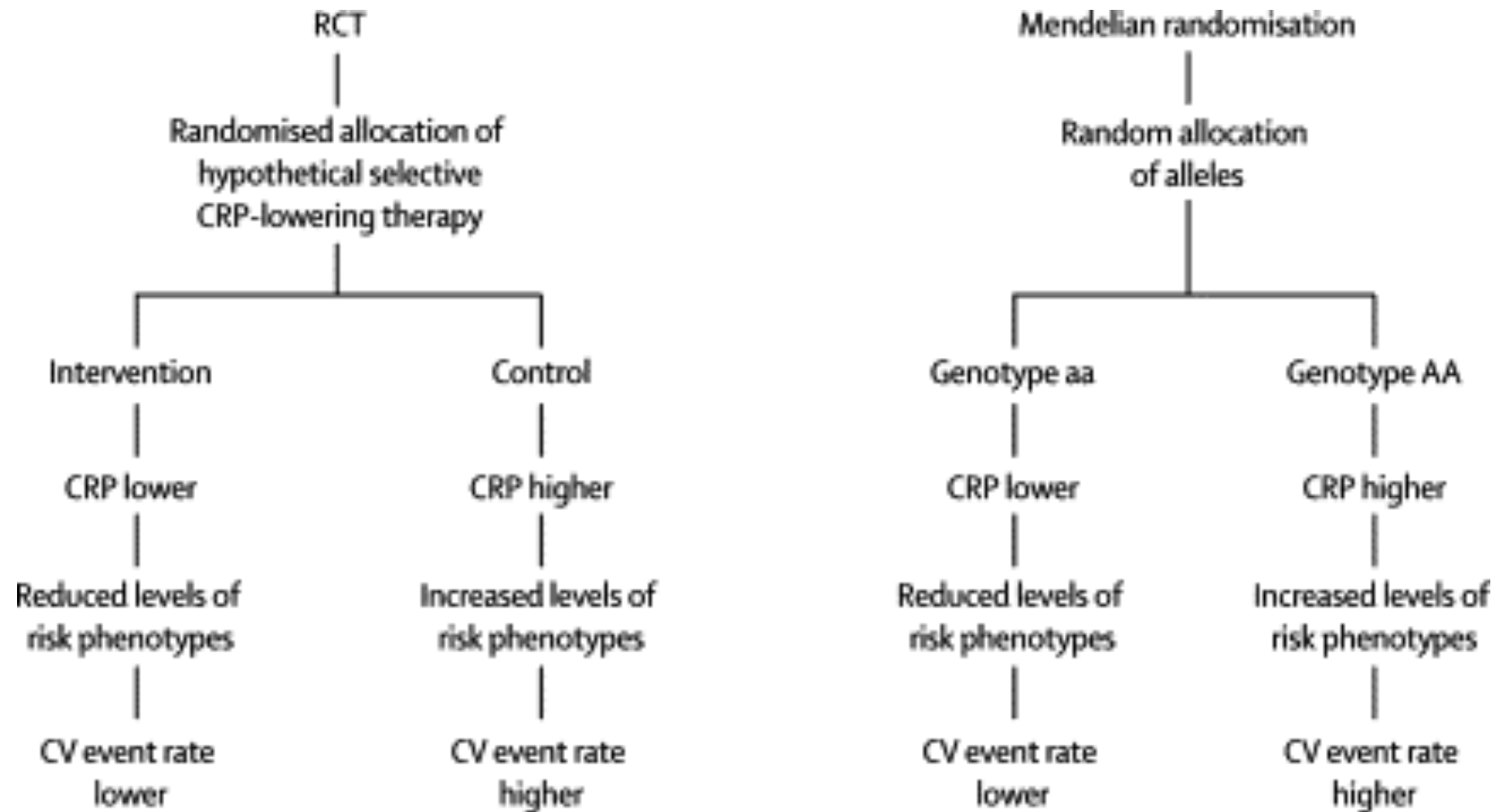
# The power of genetics



# Mendelian Randomization

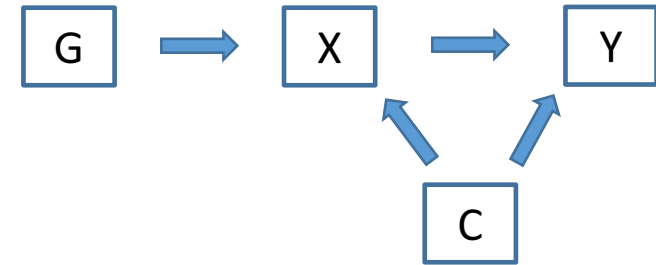
- *Basic principle: “genetic variants which mirror the biological effects of a modifiable environmental exposure and alters disease risk should be associated with disease risk to the extent predicted by their influence on exposure to the risk factor.”*
- The random allocation of genetic variants from parents to offspring means these variants will generally be unrelated to other factors which affect the outcome.
- Furthermore, associations between the genotype and the outcome will not be affected by reverse causation because disease does not affect genotype

Possible effects of C-reactive protein (CRP) on cardiovascular (CV) events. Expected outcome from hypothetical randomized clinical trial of selective CRP-lowering intervention, and from Mendelian randomization analysis, if CRP were causal in developing CV.



# Three key assumptions in MR analysis

1. G (SNP or a combination of multiple SNPs) is robustly associated with X (risk factor)
2. G is unrelated to any confounders C, that can bias the relationship between G and Y (outcome). In other words, there are no common causes of G and Y (e.g. population stratification)
3. G is related to Y only through its association with X (i.e. no pleiotropy)



# Assumption 1: G is robustly associated with X

- Under certain conditions, the relative bias of the instrument variable (IV) estimate is  $\sim 1/F$ . A “weak” IV has been defined as having  $F < 10$ , where

$$F = \frac{R^2(n - 1 - k)}{(1 - R^2)k}$$

$R^2$  is variance in X explained by the IV(s),  
n is sample size and k is number of IVs

- Weak IVs can lead to biased effect estimates (in the direction of the observed X-Y association) in the presence of confounding of the X–Y relationship.

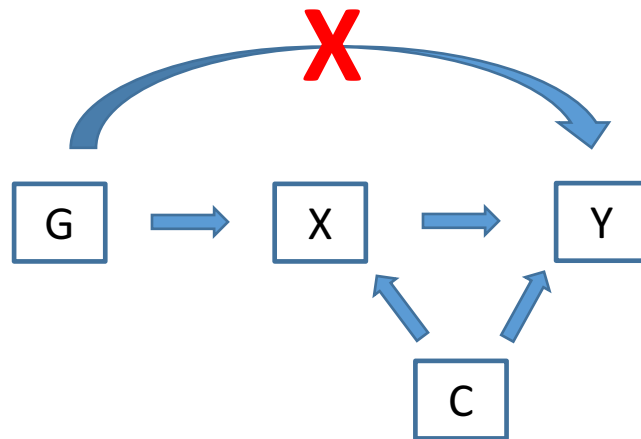
# Assumption 2: No confounding

- G is independent of factors (measured and unmeasured) that confound the X-Y relation
- Since G is randomized at birth and thus is independent of non-genetic confounders and is not modified by the course of disease, the one main concern here is population stratification – i.e. if ancestry is related both to G and Y.
- If you have individual-level data, you can test for this (e.g. PCA)



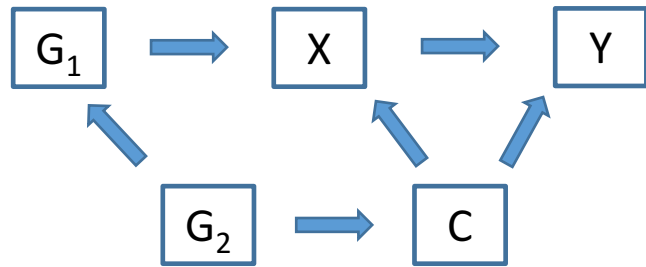
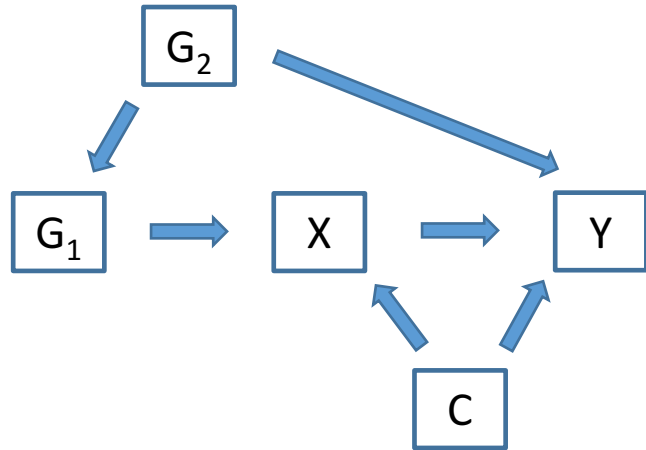
# Assumption 3: No pleiotropy

- This assumption is the trickiest
- Assumes that G is only associated with Y via X and thus the association between G and Y is fully mediated by X and not through any unmeasured factor(s). Needs to be true for SNPs in LD too

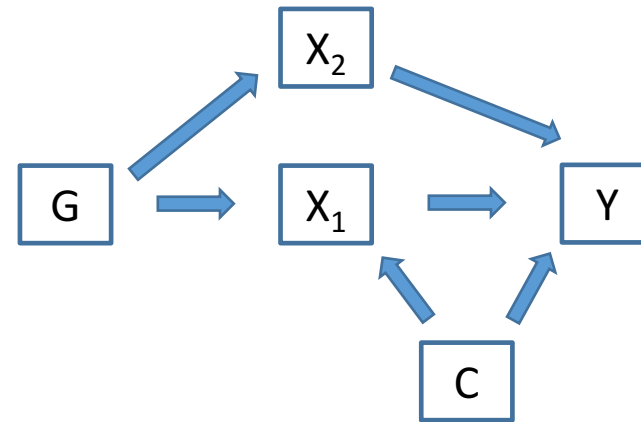
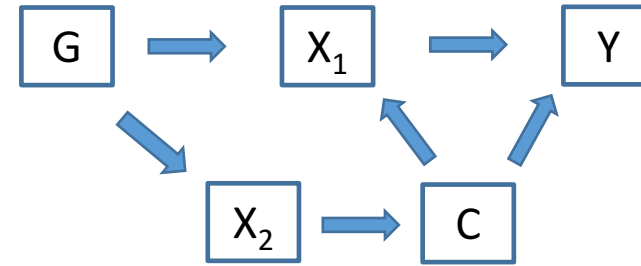


# Scenarios invalidating assumption 3

LD



Pleiotropy



# Best (but oft-forgotten) practices: the design, analysis, and interpretation of Mendelian randomization studies<sup>1</sup>

*Philip C Haycock,<sup>2\*</sup> Stephen Burgess,<sup>3</sup> Kaitlin H Wade,<sup>2</sup> Jack Bowden,<sup>2,4</sup> Caroline Relton,<sup>2</sup> and George Davey Smith<sup>2</sup>*

**TABLE 2**

Different design strategies for MR<sup>1</sup>

Study design	Test	Comments
G-X + G-Y	Implies $X \rightarrow Y$	No estimation of magnitude of causal effect
One-sample MR	Various hypotheses	Requires individual-level data; lower power; MR estimates are biased toward the confounded observational association by weak instruments
Two-sample MR	Various hypotheses	Individual-level or summary data; greater power (due to greater potential sample sizes); MR estimates are biased toward the null by weak instruments
Bidirectional MR	$X \rightarrow Y$ and $Y \rightarrow X$	Assesses causation in both directions
Two-step MR	$X \rightarrow M \rightarrow Y$	Tests mediation in a causal pathway
G×E	$X \rightarrow Y$ (relation is dependent on environment variable)	Able to detect direct effects (a violation of assumption 2 of MR)

<sup>1</sup>G×E, gene-environment interaction; G-X, SNP-exposure association; G-Y, SNP-outcome association, M, mediator; MR, Mendelian randomization; SNP, single nucleotide polymorphism; X, hypothesized exposure; Y, outcome variable of interest.

# Individual-level data in one sample

- Access to SNPs, risk factor, and outcome for all participants
- The causal effect of  $X$  on  $Y$  can be estimated using 2-stage least-squares (2SLS) regression:
  1.  $X = a + \gamma G$
  2.  $Y = c + \beta X^*$ , where  $X^*$  are the genetically predicted exposure levels as measured in (1)
- The causal estimate is given by  $\beta$
- Can be implemented in R using the “ivpack” package
- Weak instruments cause bias towards the observed confounded association

# Summary data from two samples

- The G-X and the G-Y associations are estimated in two different samples.
- Assumes no overlap among samples and that the two populations are similar (ethnicity, age, sex, etc.)
- Here, bias due to weak IVs will be towards the null
- Note: The G-X and G-Y associations need to be coded using the same effect allele

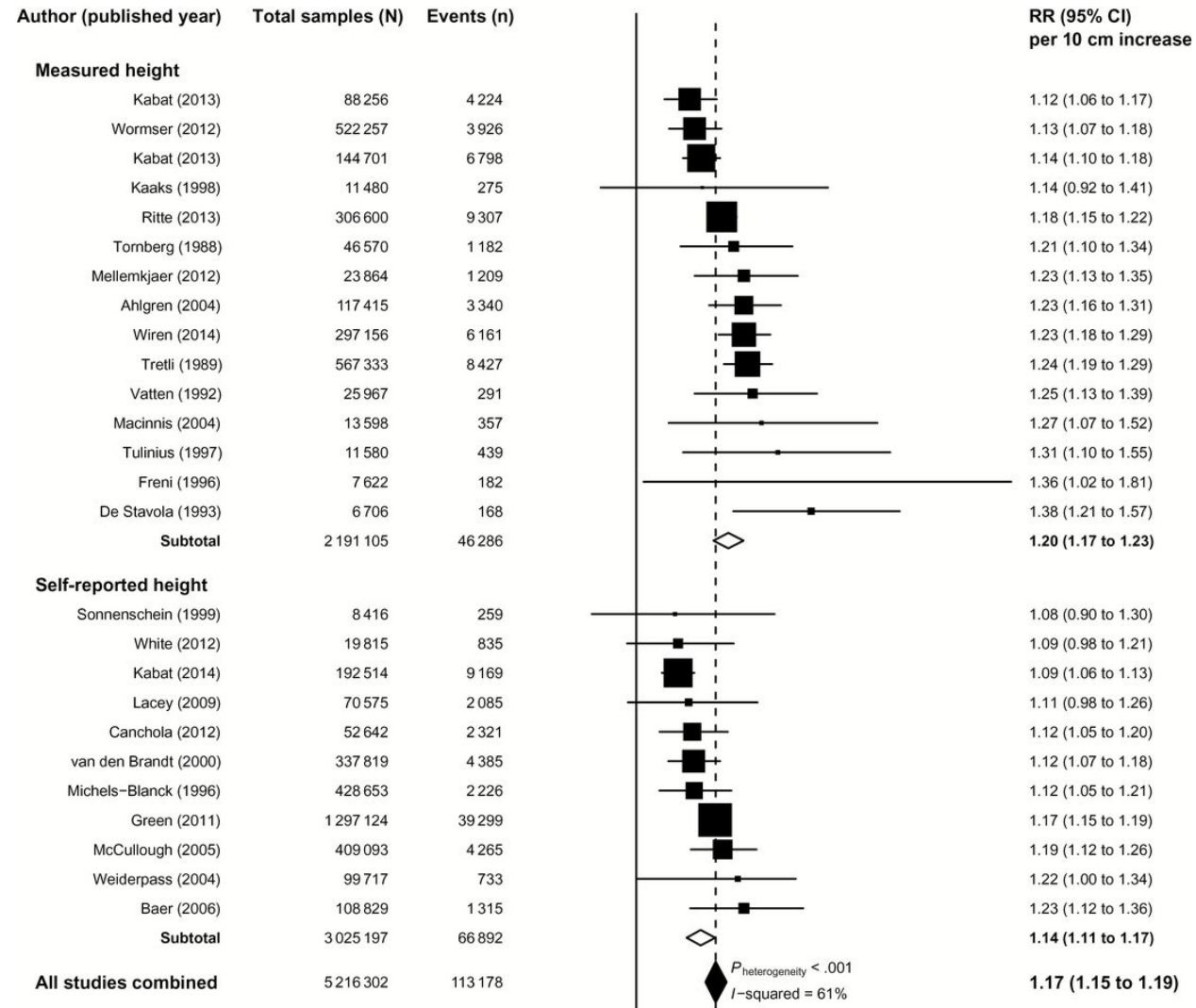
# Summary data from two samples

$$\hat{\beta} = \frac{\sum_k \beta_{1k} \beta_{2k} \sigma_{\beta_{2k}}^{-2}}{\sum_k \beta_{1k} \sigma_{\beta_{2k}}^{-2}}$$

$$se(\hat{\beta}) = \sqrt{\frac{1}{\sum_k \beta_{1k}^2 \sigma_{\beta_{2k}}^{-2}}}$$

$\beta_{1k}$  is the mean change in X per allele for SNP k,  $\beta_{2k}$  is the mean change in Y per allele for SNP k,  $\sigma_{\beta_{2k}}^{-2}$  is the inverse variance for the G-Y association.

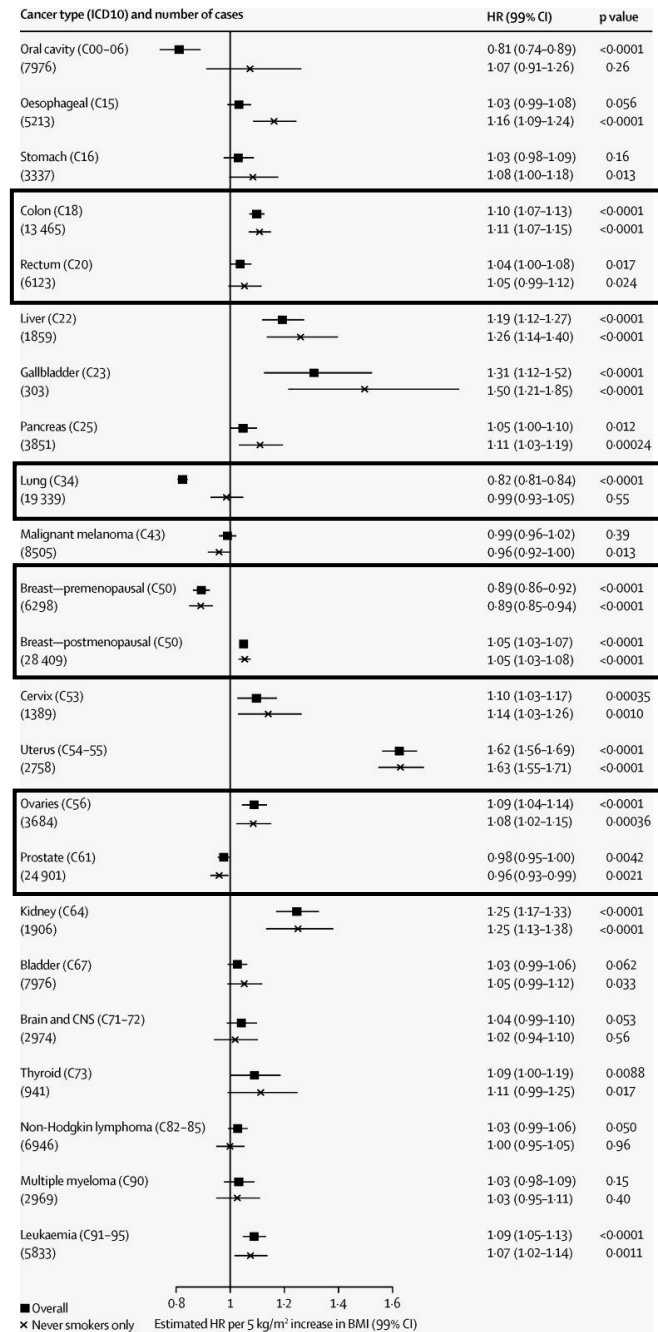
# Meta-analysis of associations between height and risk of breast cancer in prospective cohort studies.



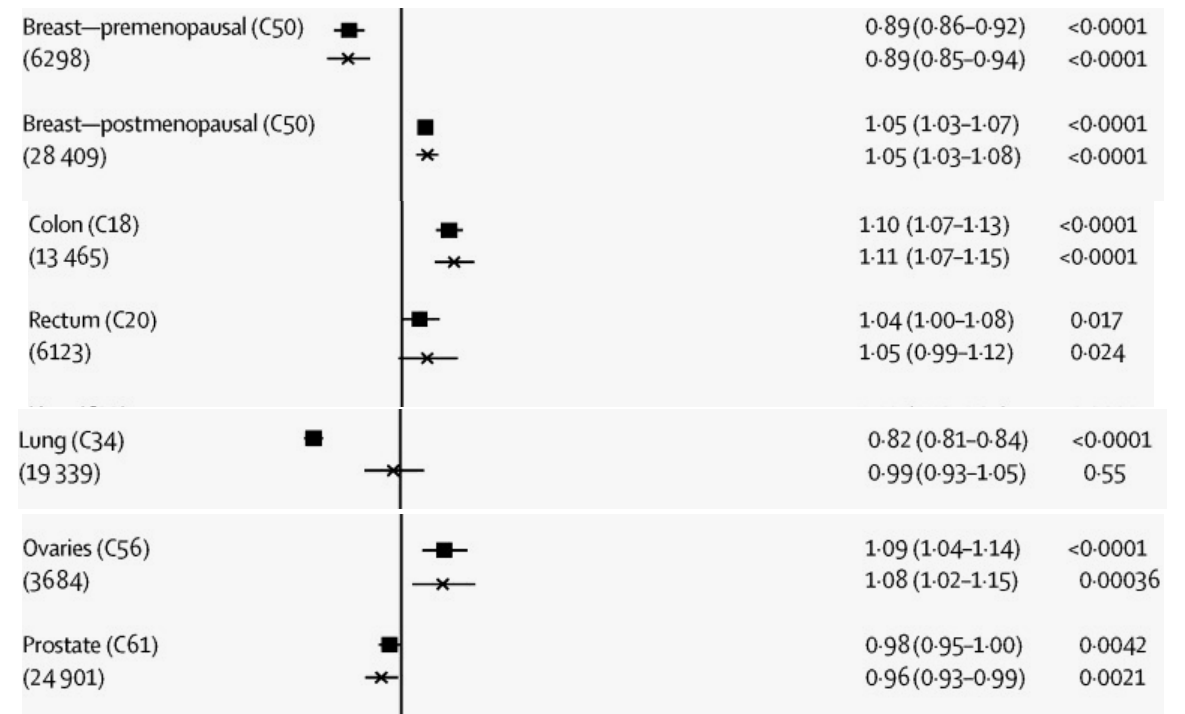
**Table 3.**  
Association of height and breast cancer risk in women

Breast cancer group	Meta-analysis of prospective studies			Breast Cancer Association Consortium			Breast Cancer Association Consortium		
	N/events	Observational estimate RR (95% CI)*	P	Case patients/ control subjects	Instrumental variable estimate OR (95% CI)*	P	Case patients/ control subjects	Observational estimate OR (95% CI)*	P
All women combined									
All case patients	5216302/113178	1.17 (1.15 to 1.19)	<.001	46325/42482	1.22 (1.13 to 1.32)	<.001	30248/20458	1.13 (1.10 to 1.16)	<.001
By menopausal status									
Premenopausal	2801907/15439	1.16 (1.12 to 1.21)	<.001	10209/9053	1.29 (1.07 to 1.56)	.007	8959/6225	1.11 (1.05 to 1.17)	<.001
Postmenopausal	3111070/63606	1.17 (1.14 to 1.21)	<.001	23069/19355	1.32 (1.17 to 1.49)	<.001	20197/13311	1.14 (1.10 to 1.18)	<.001
<i>P</i> interaction			.79			.86			.35
By ER status									
ER-positive	433810/7947	1.18 (1.13 to 1.23)	<.001	27074/42482	1.26 (1.14 to 1.38)	<.001	19953/20458	1.16 (1.12 to 1.20)	<.001
ER-negative	433810/1845	1.00 (0.87 to 1.13)	.95	7288/42482	1.02 (0.87 to 1.18)	.84	4810/20458	1.05 (1.00 to 1.10)	.07
<i>P</i> interaction			.02			.02			.002

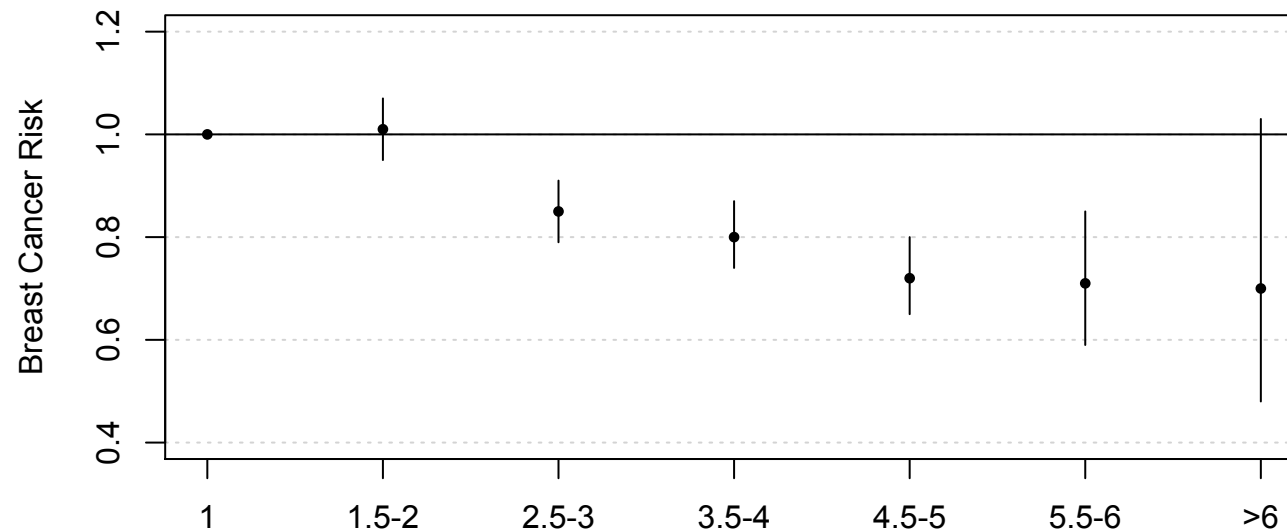
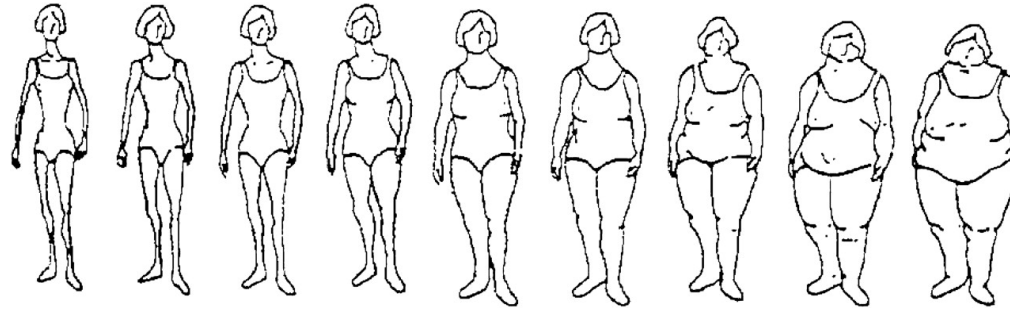




- Association between BMI and cancer risk was assessed for 22 cancers
- 5.24 million individuals (166,996 cancer cases)



# Childhood body fatness is inversely associated with breast cancer risk

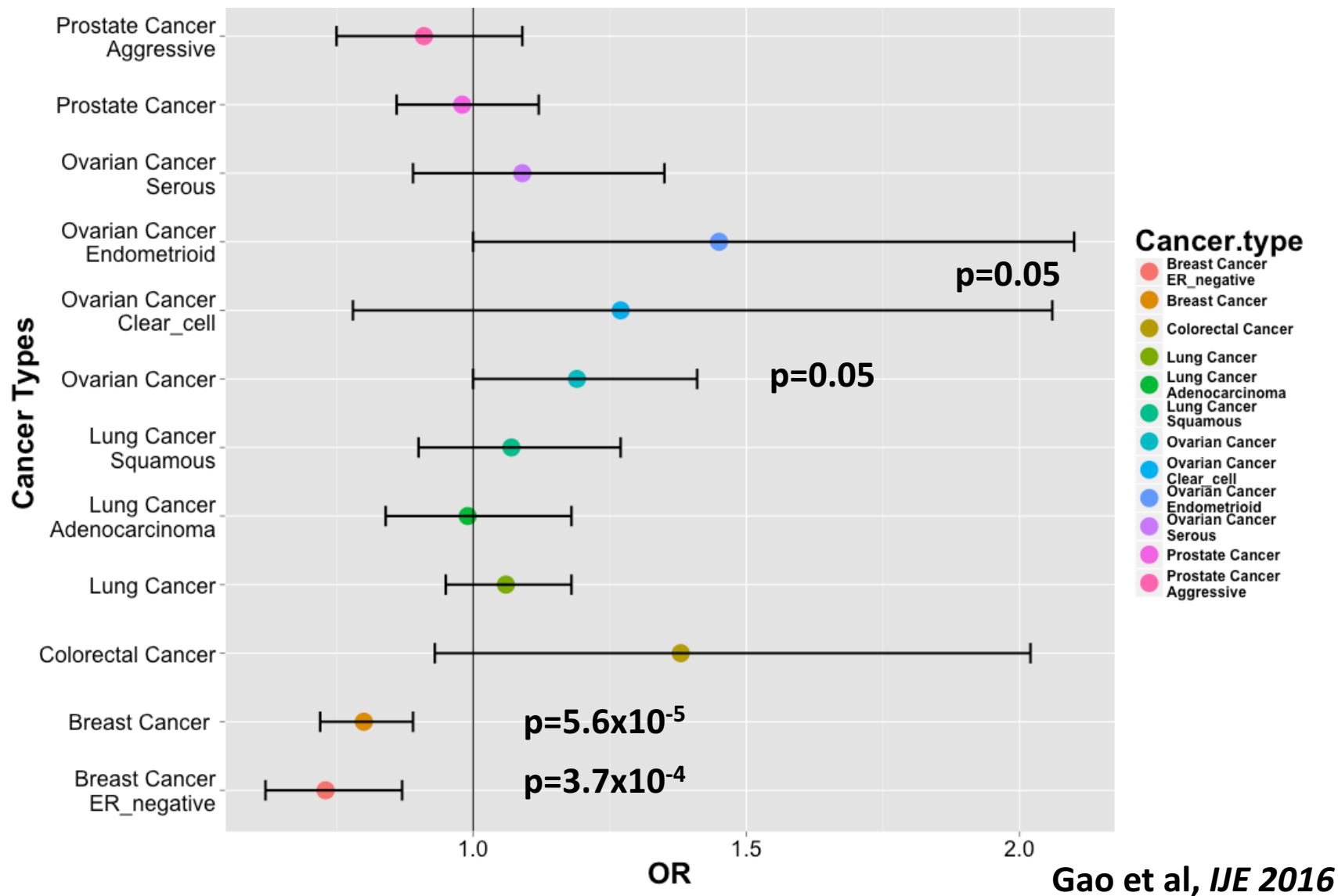


# Expansion to other cancer types within GAME-ON

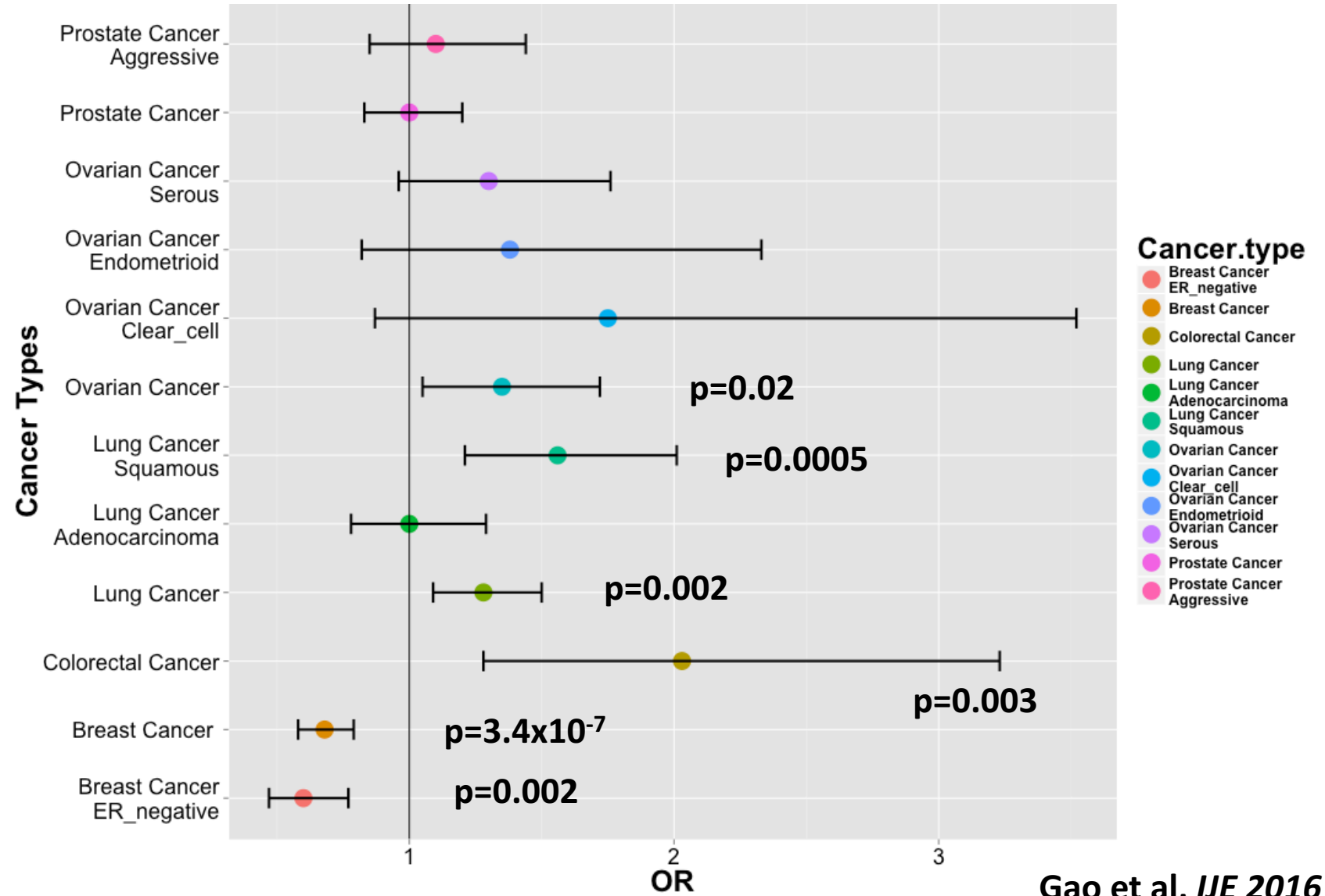
Cancer Type	Cases	Controls	GWAS studies
<b>Breast</b>			
All	15,569	18,204	11
ER-negative	4,760	13,248	8
<b>Colorectal</b>	5,100	4,831	6
<b>Lung<sup>a</sup></b>			
All	12,527	17,285	6
Adenocarcinoma	3,804	16,289	6
Squamous	3,546	16,434	6
<b>Ovarian<sup>a</sup></b>			
All	4,369	9,123	3
Clear-cell	356	9,123	3
Endometrioid	715	9,123	3
Serous	2,556	9,123	3
<b>Prostate</b>			
All	14,160	12,712	6
Aggressive	4,446	12,724	6
<b>Total</b>	<b>51,725</b>	<b>62,155</b>	

Gao et al, *IJE* 2016

# Childhood body fatness (9 SNPs)



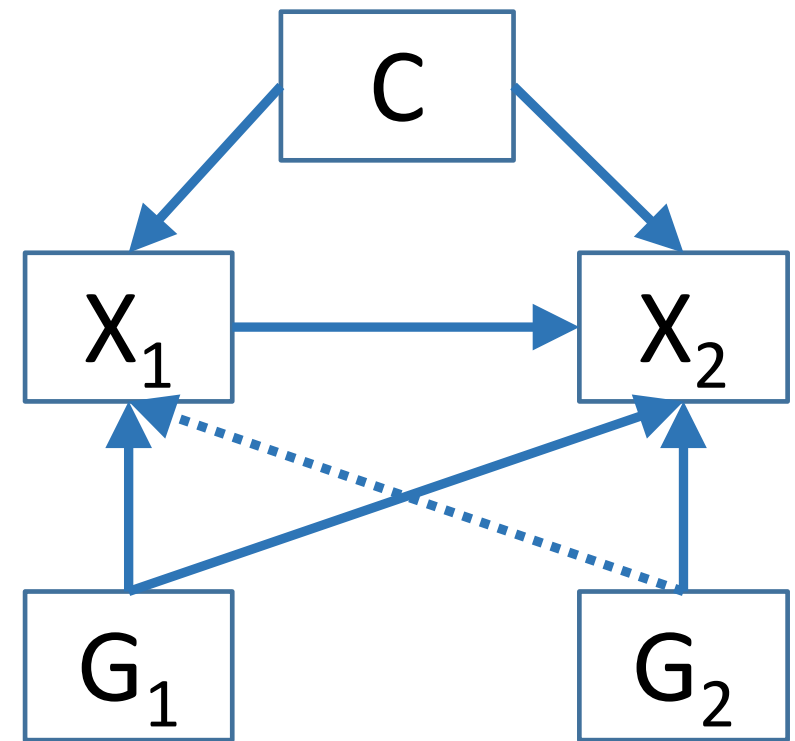
# Adult BMI (77 SNPs)



# Bidirectional MR analysis

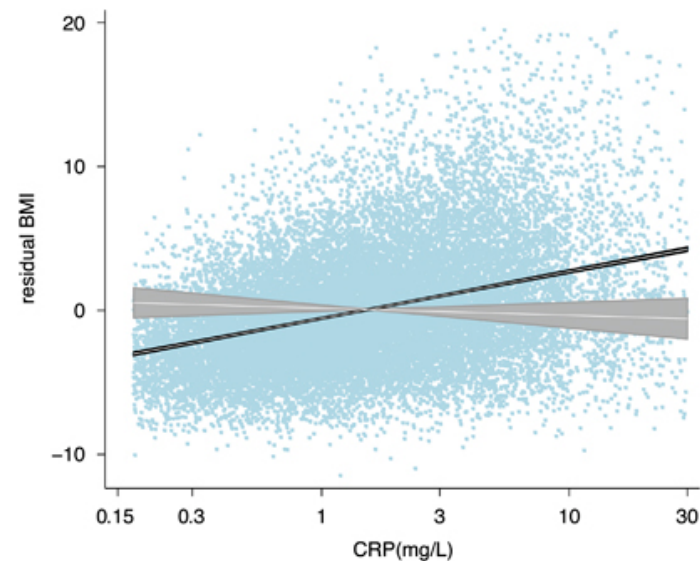
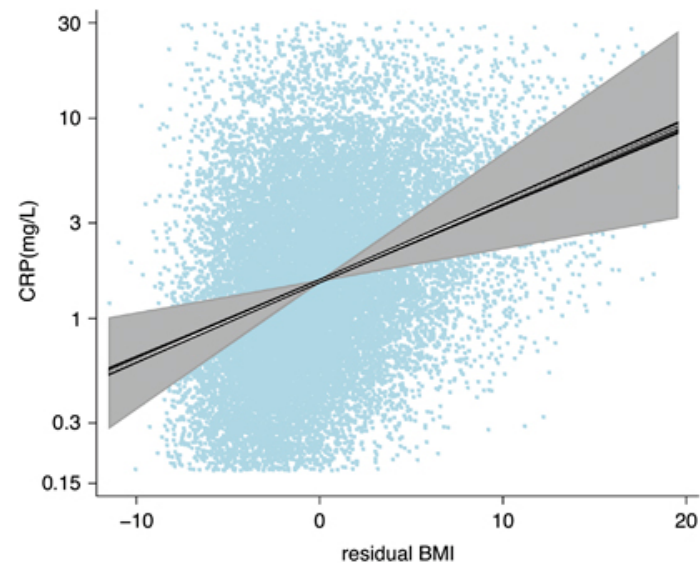
- Approach to overcome reverse causation
- IVs for both  $X_1$  and  $X_2$  are used to assess the causal association in both directions
  1. Is  $G_1$  associated with  $X_2$ ?
  2. Is  $G_2$  associated with  $X_1$ ?

(Also confirm that  $G_1$  is associated with  $X_1$  and that  $G_2$  is associated with  $X_2$ )



# BMI and CRP – what causes what?

- There is a consistent observed association between high BMI and high CRP levels



Light grey points represent a scatter plot of the correlation between circulating CRP and residual BMI. Gray areas represent 95% confidence regions around IV estimates. Black area represents 95% confidence regions around simple linear regression estimates.

- These data suggest that the observed association between circulating CRP and measured BMI is likely to be driven by BMI, with CRP being a marker of elevated adiposity.

**Table 4. Relationships between genotypic variation and BMI and circulating CRP**

		<i>FTO(rs9939609)</i>				<i>CRP(rs3091244)</i>			
	<i>TT</i>	<i>AT</i>	<i>AA</i>	<i>Per allele effect</i>	<i>P-value</i>				
BMI	26.07 (25.98, 26.17)	26.37 (26.29, 26.45)	26.73 (26.59, 26.87)	0.32 (0.24, 0.40)	<0.0001				
CRP	1.51 (1.48, 1.55)	1.55 (1.52, 1.58)	1.61 (1.56, 1.67)	1.03 (1.01, 1.05)	0.003				
	<i>CC</i>	<i>CT</i>	<i>TT</i>	<i>CA</i>	<i>AT</i>	<i>AA</i>	<i>Per allele effect</i>	<i>P</i>	
BMI	26.32 (26.23, 26.41)	26.36 (26.27, 26.44)	26.24 (26.07, 26.42)	26.25 (26.02, 26.47)	26.29 (25.98, 26.61)	27.15 (26.02, 28.28)	-0.01 (-0.06, 0.04)	0.7	
CRP	1.37 (1.34, 1.40)	1.61 (1.57, 1.64)	1.82 (1.74, 1.90)	1.71 (1.62, 1.81)	2.11 (1.95, 2.28)	2.56 (1.95, 3.37)	1.11 (1.10, 1.13)	<0.0001	

**Table 5. Observational and instrumental variable derived relationships between BMI and circulating CRP.**

<i>Outcome/explanatory variable</i>	<i>Effect estimates</i>				
	<i>Observational</i>	<i>Instrumental variable</i>	<i>P<sub>IV</sub></i>	<i>P<sub>diff</sub></i>	<i>F<sub>first</sub></i>
CRP/BMI	1.46 (1.44, 1.48)	1.41 (1.10, 1.80)	0.006	0.8	31.1
BMI/CRP	1.03 (1.00, 1.07)	-0.24 (-0.58, 0.11)	0.2	<0.0001	57.3

Abbreviations: BMI, body mass index; CI, confidence interval; CRP, C-reactive protein.

Observational analysis effects (95% CI) derived from linear regression adjusted for sex, age, age squared, age-sex interaction, log(height), smoking, drinking, education and income.

CRP is log transformed for analyses above and effects on CRP are shown as ratios of geometric means for a s.d. increase in BMI.

BMI effects are expressed as kg m<sup>-2</sup> for a doubling in logCRP.

Instrumental variable derived estimates of the same effects include the same covariates.

*P<sub>IV</sub>* is the *P*-value from a test that the instrumental variable estimate is equal to the null.

*P<sub>diff</sub>* is the *P*-value from a test for difference between the observational and instrumental variable estimates.

*F<sub>first</sub>* is the first stage F-statistic from instrumental variable analysis.



# Drawbacks with MR analysis

- Large sample sizes are needed!
- As genetic effects on risk factors are typically small, MR estimates of association have much wider confidence intervals than conventional epidemiological estimates.
- Make sure that the three key assumptions hold!